

Effects of Microstructure and Chemistry on Ignition Sensitivity of Polymer-bonded Explosives Under Shock Loading

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What are High Explosives?

- High Explosives (HEs) and their detonation properties have been an important field of study following WWII.

➤ **High explosives** refer to explosive materials that detonate (i.e. supersonic shock fronts pass through material).

VS.

➤ **Low explosives** are subsonic → Flame front propagated by deflagration.

- Applications include:

- **Solid rocket propellants**
- **Insensitive munitions**
- **Tunnel construction**
- **Demolition**
- **Explosives in nuclear weapons**



- Insensitive High Explosives

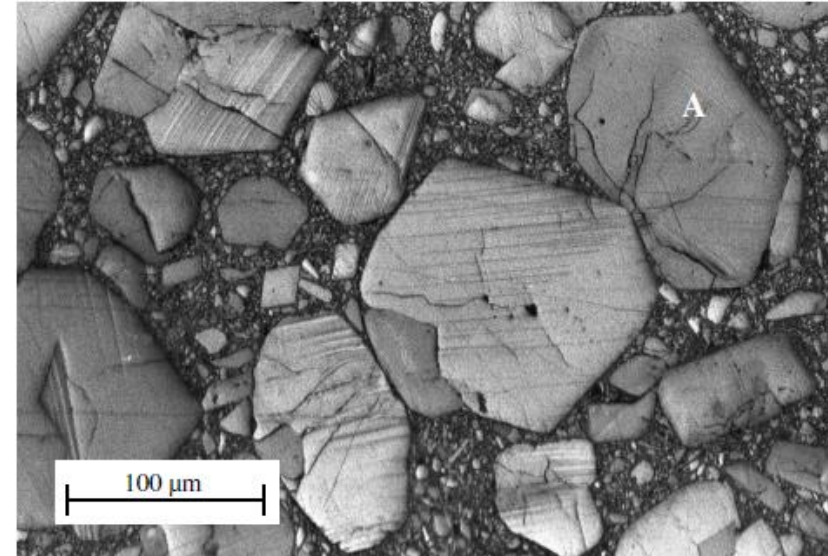
- Palomares B-52 Plane Crash, 1966



Polymer Bonded Explosive (PBX)

➤ Primarily composed of 2 or 3 parts:

- **Explosive Grains**
 - Brittle fracture under low pressure
 - Plastic deformation under high pressure
- **Binder**
 - Bonding between constituents
 - Viscoelastic behavior
 - Low stiffness
- **Additives**
 - Low sensitivity

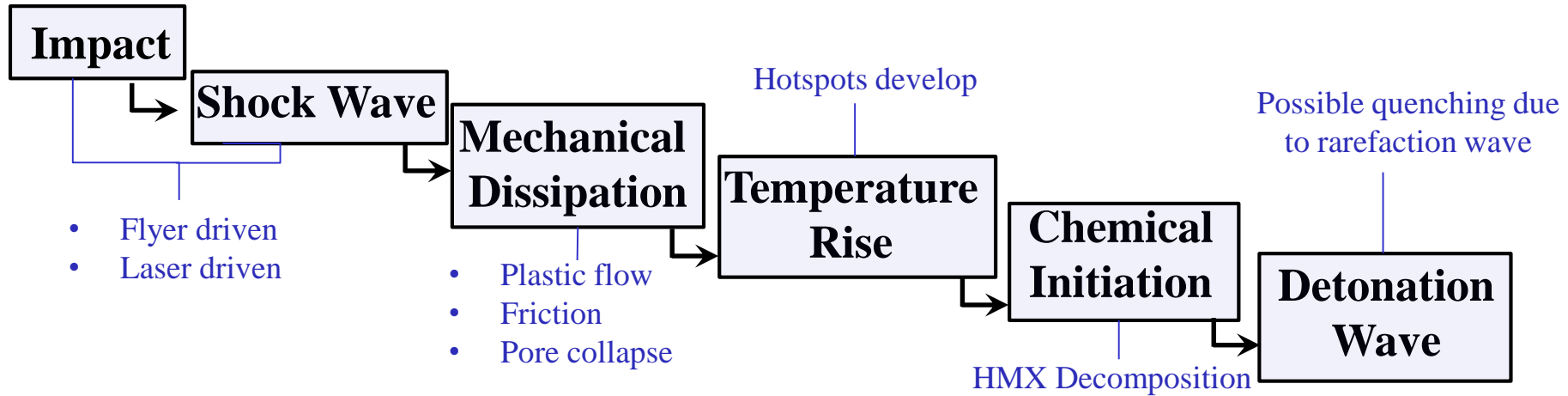


Rae *et al.*, 2002.

PBX constituents

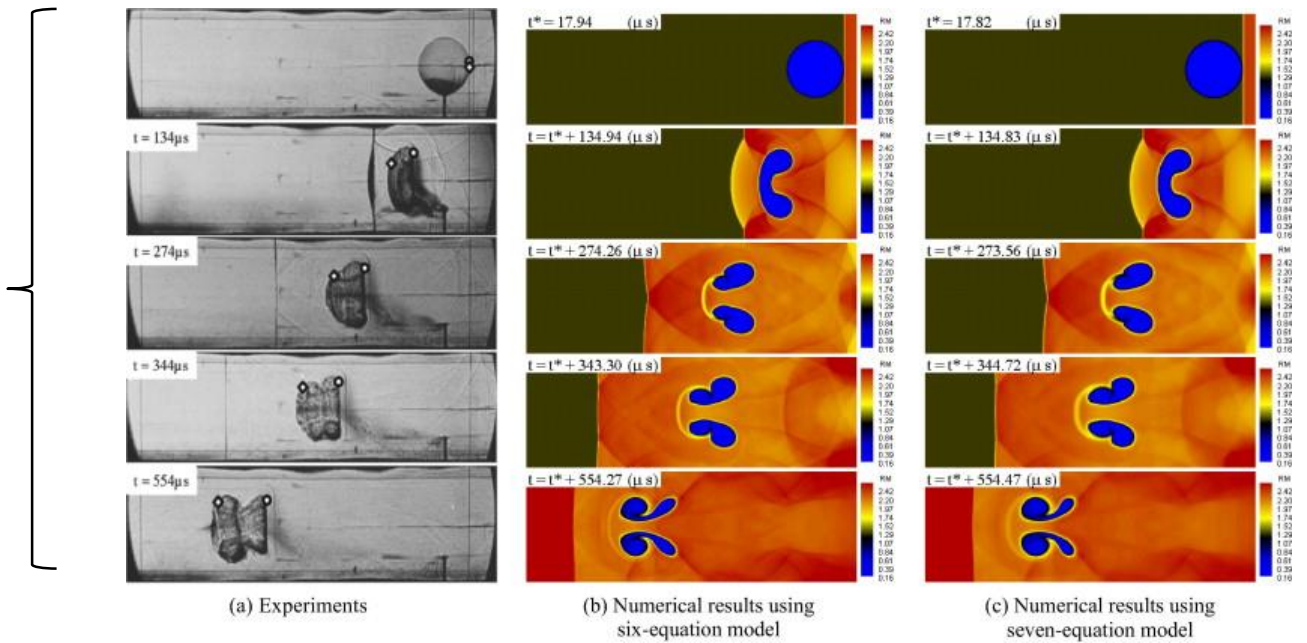
Explosive Grains	Binder Systems	Additives	
➤ HMX	➤ Estane	➤ Aluminum	PBX 9501
➤ RDX	➤ Viton	➤ Ammonium Perchlorate (AP)	
➤ PETN	➤ HTPB	➤ Wax	
➤ TATB	➤ Kel-F 800	➤ Inert Materials	
➤ HNS	➤ Polyurethane		

How do PBXs detonate?



Modeling shock with void in Fortran using Navier-stokes equations

Ha *et al.*, 2015.



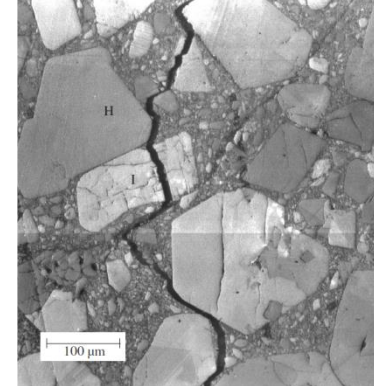
Development of Hotspots

- **Mechanical failure and interactions**
 - Inter-granular interactions
 - Trans-granular fractures
 - Debonding at grain-binder interface

- **Defects in microstructures**
 - Imperfectly bonded interfaces
 - Voids (Micropores)

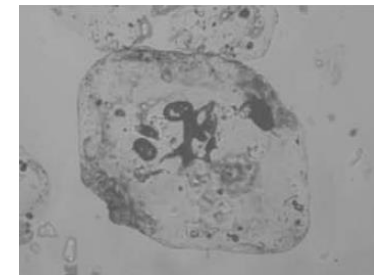
- **Shear bands** (plastic flow)
 - Localized heating along crystallographic slip planes

Rae et al., 2002.



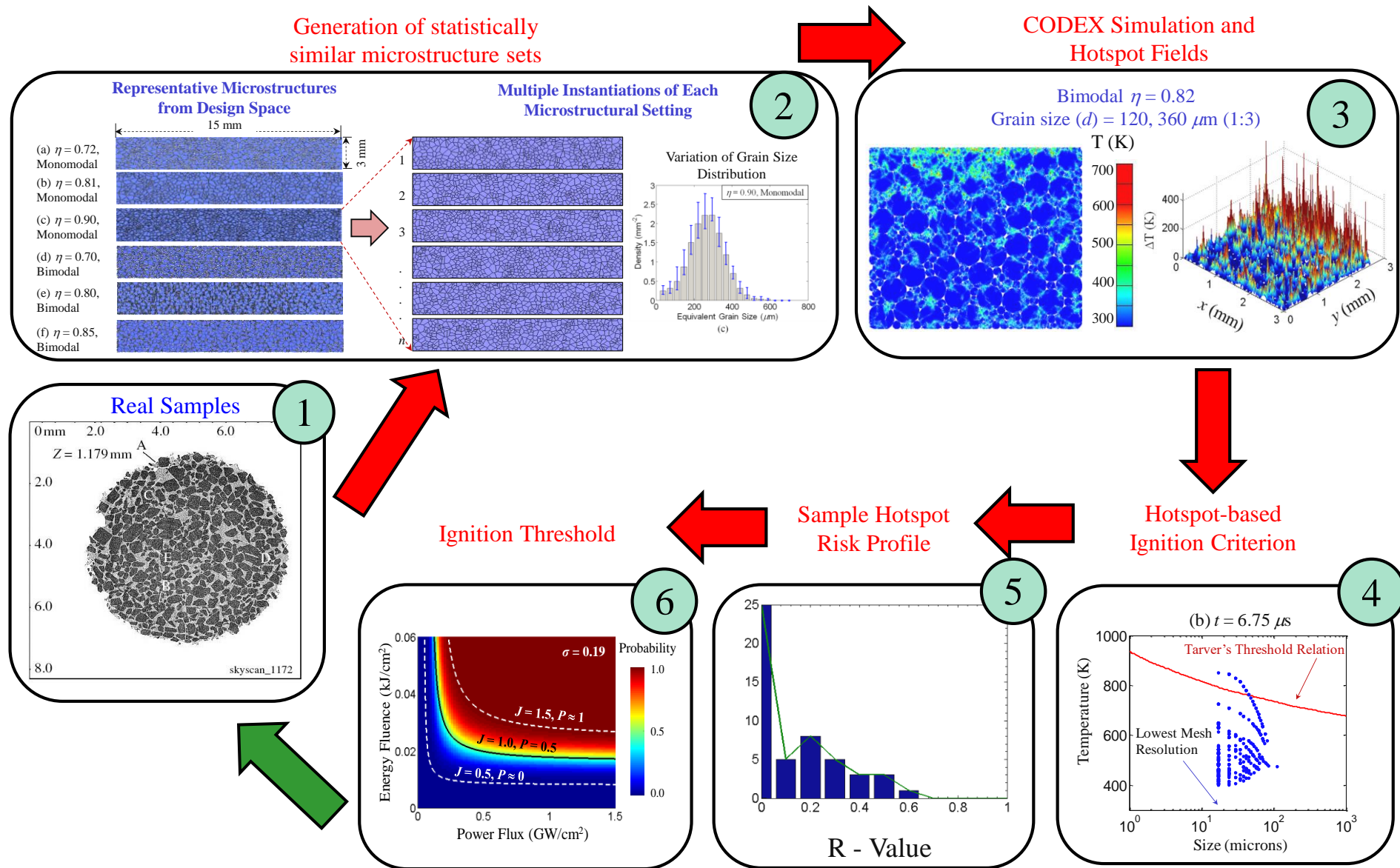
Fracture path

Czerski et al., 2007



Voids in RDX

CODEX Approach for Predicting Probabilistic Ignition Behavior of HEMs



Types of Microstructures Used

➤ Microstructural Effects

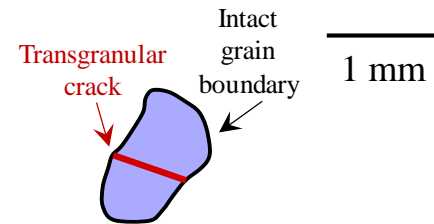
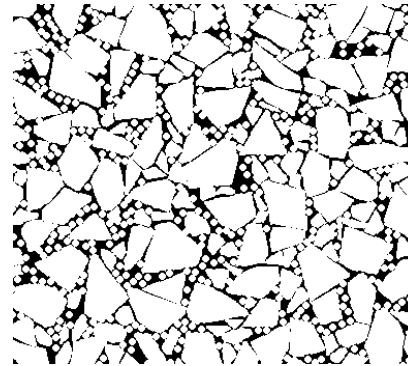
❖ Code is optimized to study the effects of mesoscale microstructural variables including the following:

- Microstructural heterogeneities
- Debonding
- Cracking
- Particulates
- Interfaces
- Various Types of dissipation

➤ Dissipation Mechanisms

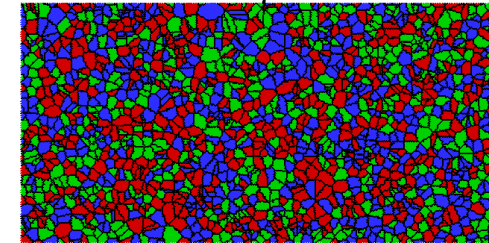
- | | |
|--------------------------|-----------------|
| • Elasto-viscoplasticity | • Fracture |
| • Viscoelasticity | • Friction |
| • Hyperelasticity | • Heat transfer |

PBX, Aluminized PBX

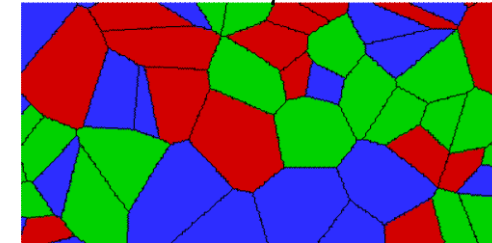


Granular EM Beds

$d = 35 \mu\text{m}$

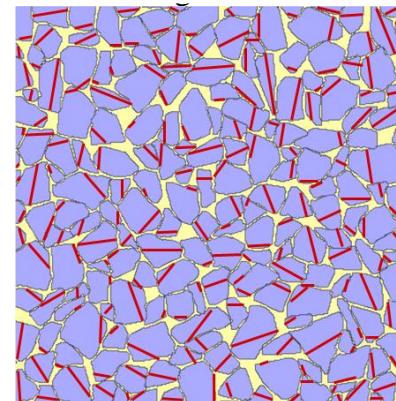


$d = 220 \mu\text{m}$



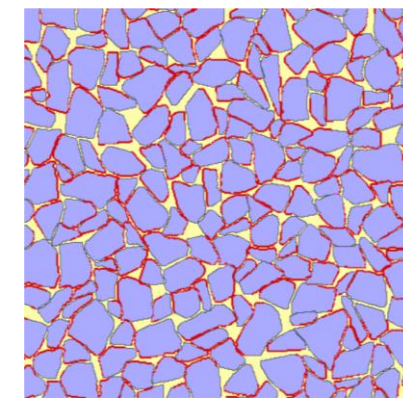
0.5 mm

Transgranular Cracks



1 mm

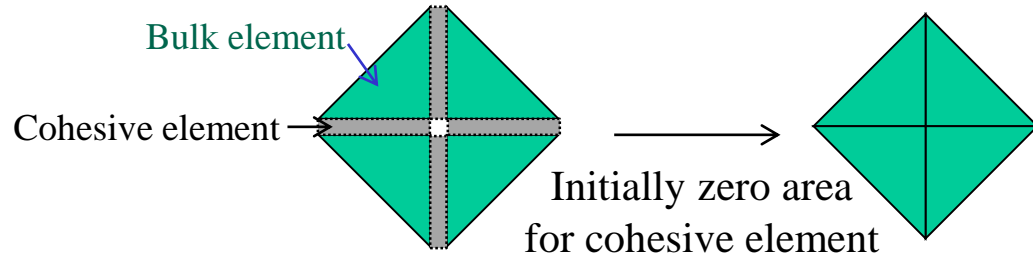
Debonding



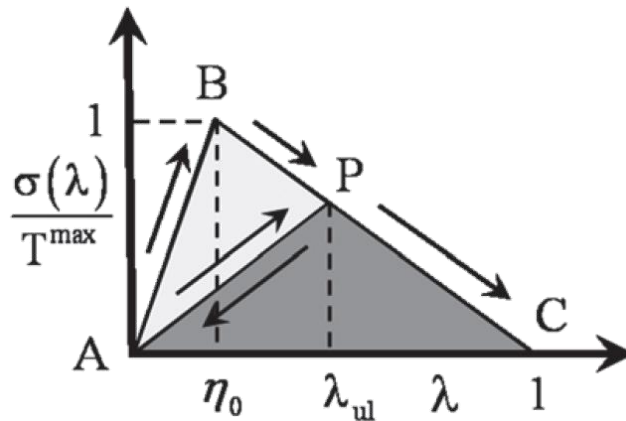
1 mm

CODEX Setup

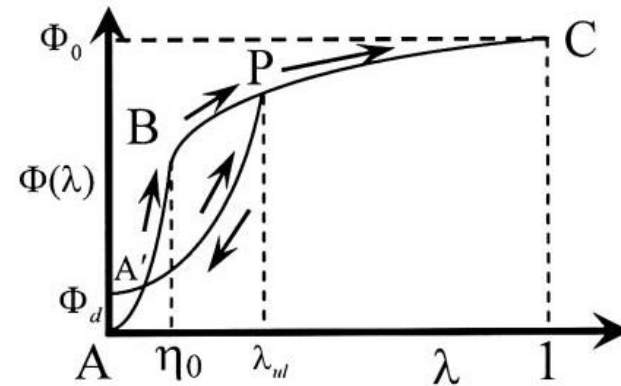
Cohesive FEM



Element configuration (bulk/cohesive element)

