

# “P.S. I Love You”

(Producing Science of Primarily Soft Stuff via Particle Simulations Plus Statistics Plus Supercomputing, from the Pico Scale to the Pedestrian Scale)

**Gerald J. Wang**

“2020” Howes Scholar Talk

July 19, 2021

M<sup>5</sup> LAB

**Carnegie Mellon University**  
Civil & Environmental Engineering

**There is a simple animating principle behind particle-based simulations... (“it’s classic!”)**

$$m \frac{d^2 \vec{r}}{dt^2} = \vec{F}$$

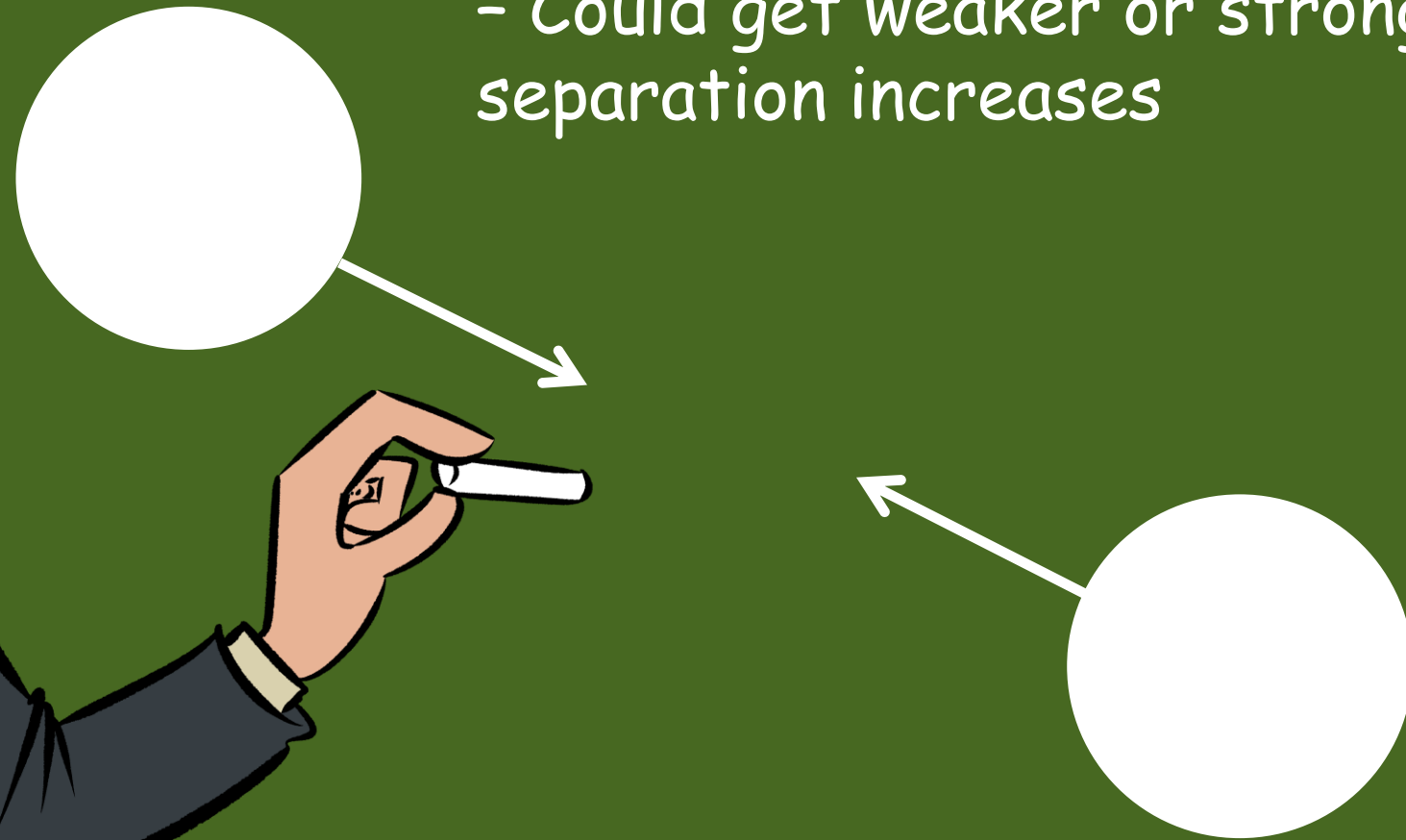
*“As long as you tell me the inter-particle forces,  
I’ll tell you the particle trajectories.”*