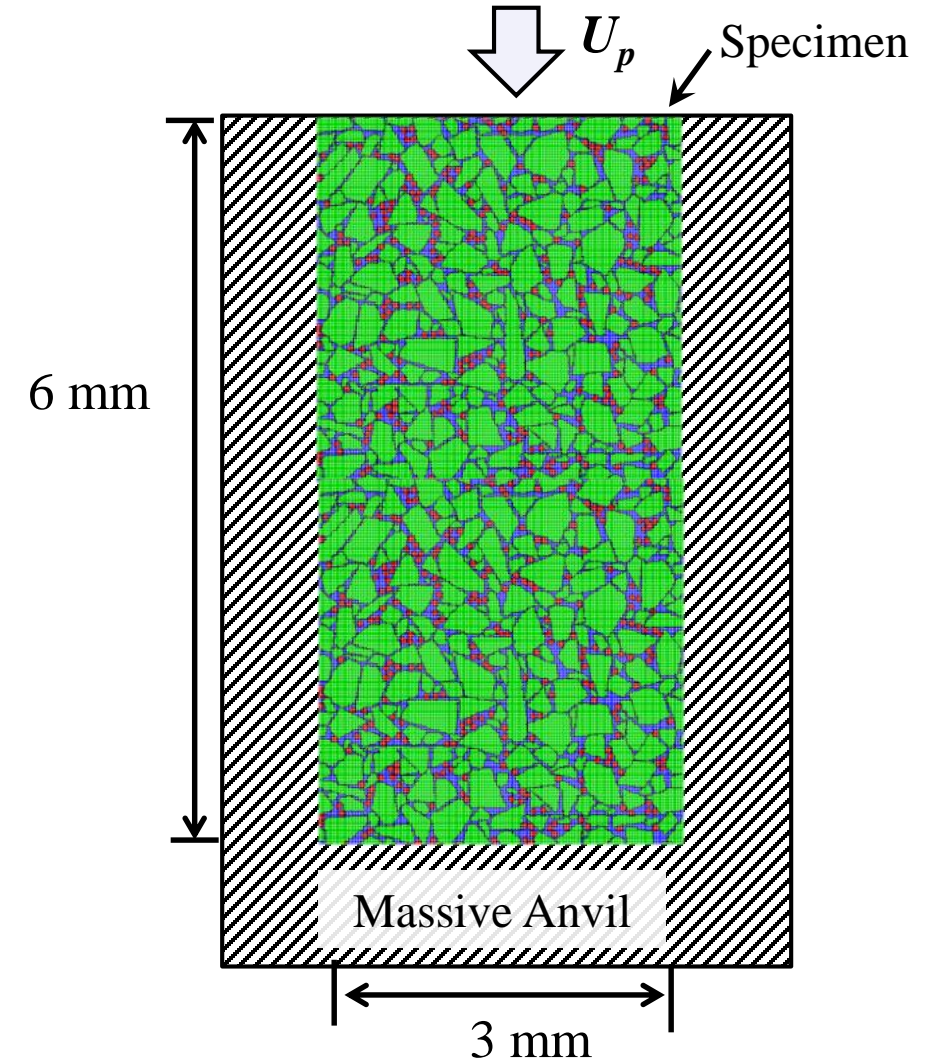


Bilinear traction-separation



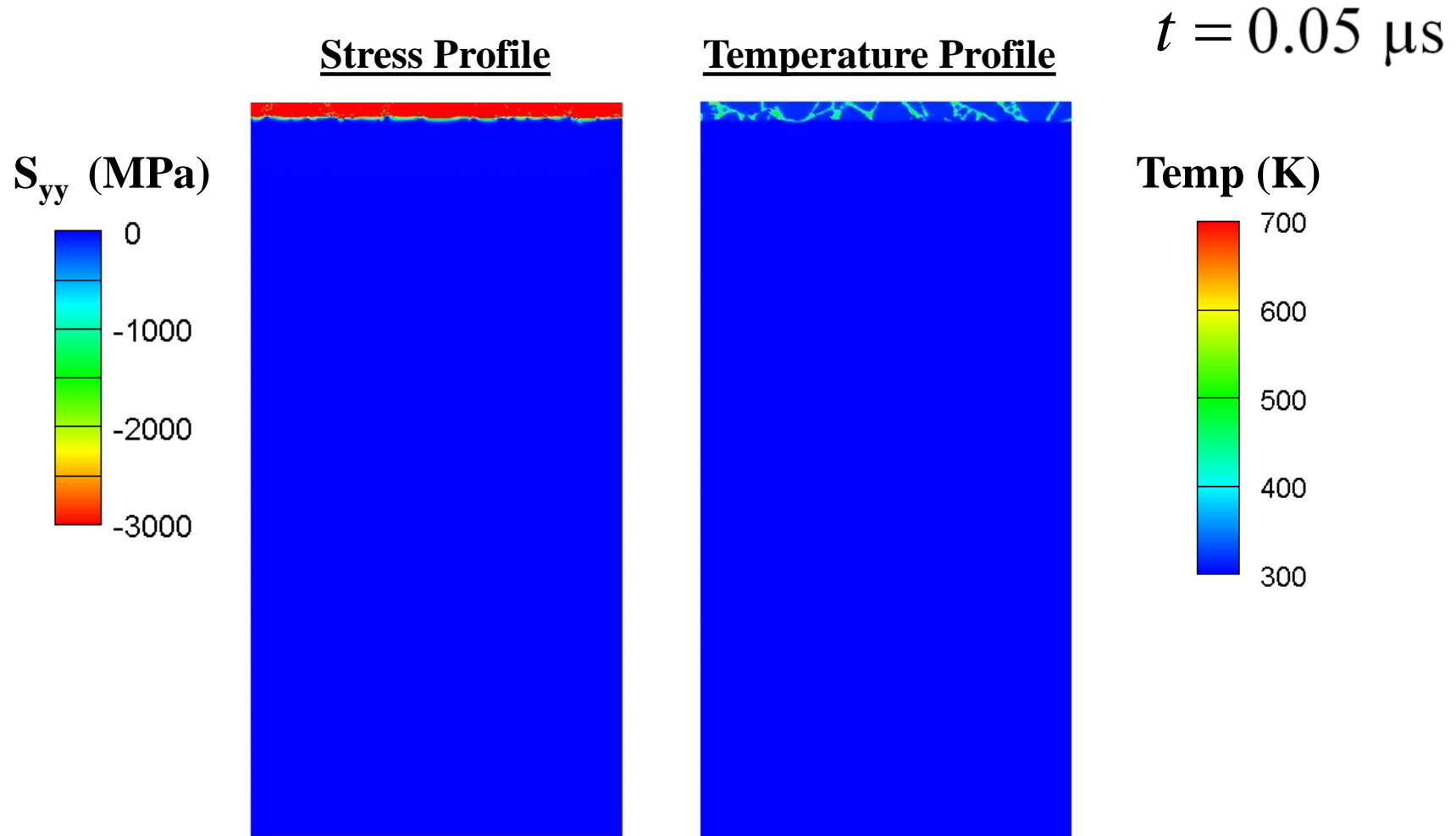
Cohesive energy

Loading Conditions



Temperature Field Evolution (high flyer velocity)

$$U_p = 500 \text{ m/s}, \Delta t_{\text{pulse}} = 280 \text{ ns}, 6\% \text{ Al}$$

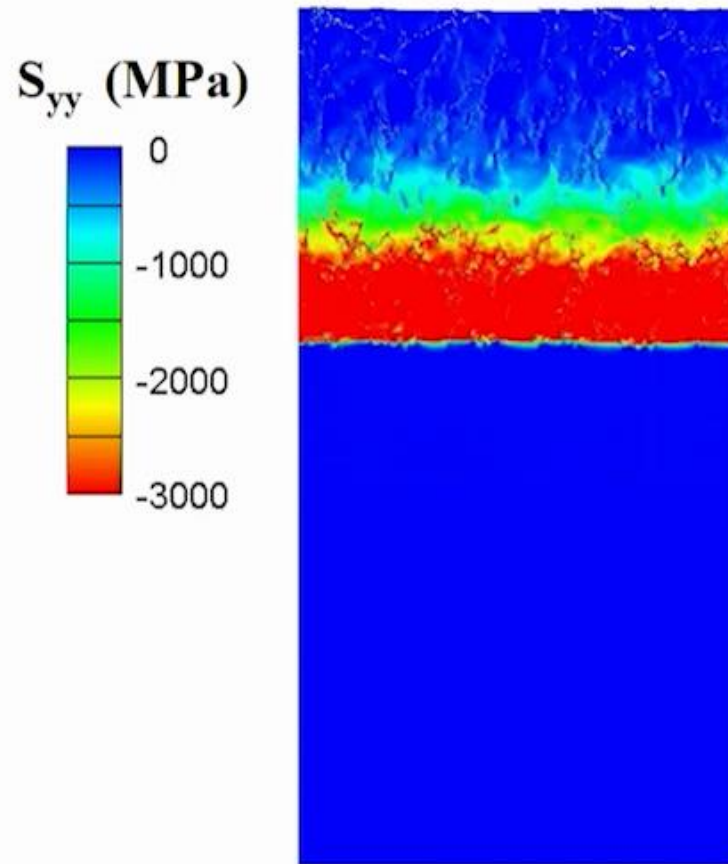


Temperature Field Evolution (high flyer velocity)

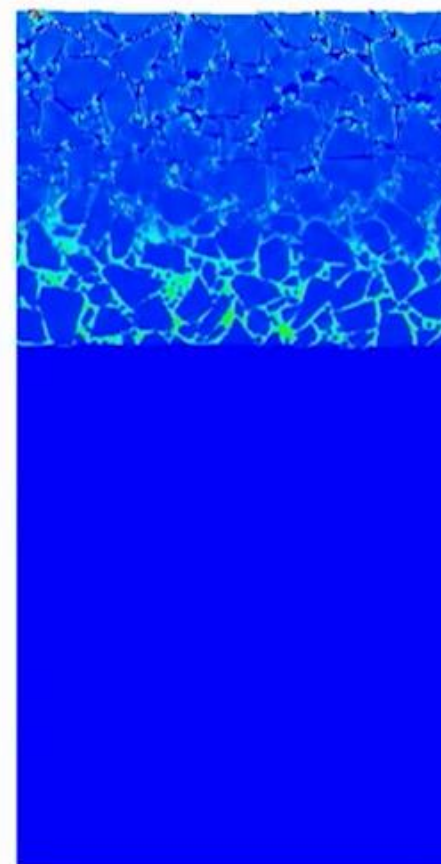
$$U_p = 500 \text{ m/s}, \Delta t_{\text{pulse}} = 280 \text{ ns}, 6\% \text{ Al}$$

$$t = 0.65 \mu\text{s}$$

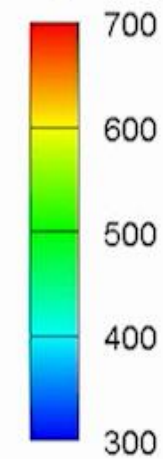
Stress Profile



Temperature Profile



Temp (K)



Temperature Field Evolution (high flyer velocity)

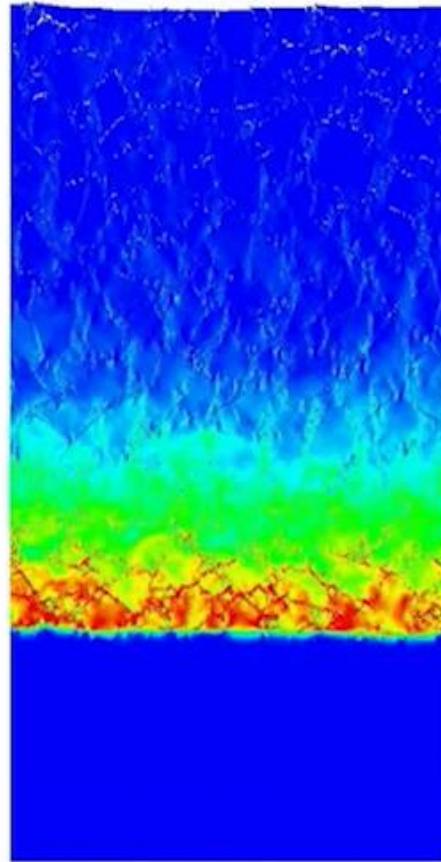
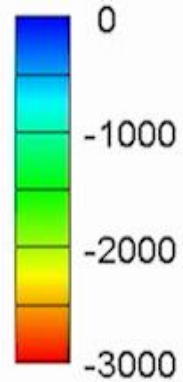
$$U_p = 500 \text{ m/s}, \Delta t_{\text{pulse}} = 280 \text{ ns}, 6\% \text{ Al}$$

$$t = 1.20 \mu\text{s}$$

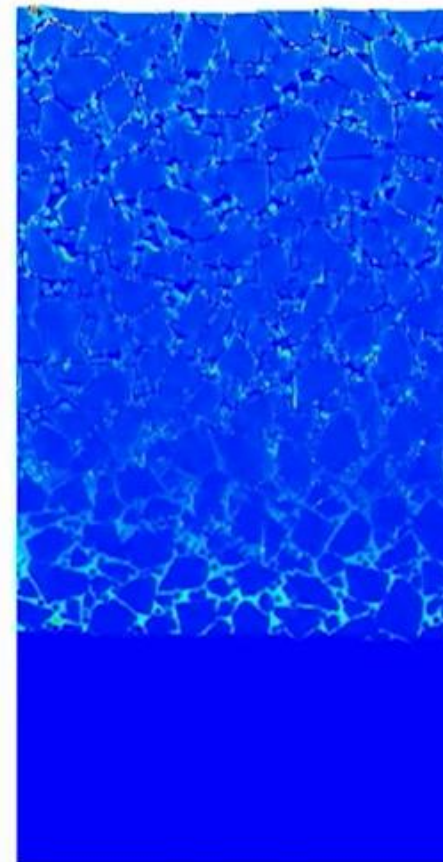
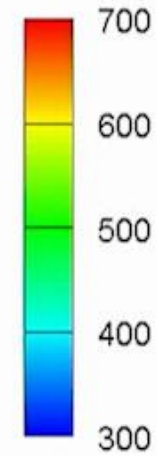
Stress Profile

Temperature Profile

S_{yy} (MPa)

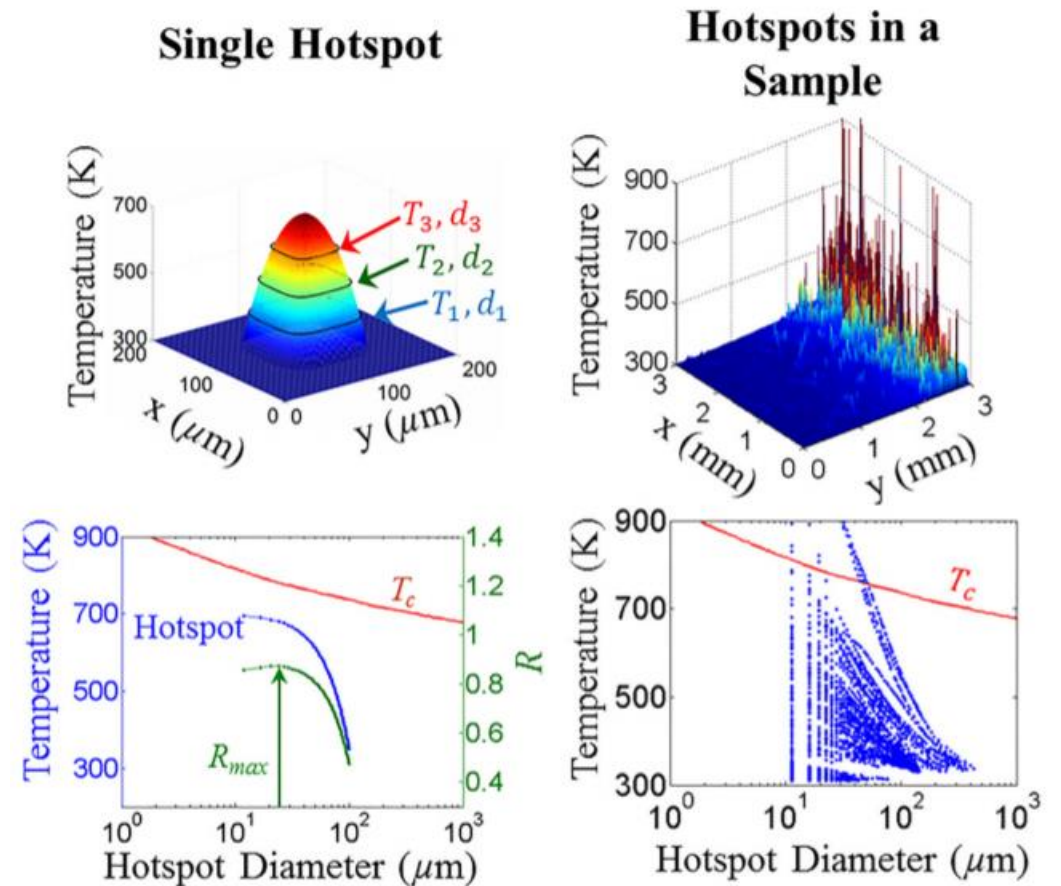


Temp (K)

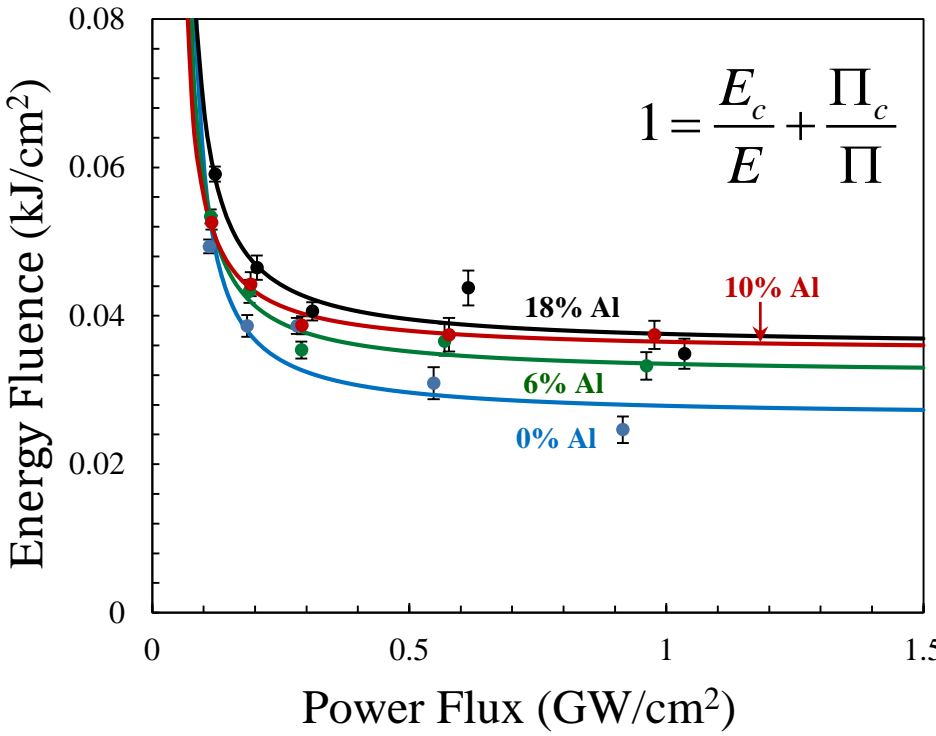


Determination of Ignition Likelihood via Hotspot Risk Analysis

- **Hotspot Ignition Risk Determinant (HIRD)**
 - Allows determination of criticality states of hotspots using a hotspot size-temperature ignition threshold
- **Ignition criterion for individual hotspots** (Barua *et al.* 2013)
 - $d(T) \geq d_c(T)$
- **Ignition criterion for microstructure**
 - If the density of hotspots exceeds 0.22 mm^{-2} at any point during the simulation. The sample is assumed to reach criticality.



Aluminized PBX Sensitivity Map

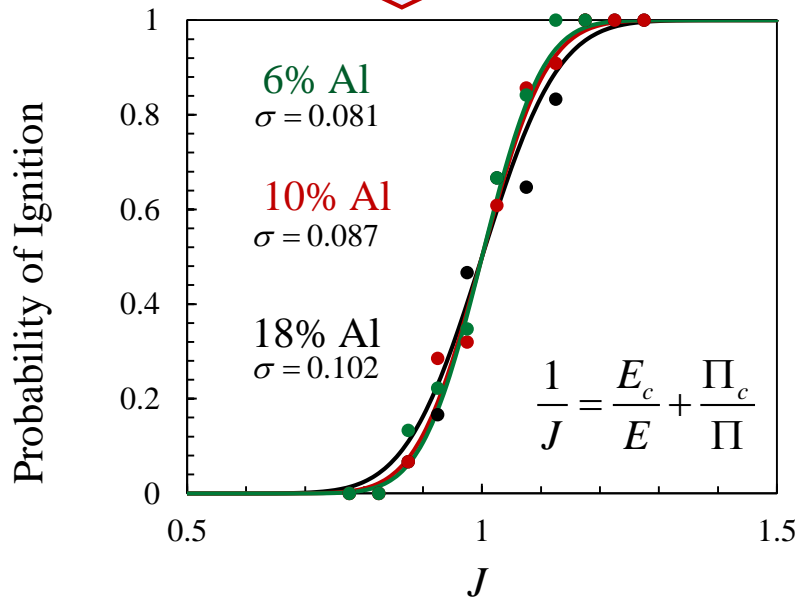


➤ Higher volume fractions of aluminum are less sensitive.

James Parameters are fit to 50% ignition threshold.

Entire probability distribution can be obtained via James parameters

Aluminum Volume Fraction	E_c (kJ/cm ²)	Π_c (GW/cm ²)
0% Al	0.0263	0.0570
6% Al	0.0320	0.0452
10% Al	0.0351	0.0376
18% Al	0.0357	0.0479

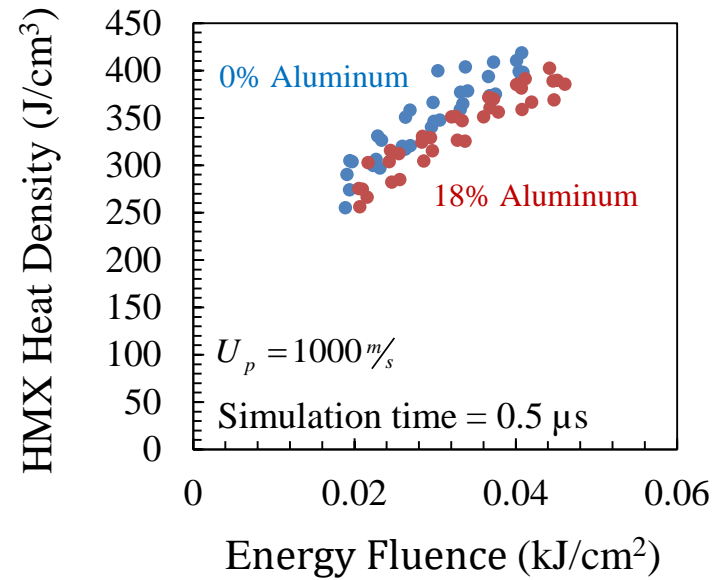


$$1 = \frac{E_c}{E} + \frac{\Pi_c}{\Pi}$$

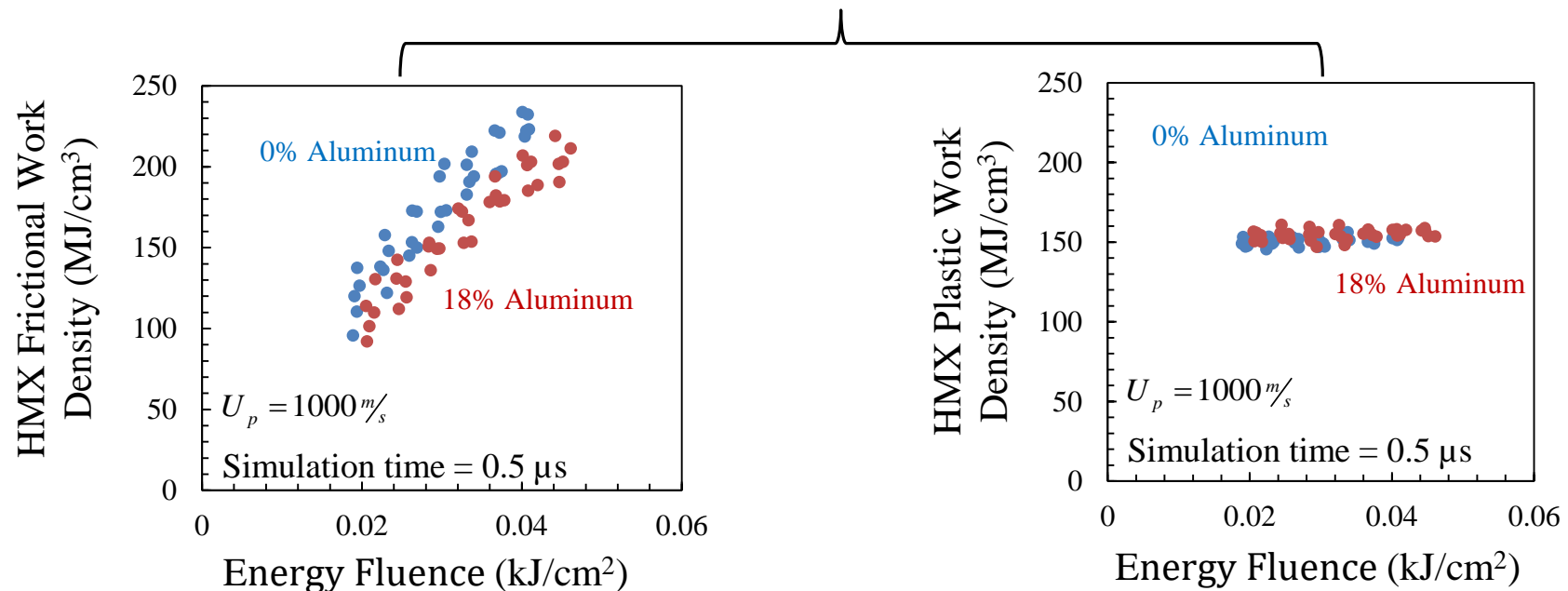
$$\frac{1}{J} = \frac{E_c}{E} + \frac{\Pi_c}{\Pi}$$

Heat Generation in HMX

- Friction generates more localized heat than plastic work
- Plastic work is responsible for the entire sample heating up, but not individual hotspots.

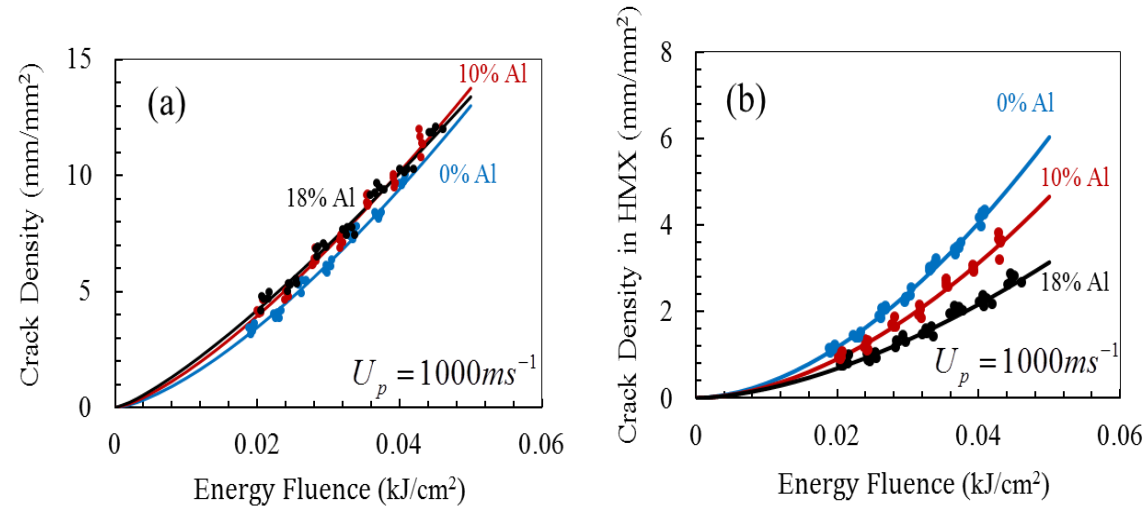


*Only areas above $T = 350\text{K}$ were analyzed

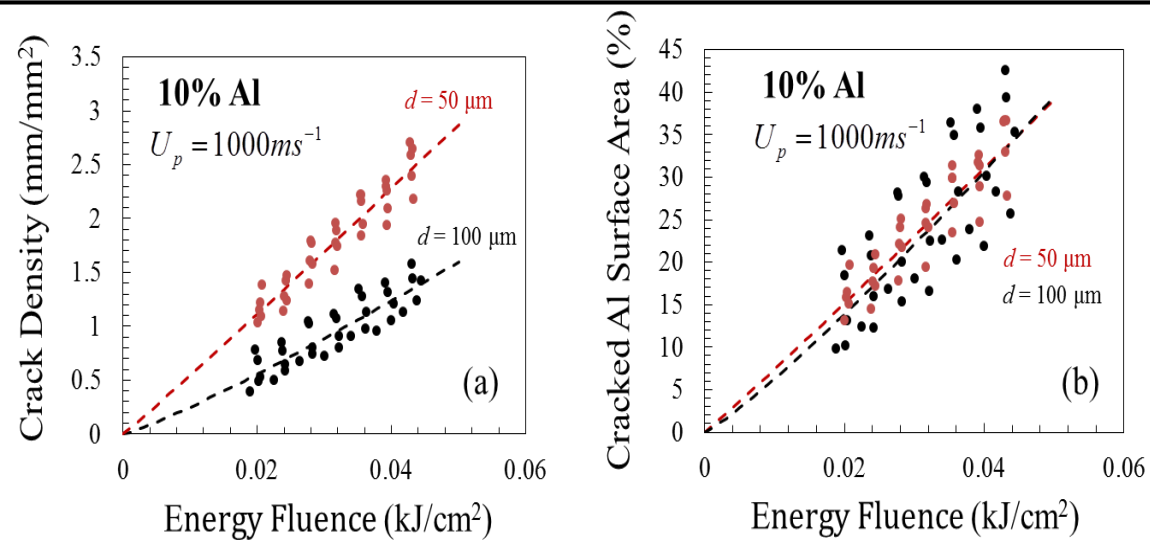


Effect of Aluminum on Fracture

- Total amount of cracks are similar between samples of varying Al concentration.
- When normalized to the relative amount of HMX, less HMX-associated cracks occur.



- Samples with smaller Al particles generate more cracks.
- When normalized to the relative surface area of aluminum, the proliferation of cracking is the same.

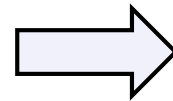


**How do we consider detonation and
void collapse?**

How do we consider detonation and void collapse?



**Sandia
National
Laboratories**



CTH – An Eulerian Hydrocode

➤ **Statistically equivalent microstructure sample sets (SEMSS)**

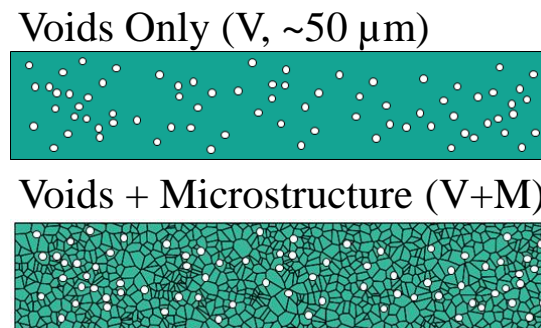
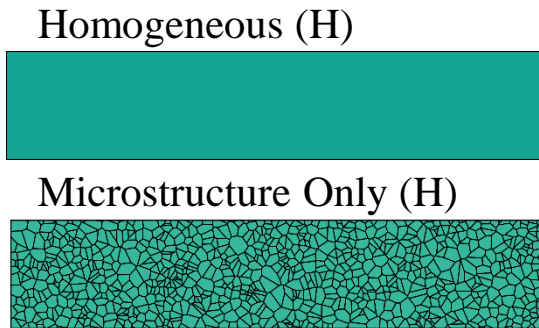
- Grains have monomodal size distribution with average size of 220 μm .
- SEMSS emulate experiments and allow evaluation of probabilistic/statistical nature of behavior.

➤ **Microstructure effects**

- Grains have random variations density ρ *
 - Hardin, Rimoli, and Zhou, *Thermochim Acta* **2014**, AIP Advances; 4, 097136 (2014)

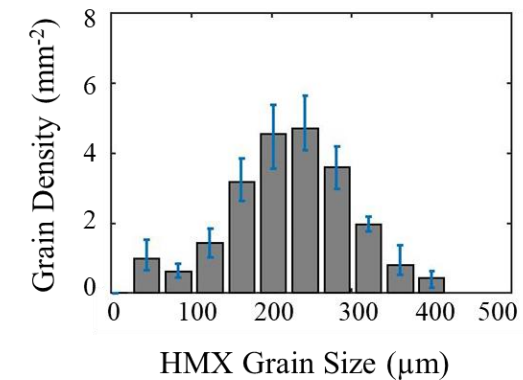
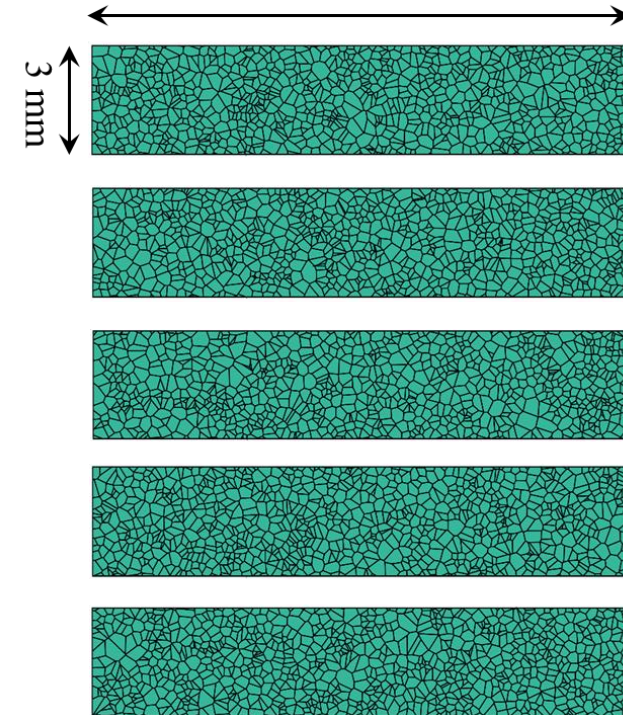
$$\left\{ \begin{array}{l} \rho_1 = 2.473 \text{ g/cm}^3 \\ \rho_2 = 1.902 \text{ g/cm}^3 \\ \rho_3 = 1.331 \text{ g/cm}^3 \end{array} \right.$$

➤ **ME-VE models (cases studied)**



SEMSS

15 mm



Simplified Steinberg–Guinan–Lund (SGL) flow stress model

$$\text{SGL: } Y = Y_A + Y_T(\dot{\epsilon}, T), \quad \dot{\epsilon}_p = \left[\frac{1}{C_1} \exp \left[\frac{2U_k}{T} \left(1 - \frac{Y_T}{Y_p} \right)^2 \right] + \frac{C_2}{Y_T} \right]^{-1}$$

Mie-Grüneisen equation of state (MG-EOS)

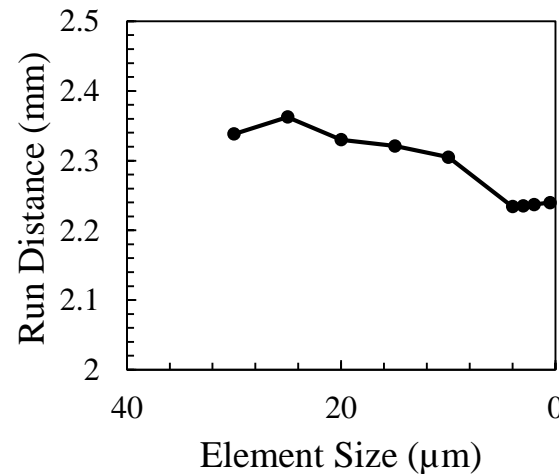
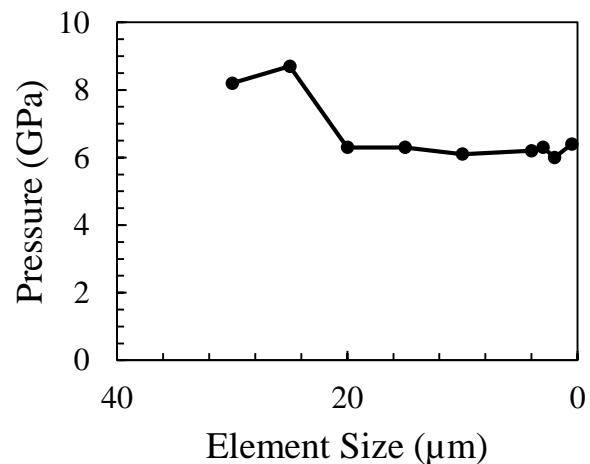
$$\text{MG-EOS: } P = \frac{\rho_0 C_0^2 (\eta - 1) \left[\eta - \frac{\Gamma_0}{2} (\eta - 1) \right]}{[\eta - s(\eta - 1)]^2} + \Gamma_0 E, \quad \eta = \frac{\rho}{\rho_0}, \quad E = \frac{1}{V_0} \int C_v dT$$

History Variable Reactive Burn (HVRB) chemistry model

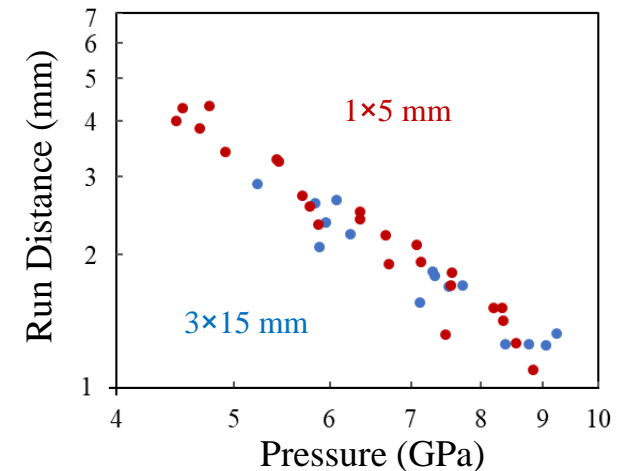
$$\text{HVRB: } \lambda = 1 - (1 - \phi^M / X)^X, \quad \phi = \tau_0^{-1} \int_0^t \left[(P - P_i) / P_R \right]^Z dt$$

- Simulations performed using CTH – an Eulerian-based hydrocode from SNL.
- Mesh convergence study performed.
 - Samples have both microstructure and 50 μm voids.
 - Pressure converges more quickly than run distance (20 μm element vs. 5 μm element).
 - Final mesh resolution of 5 μm chosen.
- A size comparison is needed to determine whether the samples are representative of a real size microstructure.
 - There is no significant discrepancy between 1 \times 5 mm microstructures and 3 \times 15 mm microstructures

Mesh resolution

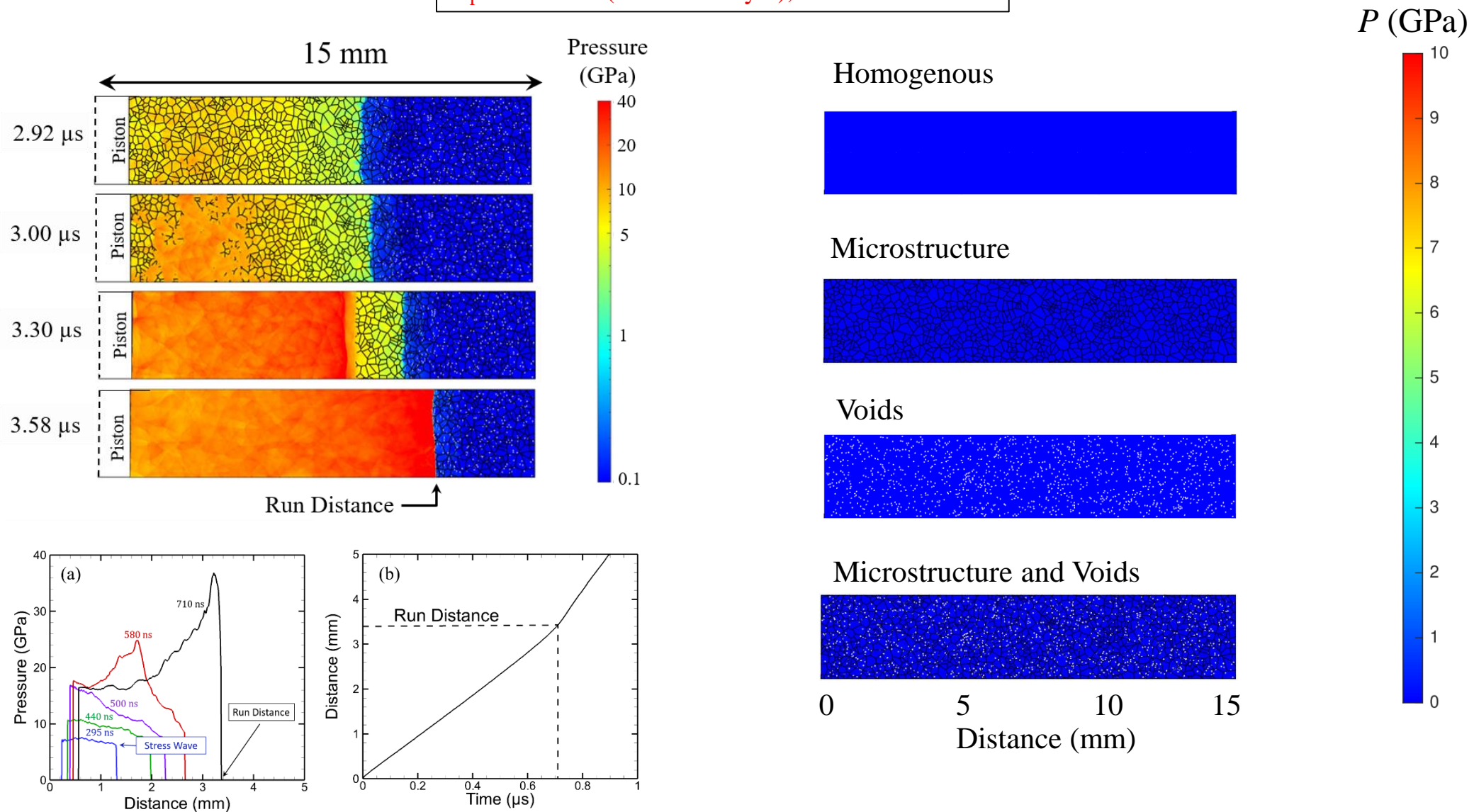


Sample size



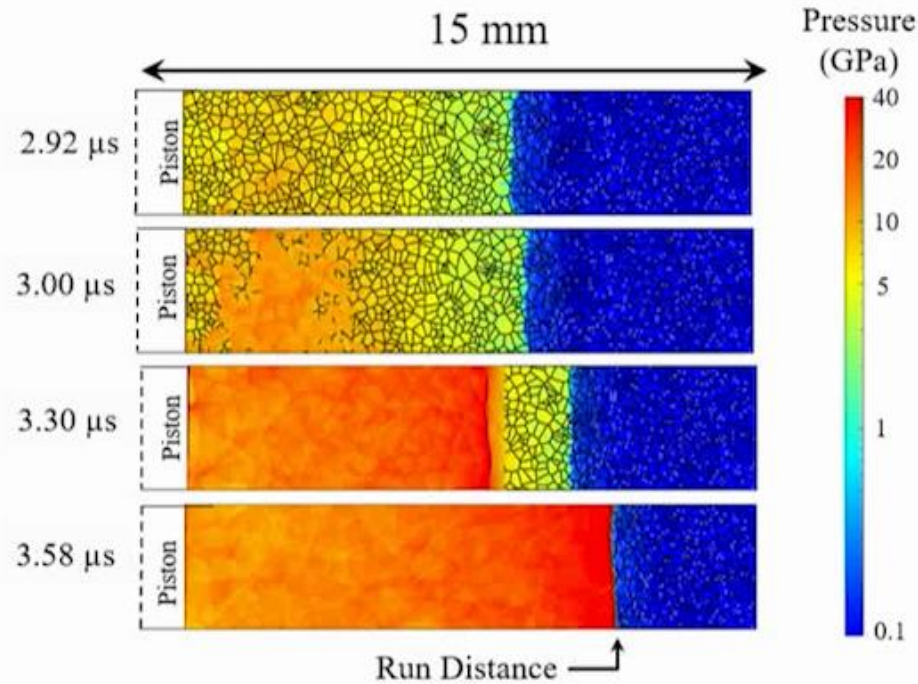
Shock to Detonation Transition (SDT)

$U_p = 600 \text{ ms}^{-1}$ (aluminum flyer), 30% MS variation

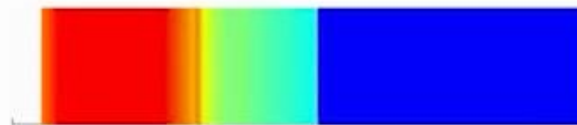


Shock to Detonation Transition (SDT)

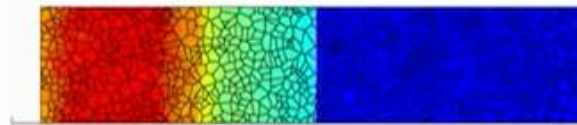
$U_p = 600 \text{ ms}^{-1}$ (aluminum flyer), 30% MS variation



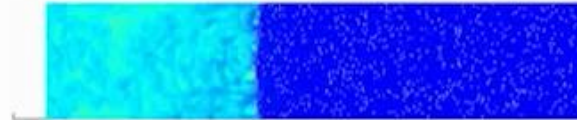
Homogenous



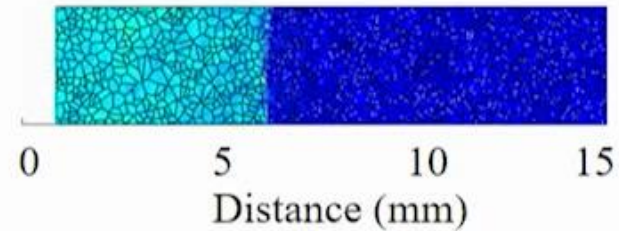
Microstructure



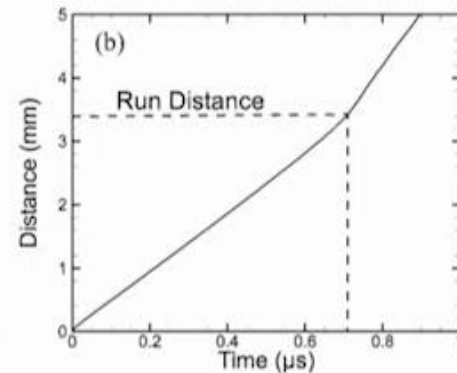
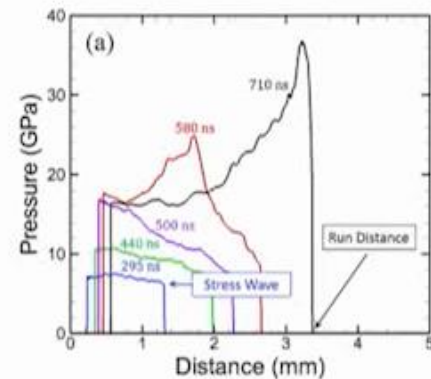
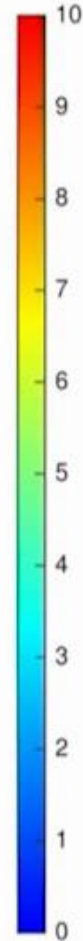
Voids



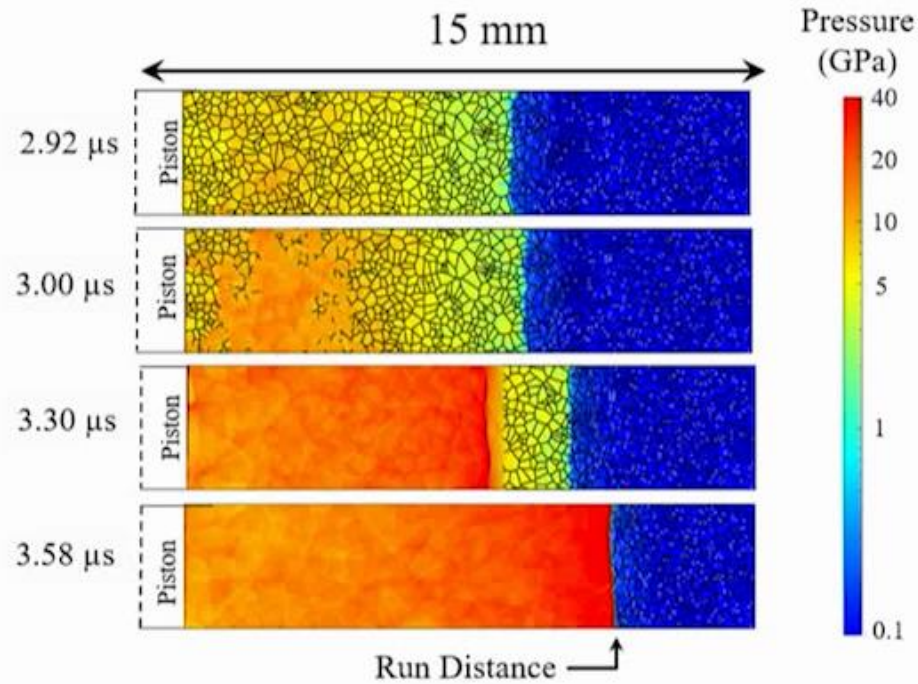
Microstructure and Voids



P (GPa)



$U_p = 600 \text{ ms}^{-1}$ (aluminum flyer), 30% MS variation



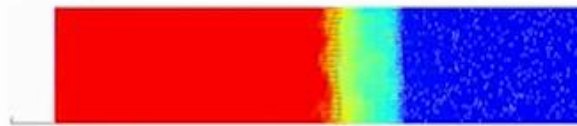
Homogenous



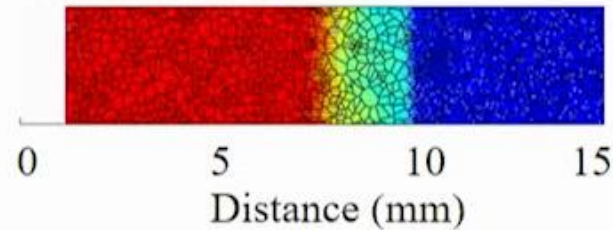
Microstructure



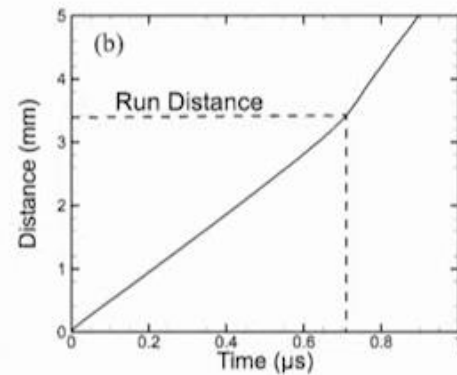
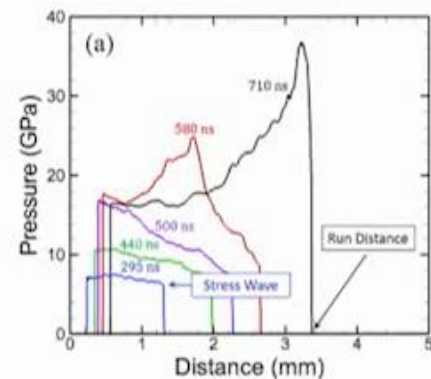
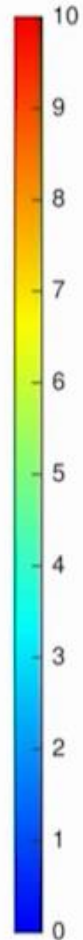
Voids

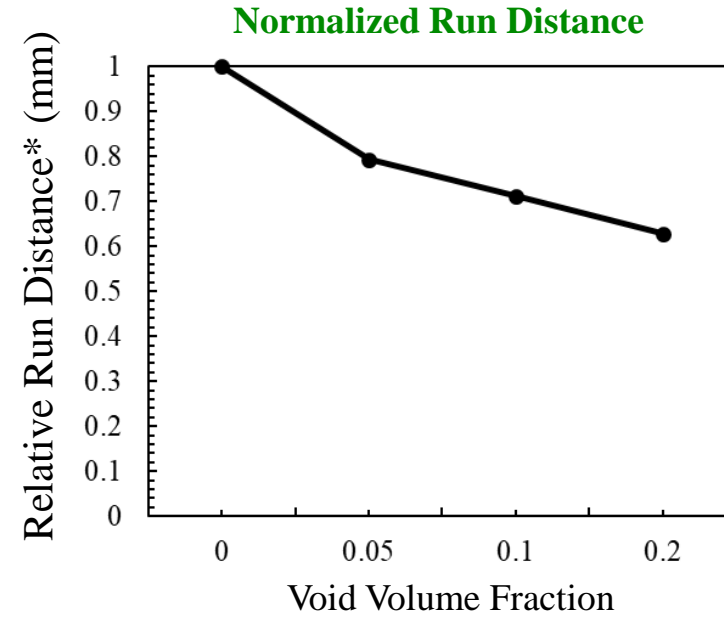
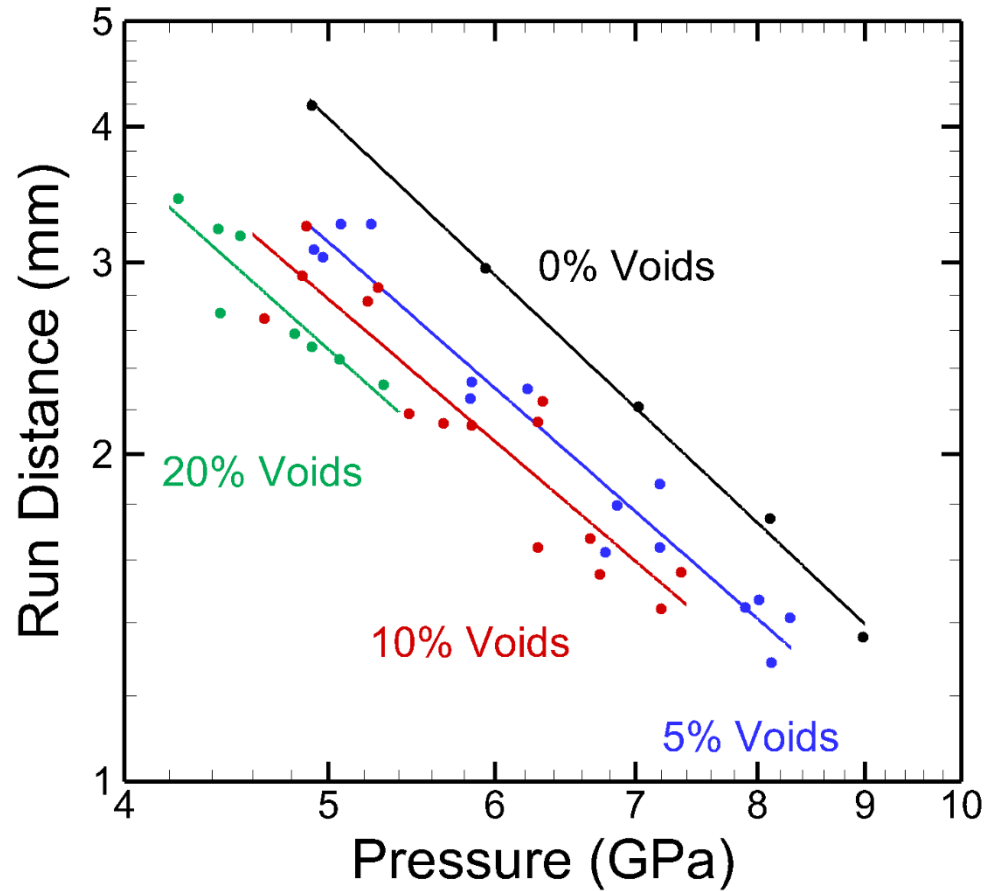


Microstructure and Voids



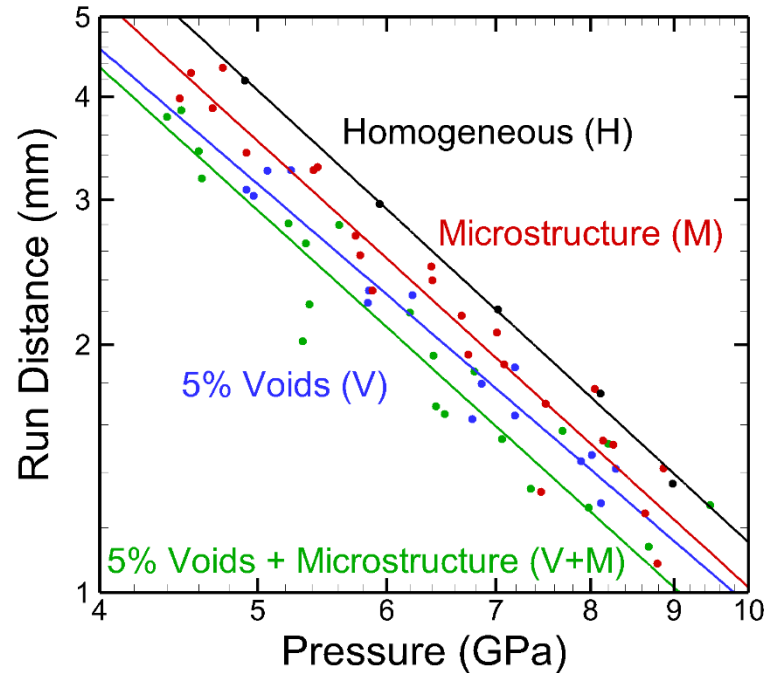
P (GPa)



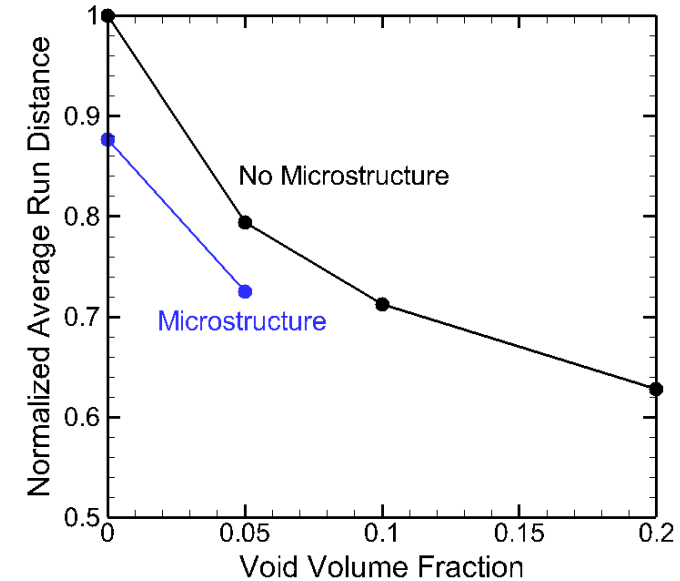


Void Volume Fraction	Average Decrease in Run Distance
5%	20.6%
10%	28.8%
20%	37.2%

Statistical Data Sets from SEMSS



- Heterogeneities (microstructure, voids) enhance SDT sensitivity (shortens run distance or lowers PP line)
- **Microstructure** = constituent and morphological heterogeneities
- **Voids** = Geometric heterogeneities



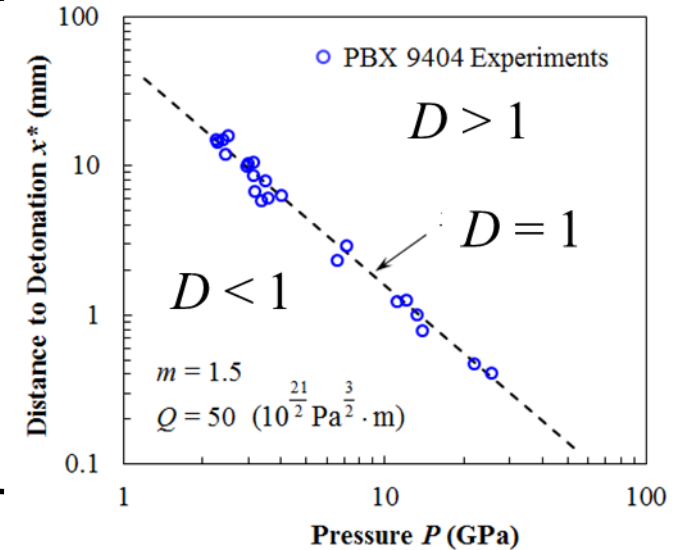
HMX Sample Set	Average Decrease in Run Distance (compared to uniform)
Microstructure	12.2%
5% Voids	20.1%
5% Voids + Microstructure	27.5%

- **Step 1:** Pop plot fits are generally based on a power law relationship

$$x^* = SP_s^{-m},$$

- **Step 2:** Introduce a Non-dimensional Pop plot number (PPN) to gauge distance from PP

$$D = \frac{(P_s - P_0)^m (x^* - x_0^*)}{S}.$$

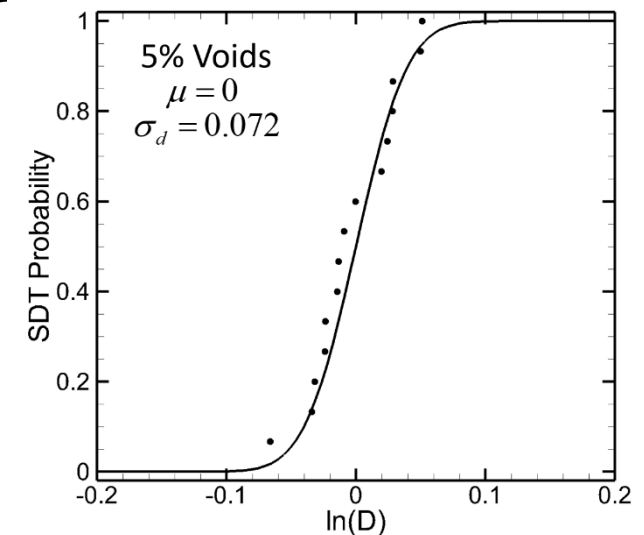


- **Step 3:** Create a probability formulation using a log-normal CDF

$$\mathcal{P}(D) = \frac{1}{\sigma\sqrt{2\pi}} \int_0^D \frac{1}{x} \exp\left[-\frac{(\ln x - \mu)^2}{2\sigma_d^2}\right] dx,$$

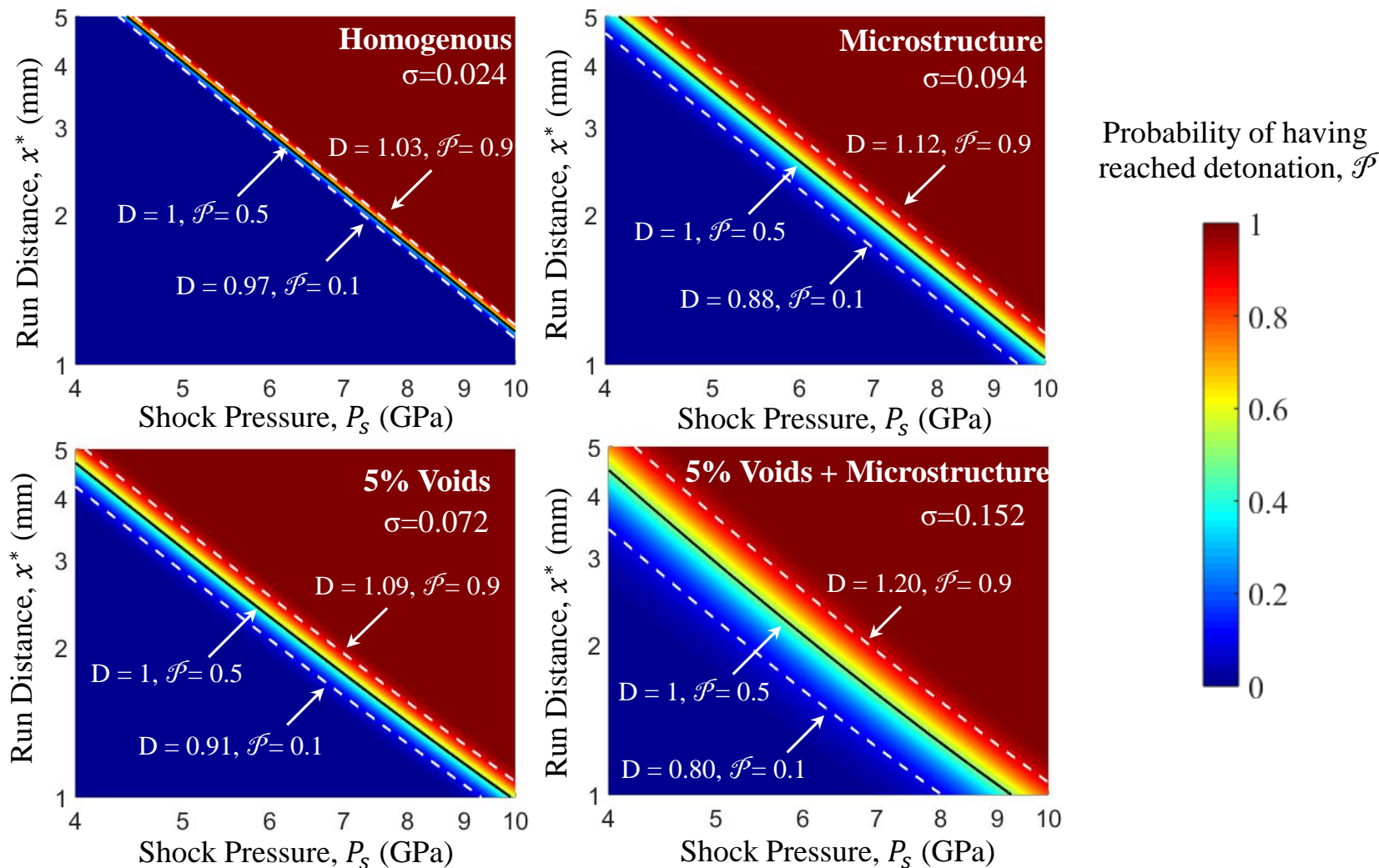
- **Step 4:** Write in terms of physical parameters (shock pressure and run distance)

$$\mathcal{P}(P_s, x^*) = \frac{1}{2} + \frac{1}{2} \operatorname{erf} \left[\frac{1}{\sqrt{2}\sigma_d} \left(\ln \left((P_s - P_0)^m \right) + \ln \left(x^* - x_0^* \right) - \ln S \right) \right].$$

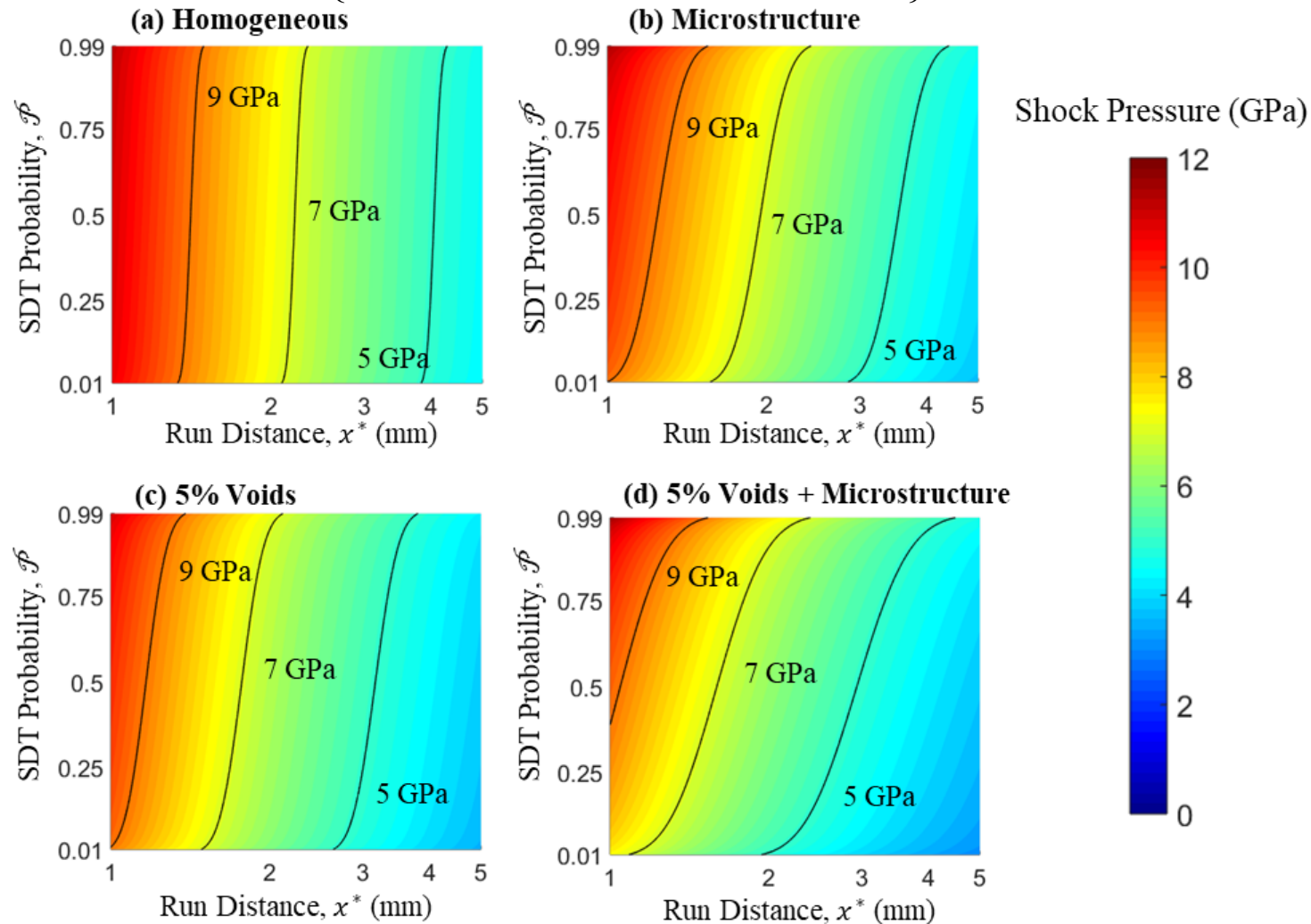


2D Probability Map

$$\mathcal{P}(P_s, x^*) = \frac{1}{2} + \frac{1}{2} \operatorname{erf} \left[\frac{1}{\sqrt{2}\sigma_d} \left(\ln \left((P_s - P_0)^m \right) + \ln(x^* - x_0^*) - \ln S \right) \right].$$

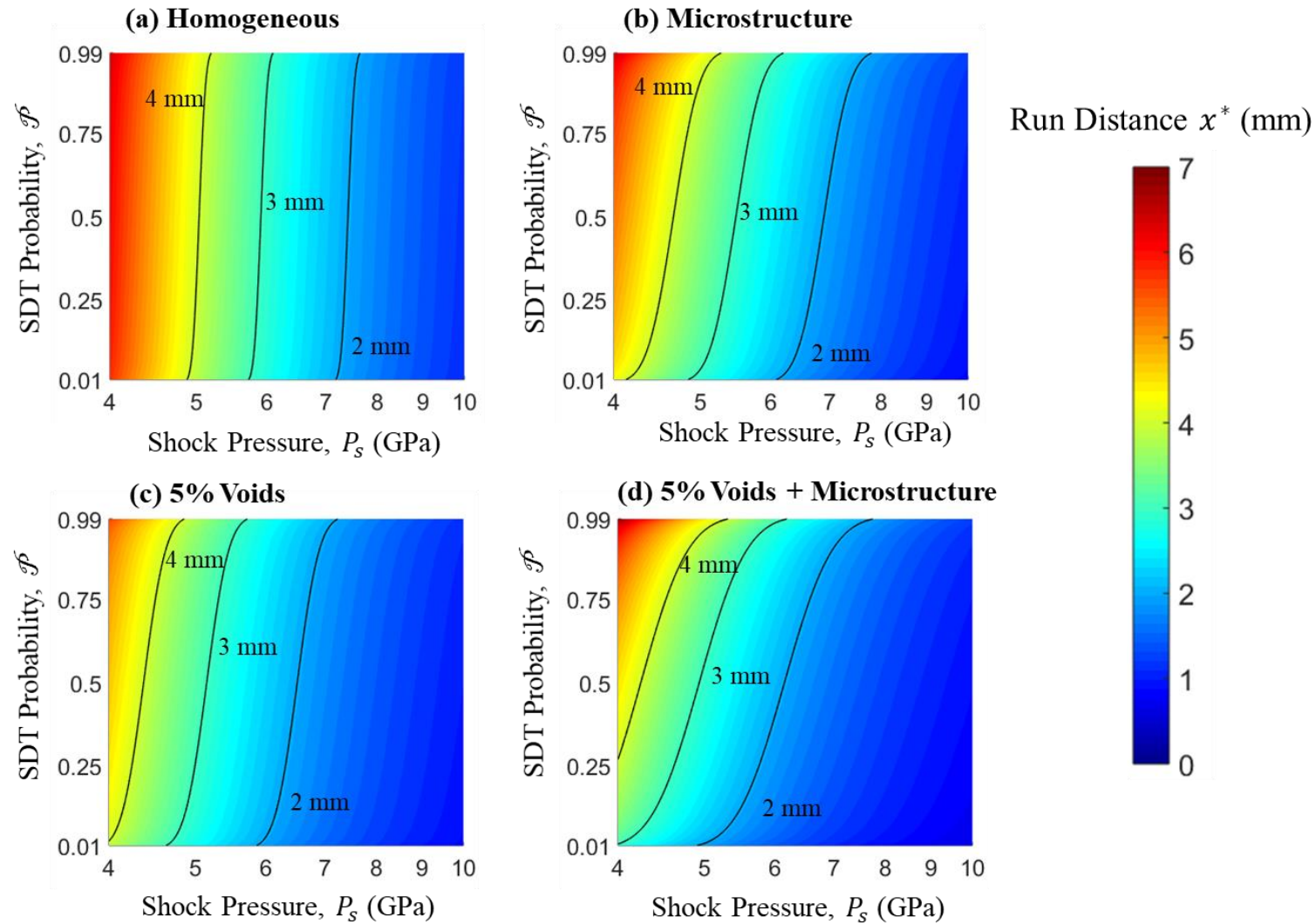


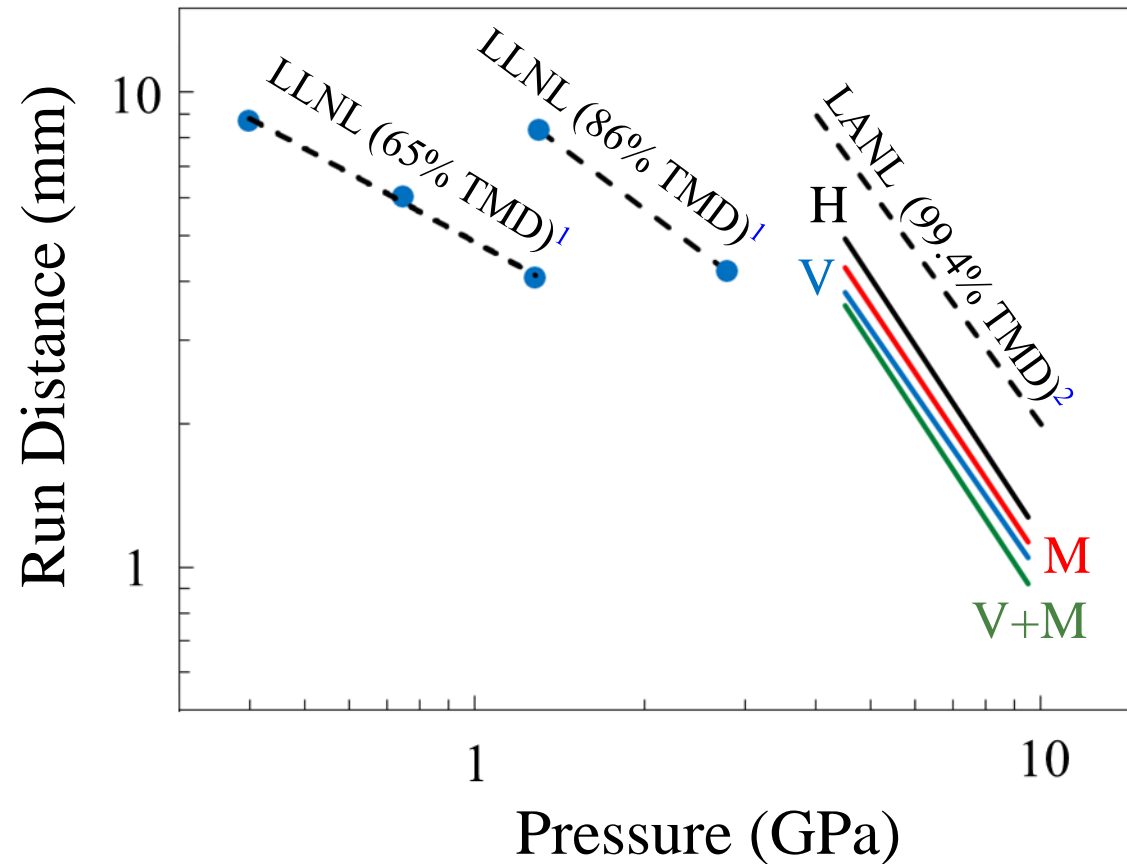
$$P_s(\mathcal{P}, x^*) = \left\{ \frac{S}{(x^* - x_0^*)} \exp\left[\sqrt{2}\sigma_d \left(\text{erf}^{-1}(2\mathcal{P} - 1)\right)\right] \right\}^{\frac{1}{m}} + P_0.$$



2D Run Distance Map

$$x^*(\mathcal{P}, P_s) = \frac{S}{(P_s - P_0)^m} \exp\left[\sqrt{2}\sigma_d \left(\text{erf}^{-1}(2\mathcal{P} - 1)\right)\right] + x_0^*$$

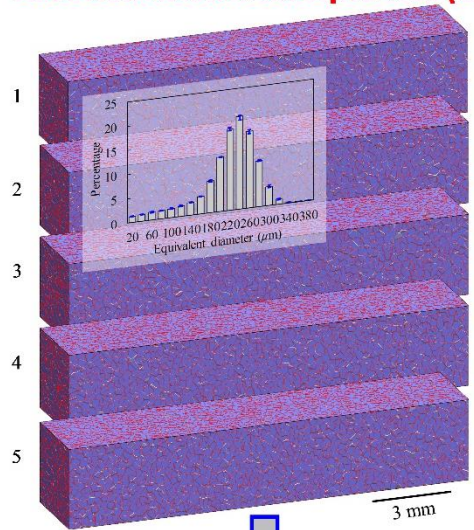




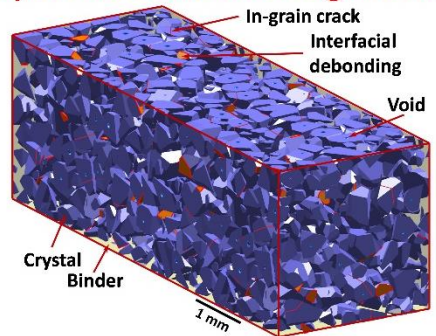
- Model trends match those seen in experiment.
- This model only represents a first approach at predicting SDT on a mm size scale.
- Further calibration of the HVRB or a transition to an Arrhenius-based chemical reaction rate model will be required.

1) Garcia, Frank, Kevin S. Vandersall, and Craig M. Tarver. "Shock initiation experiments with ignition and growth modeling on low density HMX." *Journal of Physics: Conference Series*. Vol. 500, No. 5. IOP Publishing, 2014.
2) Baytos, John F. *LASL explosive property data*. Vol. 4. Univ of California Press, 1980.

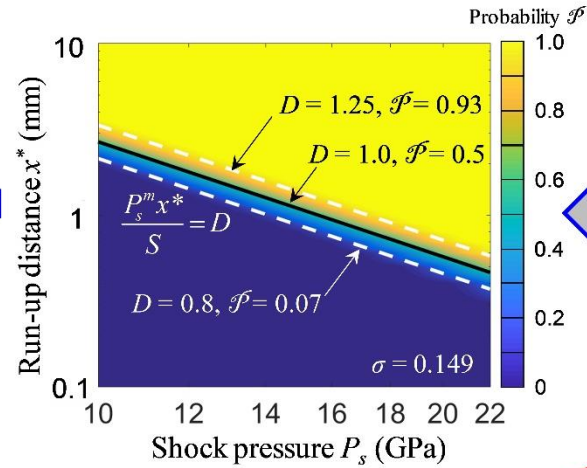
(1) Statistically equivalent microstructure sample set (SEMSS)



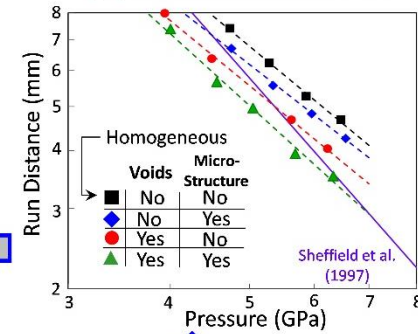
(2) Microscale heterogeneities



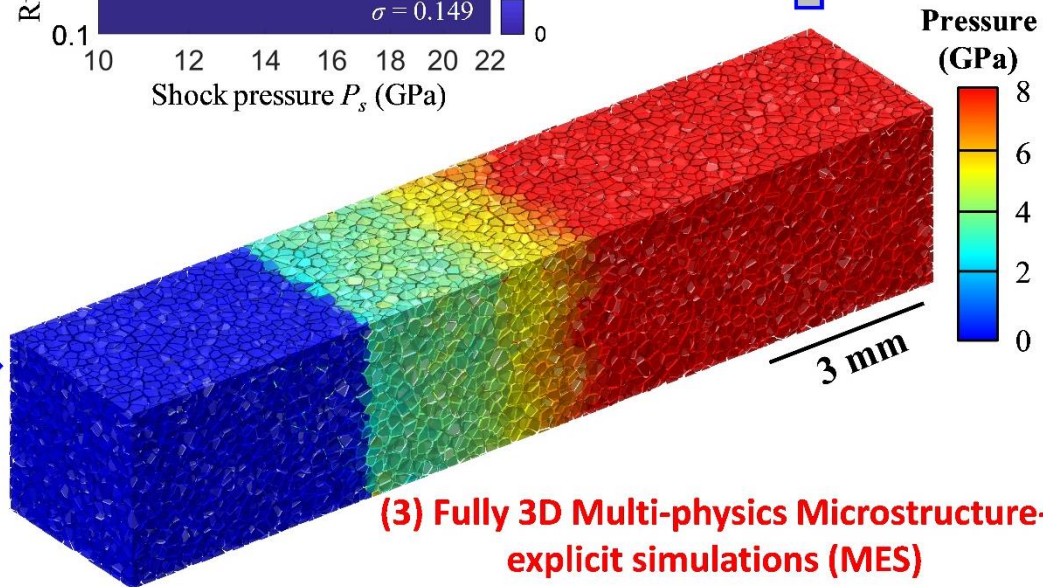
(5) SDT probability map

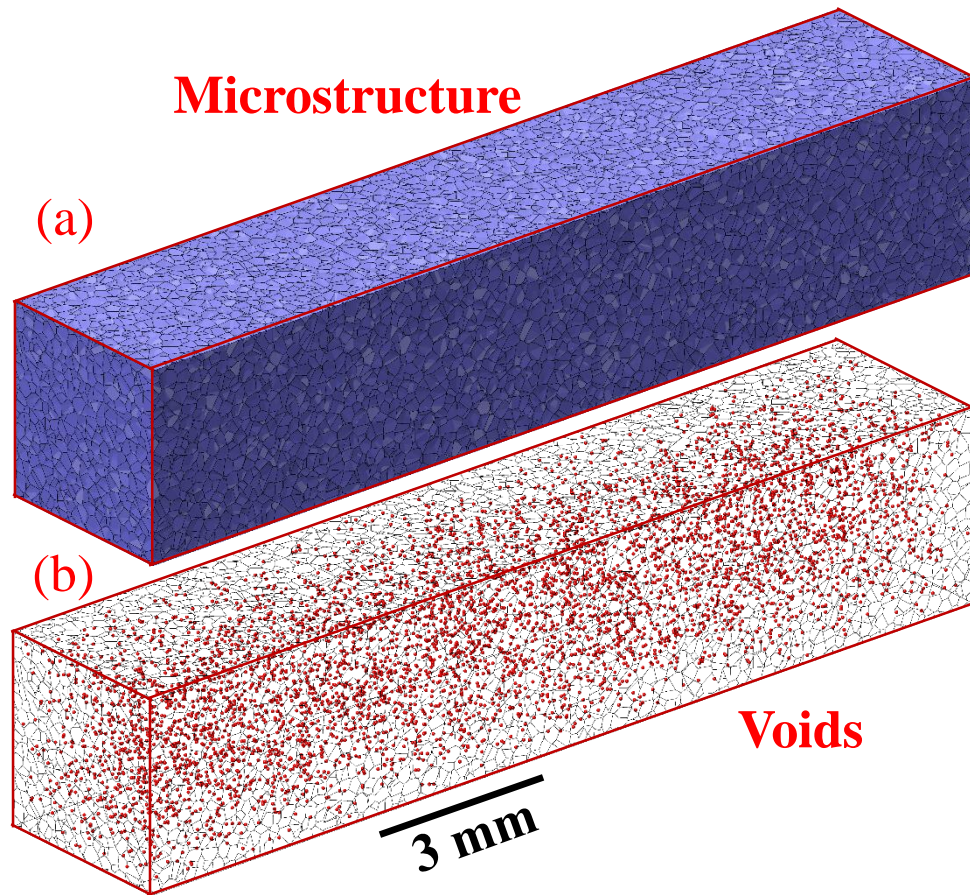


(4) SDT thresholds

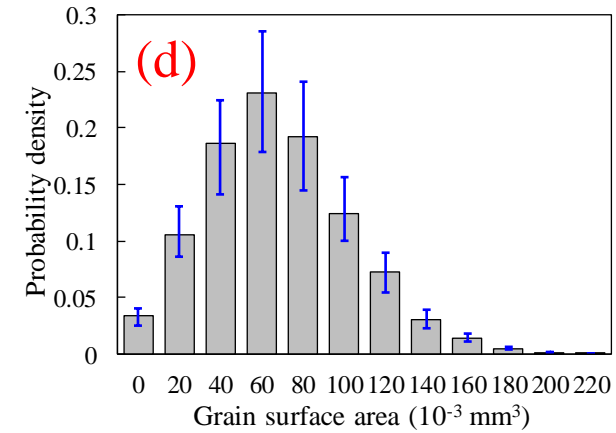
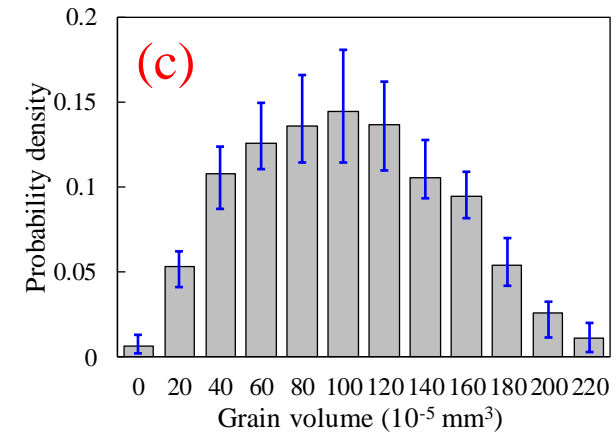


(3) Fully 3D Multi-physics Microstructure-explicit simulations (MES)



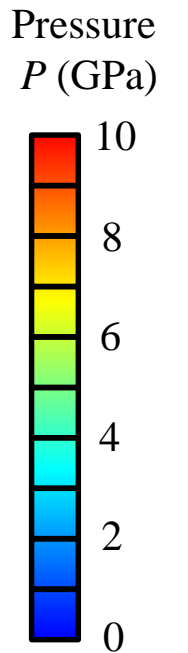
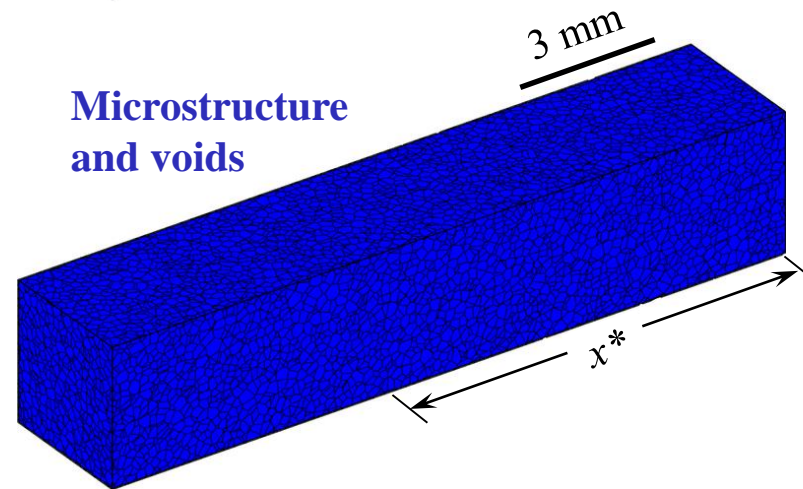
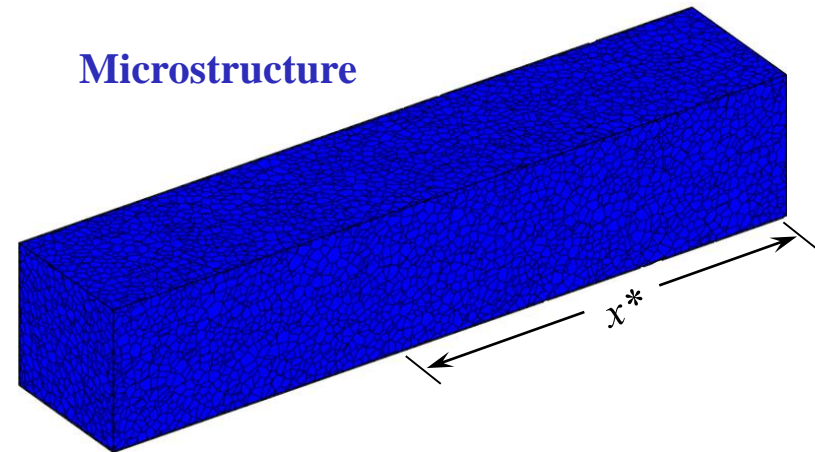
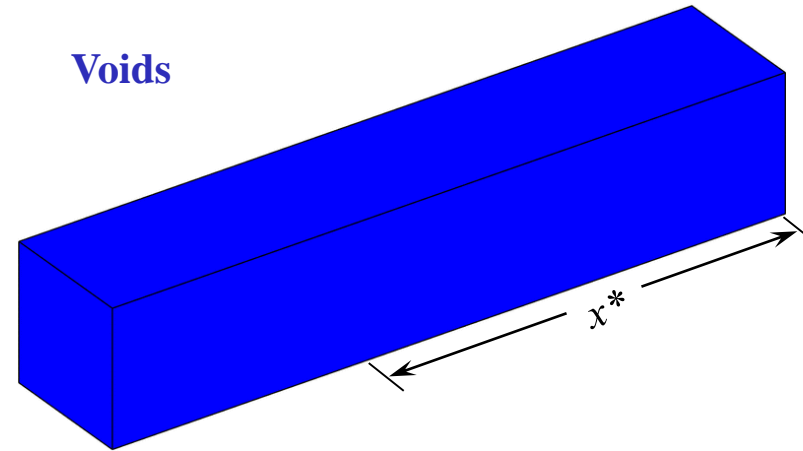
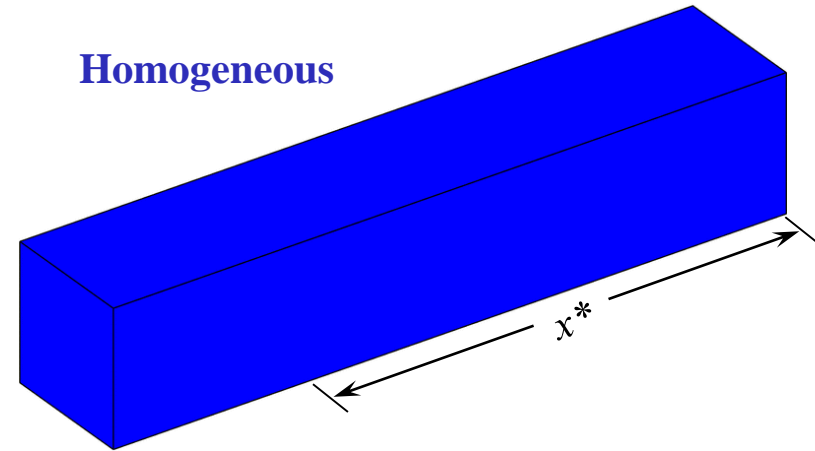


Grain size and surface area



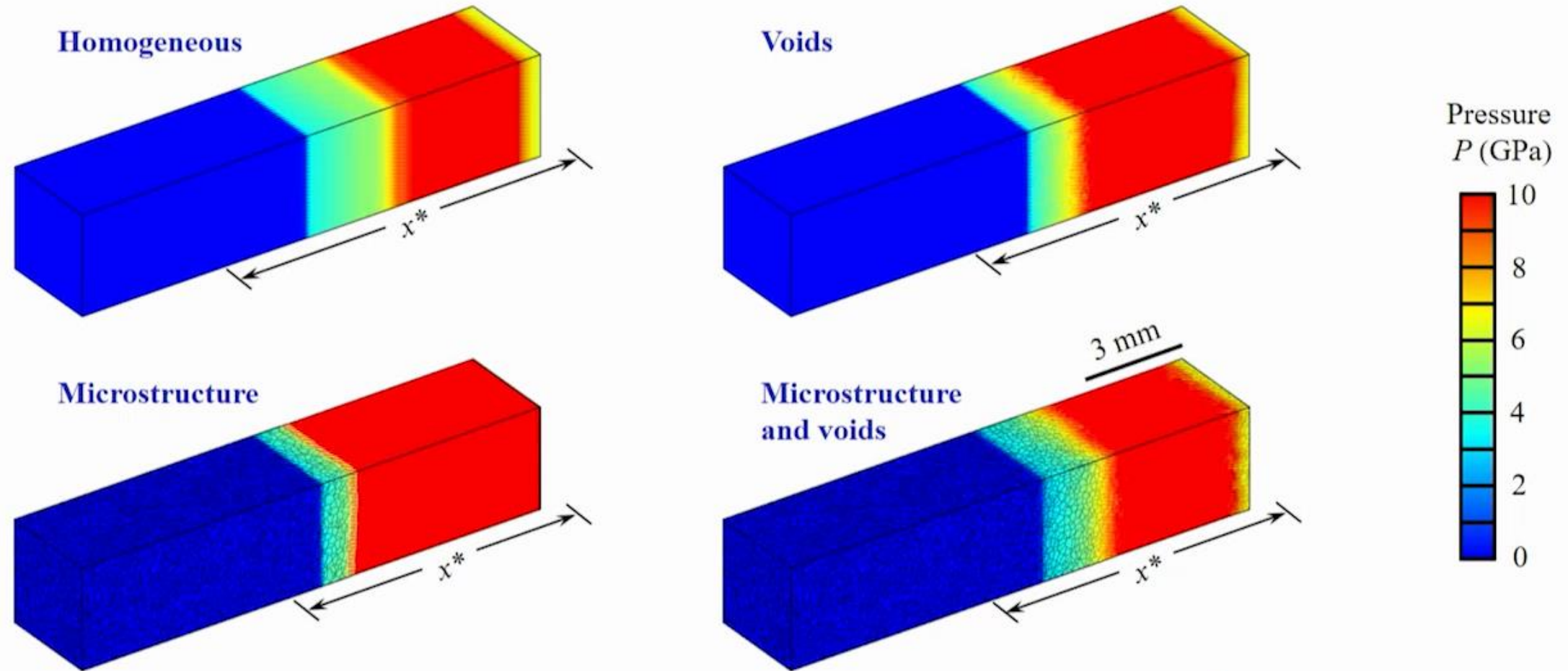
➤ Simulations performed using CTH – an Eulerian-based hydrocode from SNL.

$$U_p = 600 \text{ m/s} \quad t = 0.00 \text{ } \mu\text{s}$$



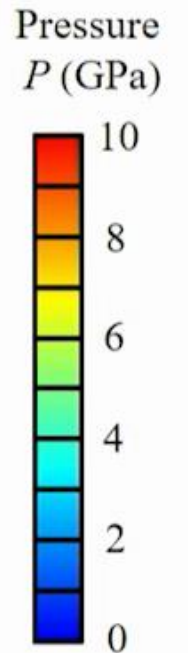
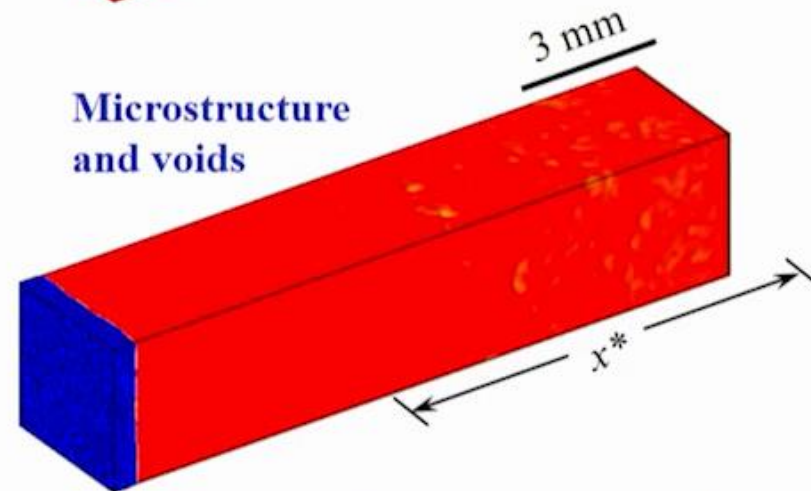
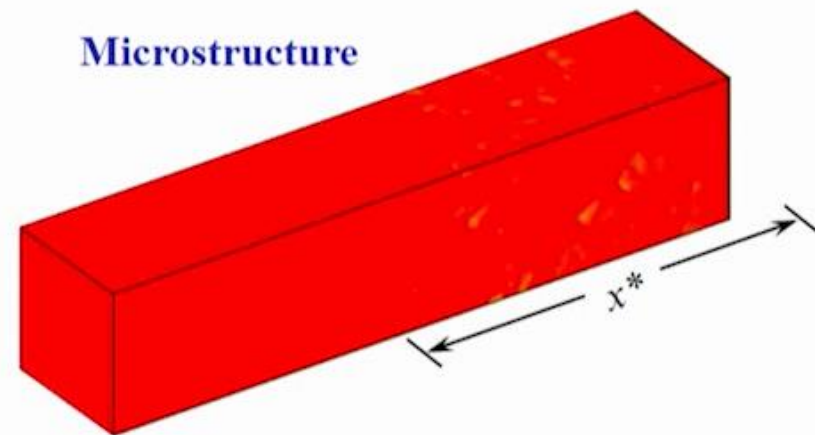
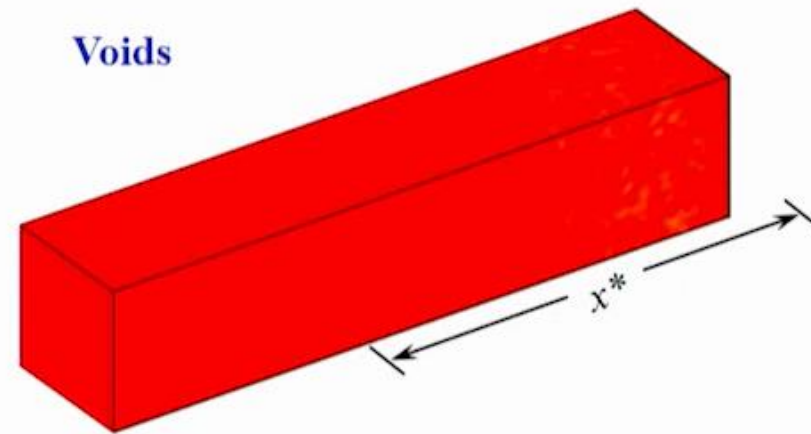
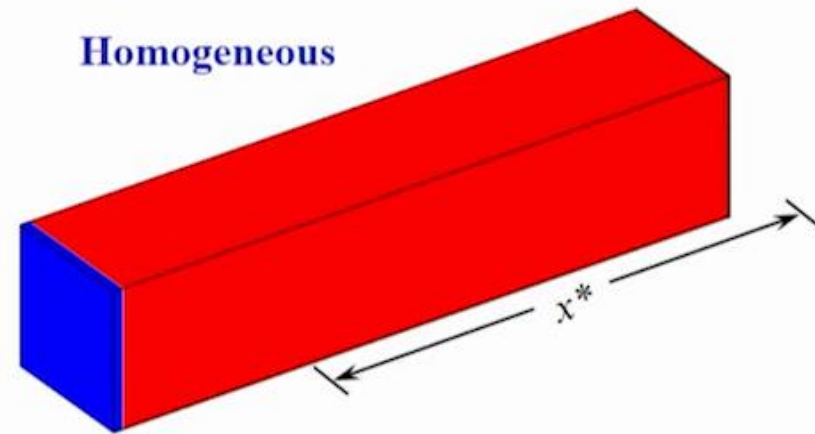
x^* : Run-to-detonation distance

$$U_p = 600 \text{ m/s} \quad t = 2.08 \mu\text{s}$$



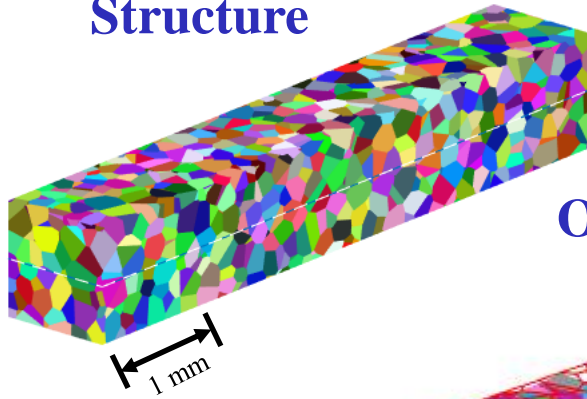
x^* : Run-to-detonation distance

$$U_p = 600 \text{ m/s} \quad t = 3.14 \mu\text{s}$$

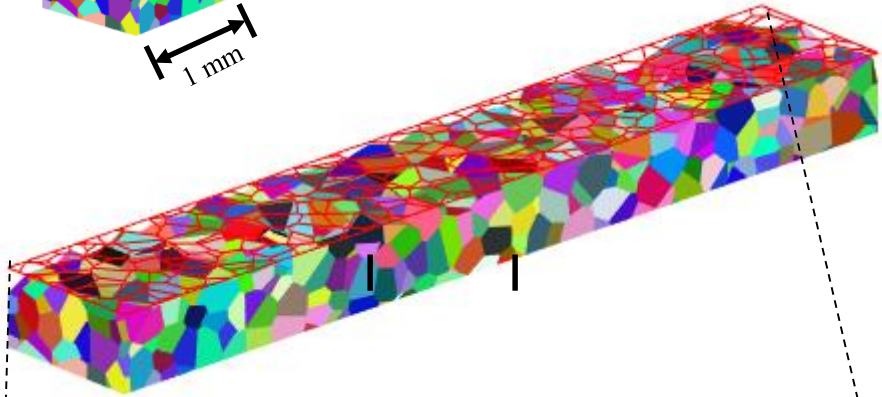


x^* : Run-to-detonation distance

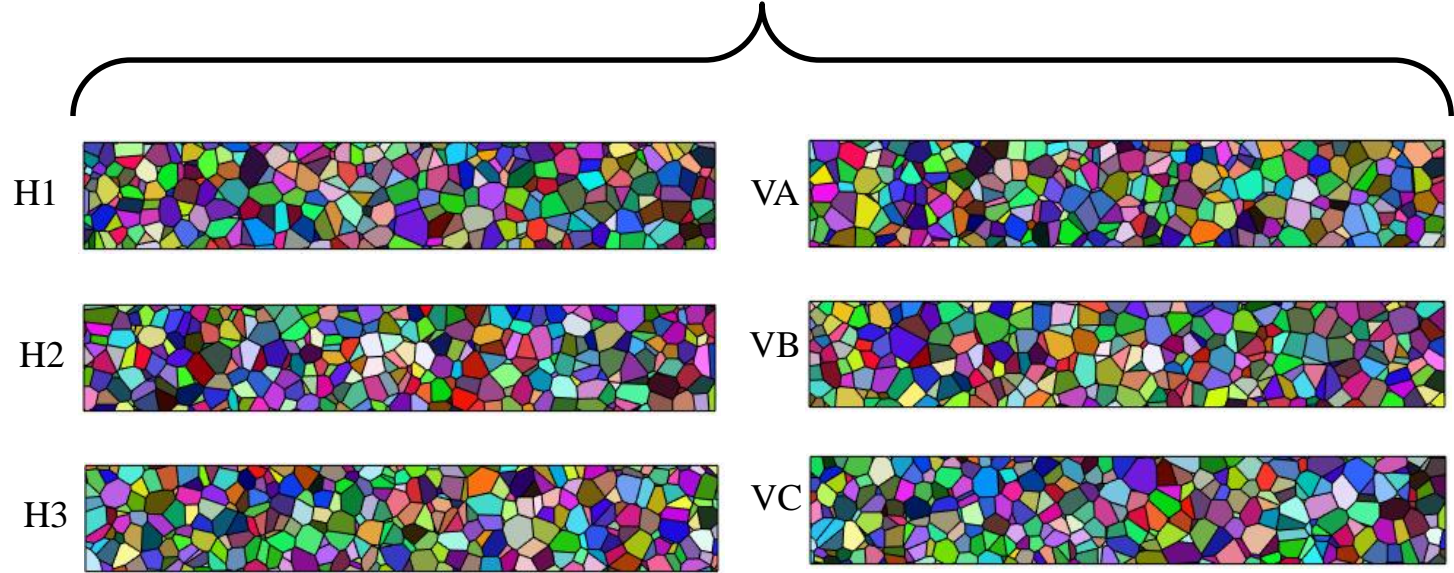
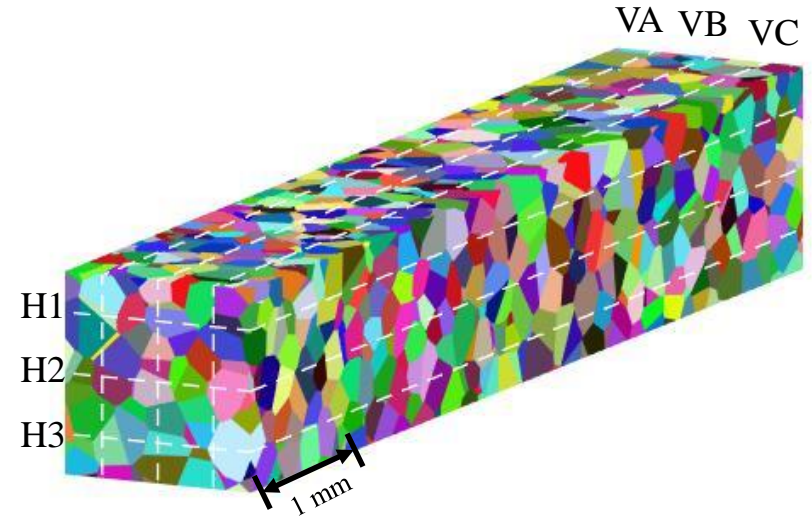
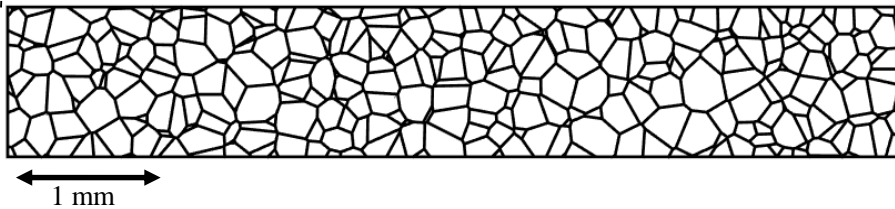
Original 3D Structure

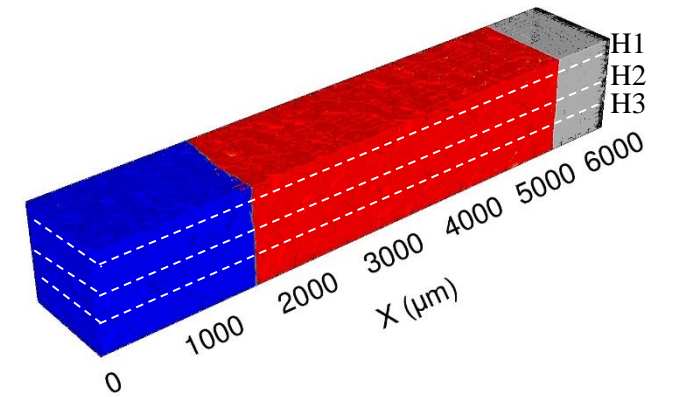
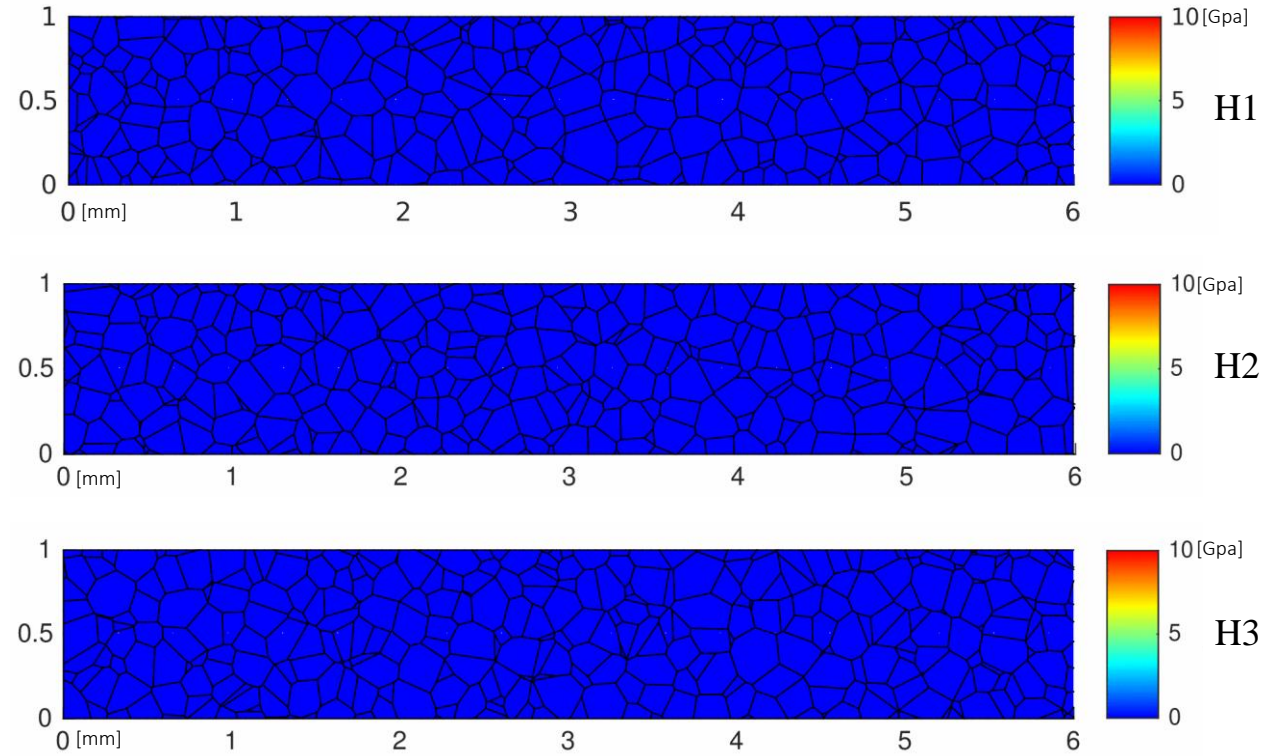


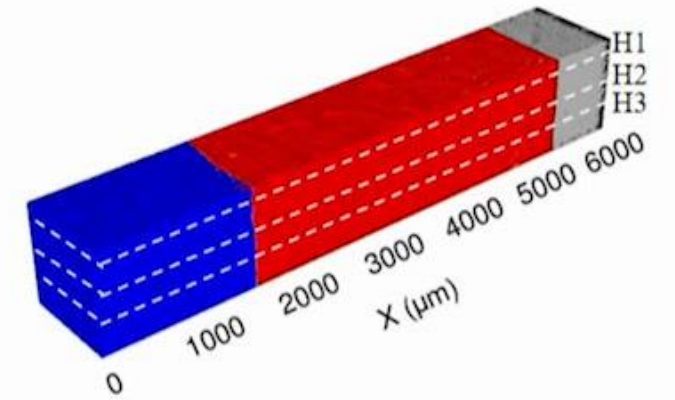
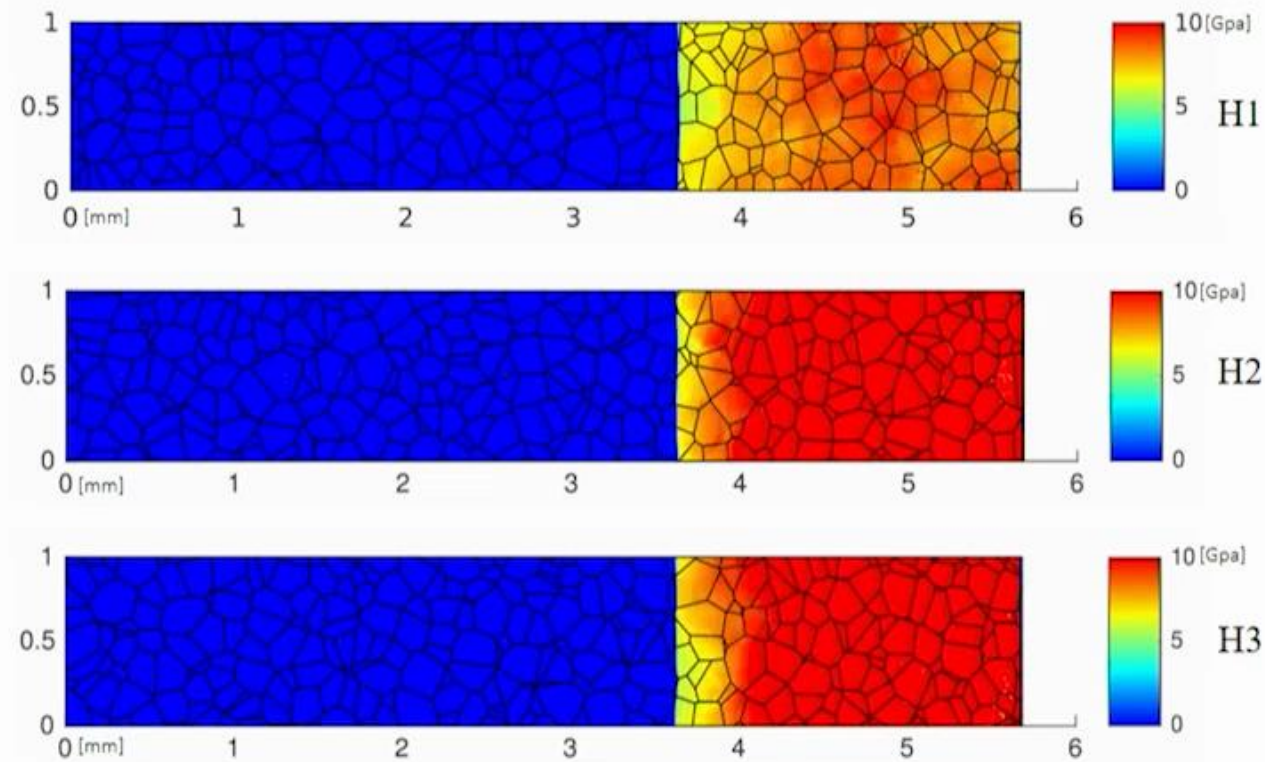
Outline of new grains on cross-section

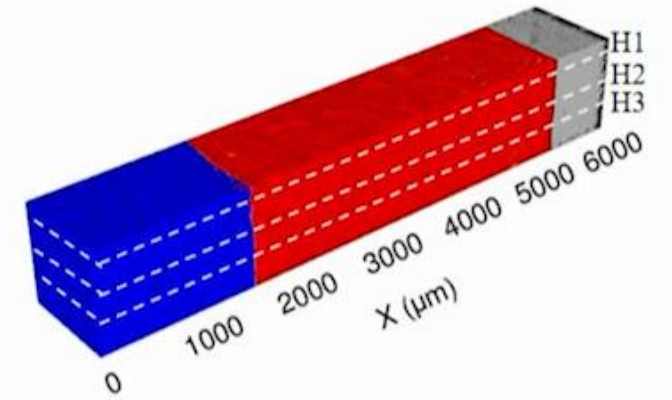
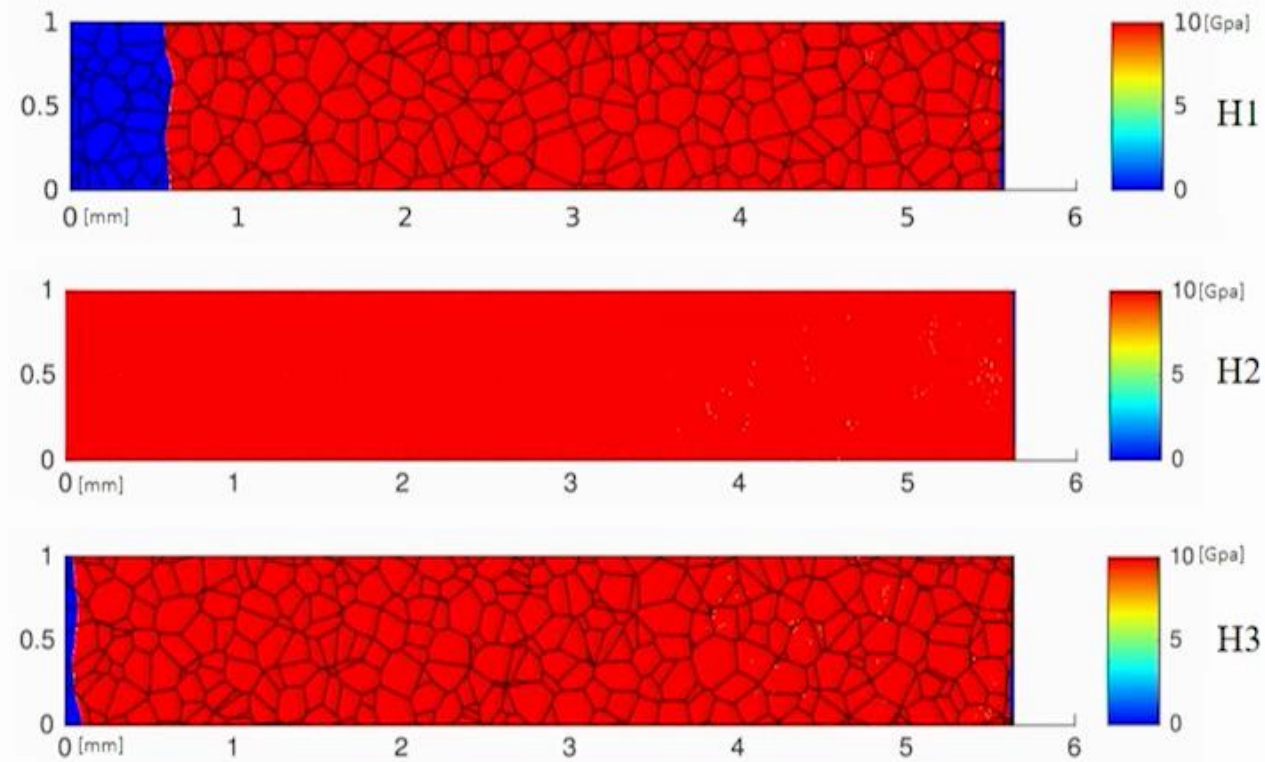


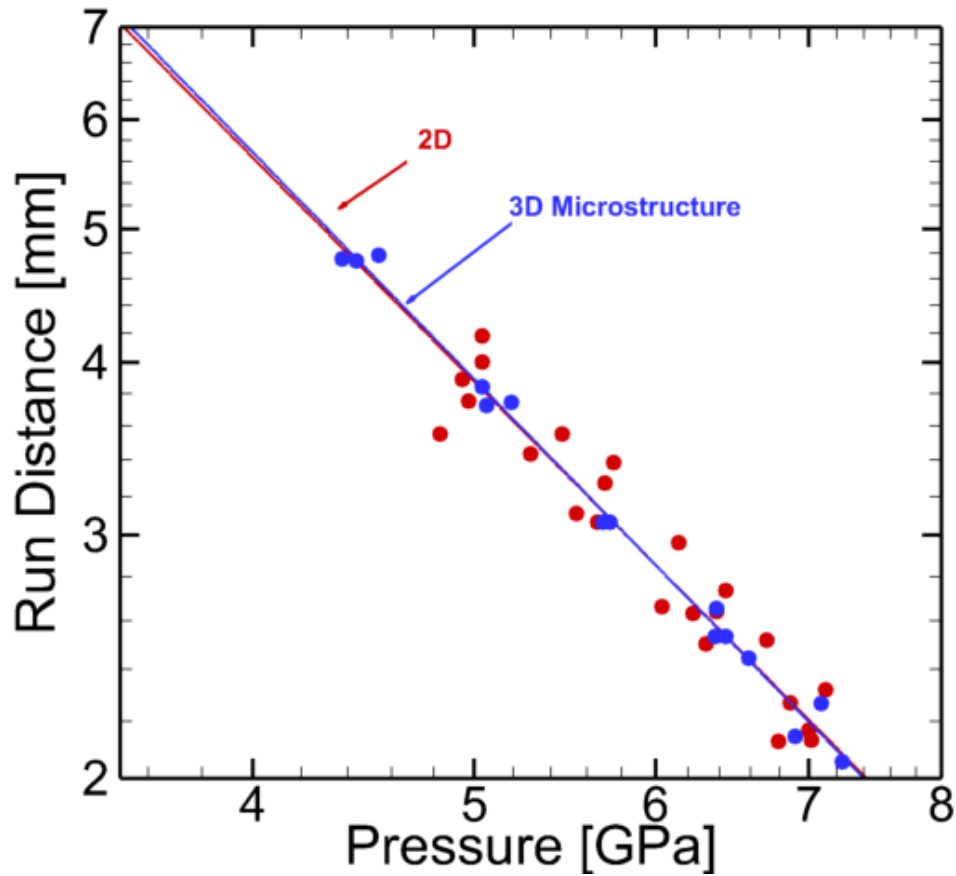
New 2D microstructure





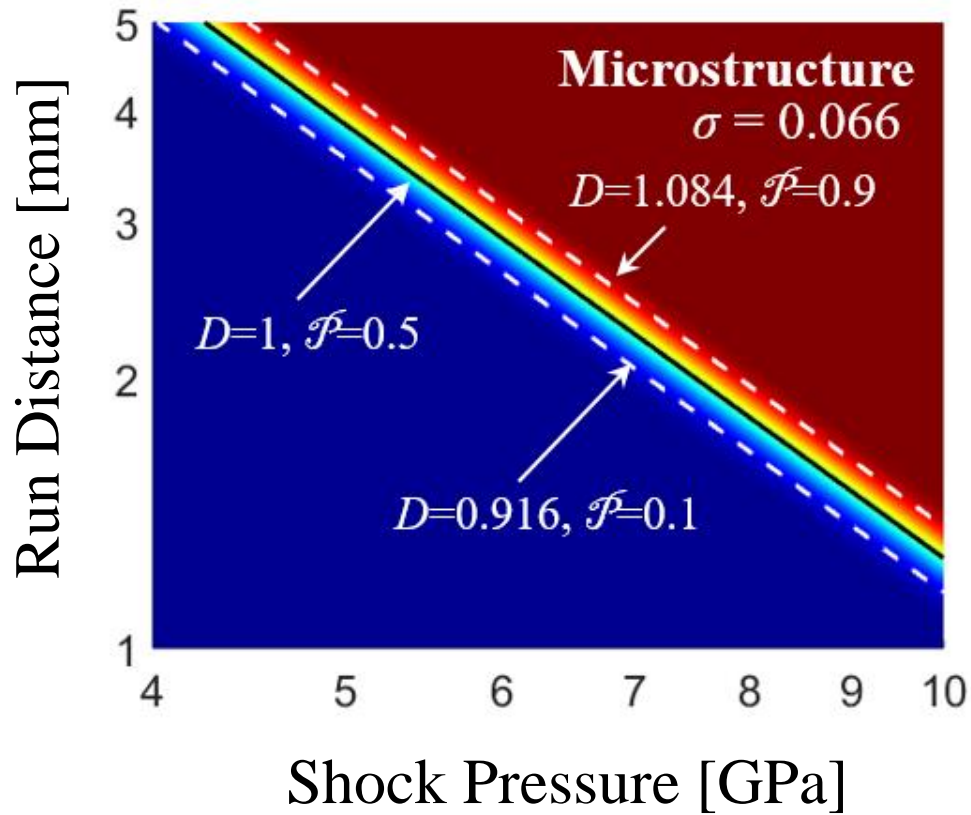




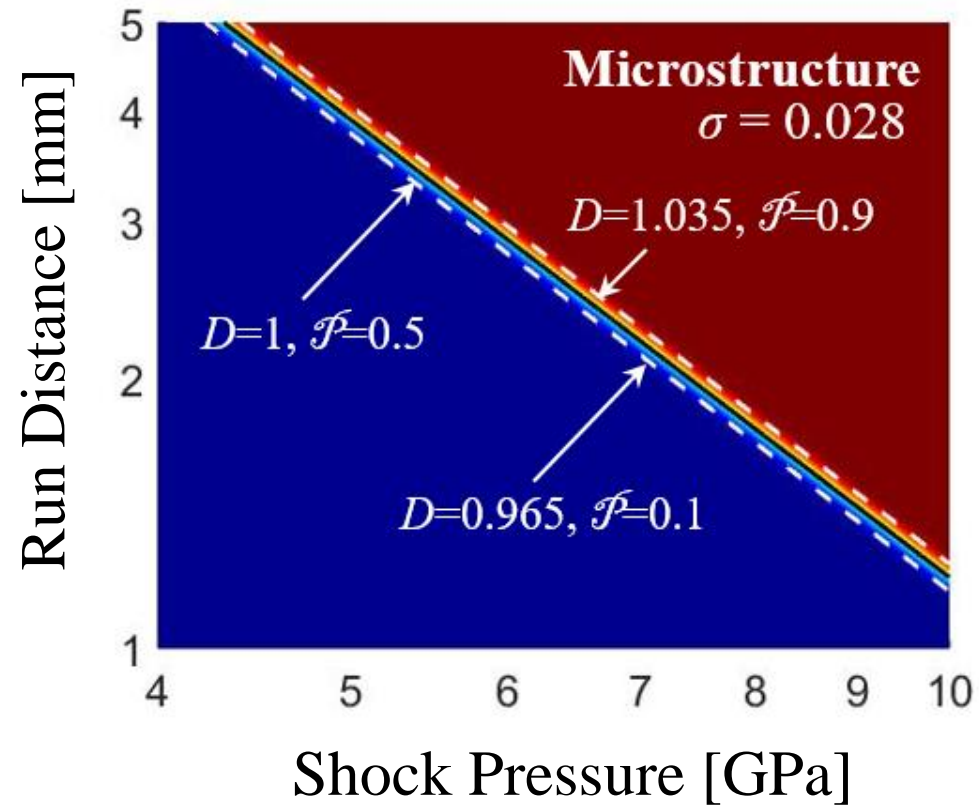


- Microstructure only case is chosen.
- There is overall agreement between the 2D and 3D results.
- 2D have more scatter than 3D, indicating that a single or smaller number of 2D runs may not accurately describe material behavior.

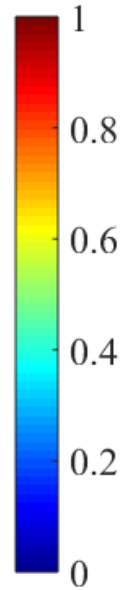
2D Results



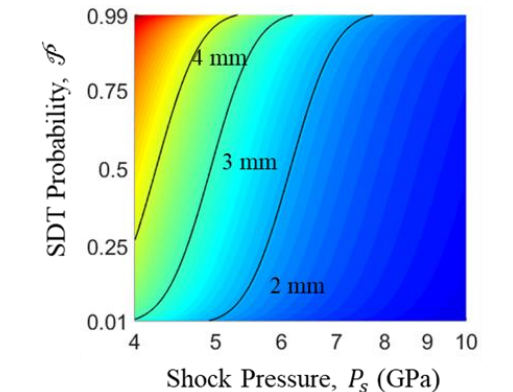
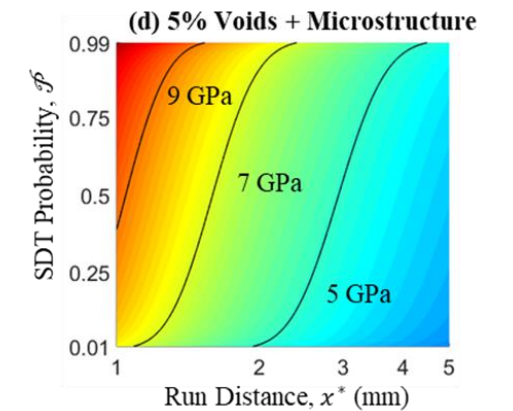
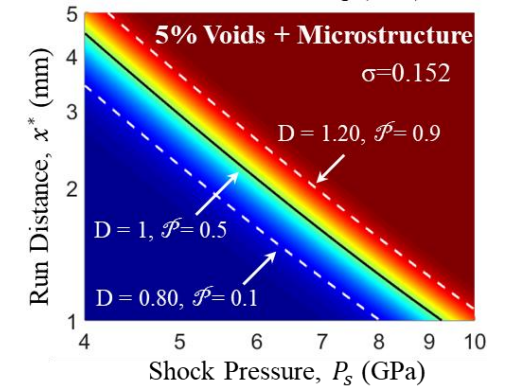
3D Results



Probability of having reached detonation, \mathcal{P}



- MES (microstructure-explicit simulations) at mm size scales allow essential material effects to be captured for prediction of real material behavior.
- SEMSS allow prediction of probabilistic behavior assessment and UQ.
- Analytical relations for macroscopic behavior as functions of material structure for performance and sensitivity are being established and can be used for EM design.



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- The authors are grateful for the collaboration with David Kittell and Cole Yarrington (Sandia National Labs), for their assistance in this work.
- All of my labmates for keep me sane these past five years!