*(And there are a lot of places  
where you might get these forces from!)*

# A Few Types of Forces between Particles

## (1) CENTRAL FORCES:

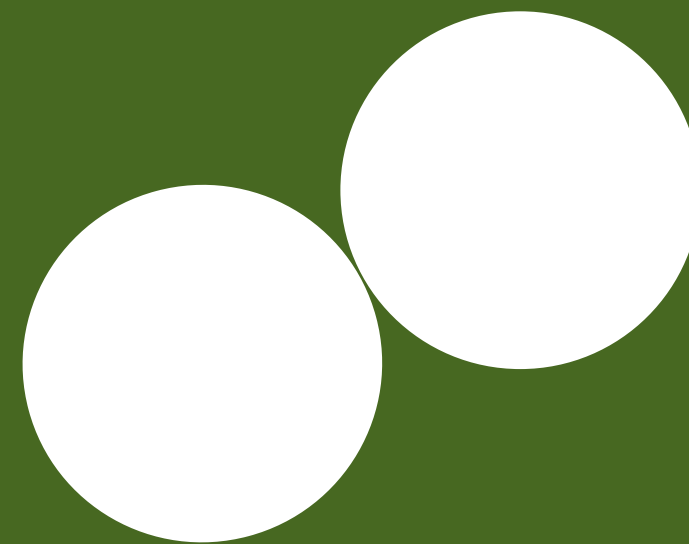
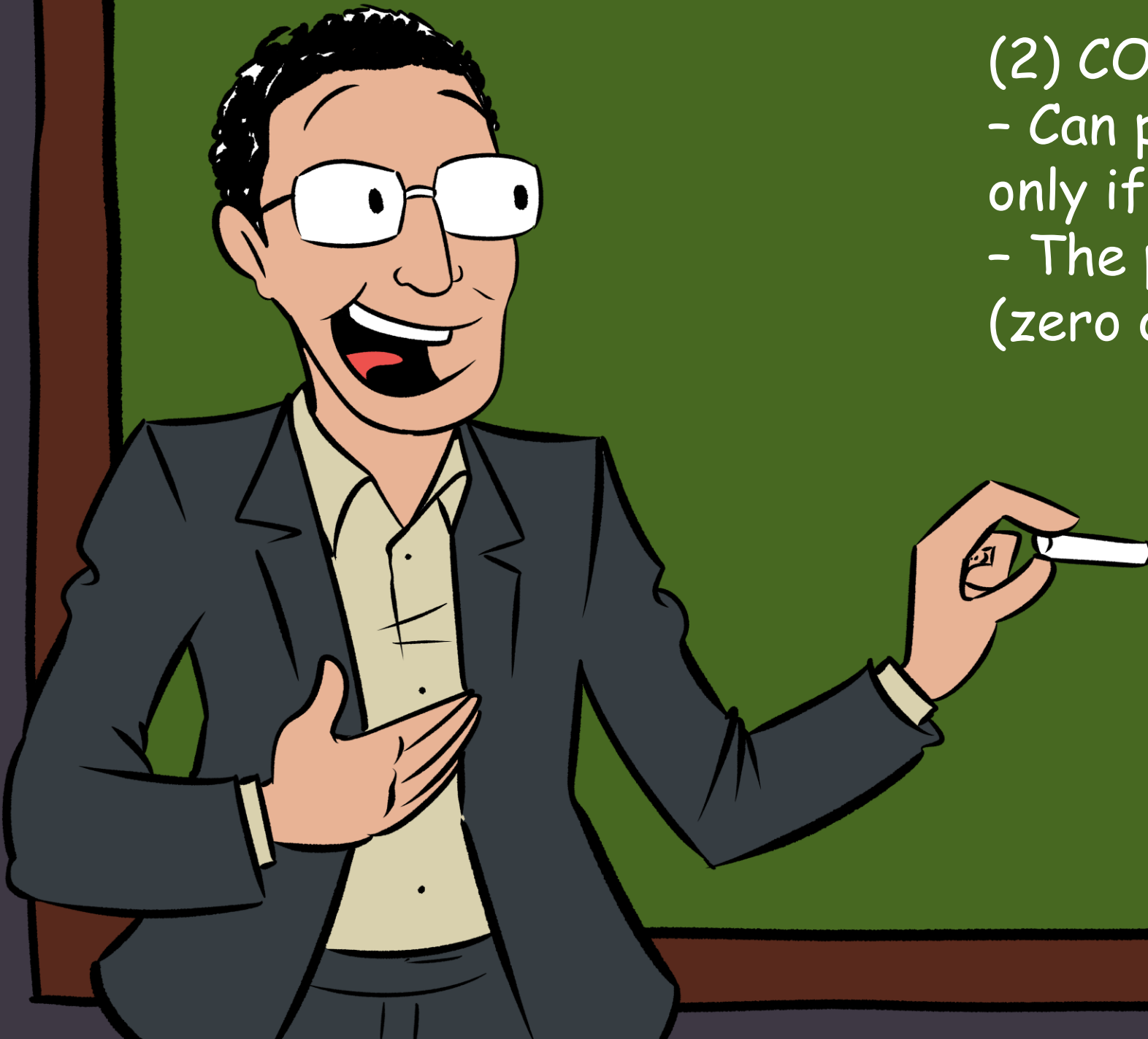
- Act along the particles' line-of-center
- Could get weaker or stronger as separation increases



# A Few Types of Forces between Particles

## (2) CONTACT FORCES:

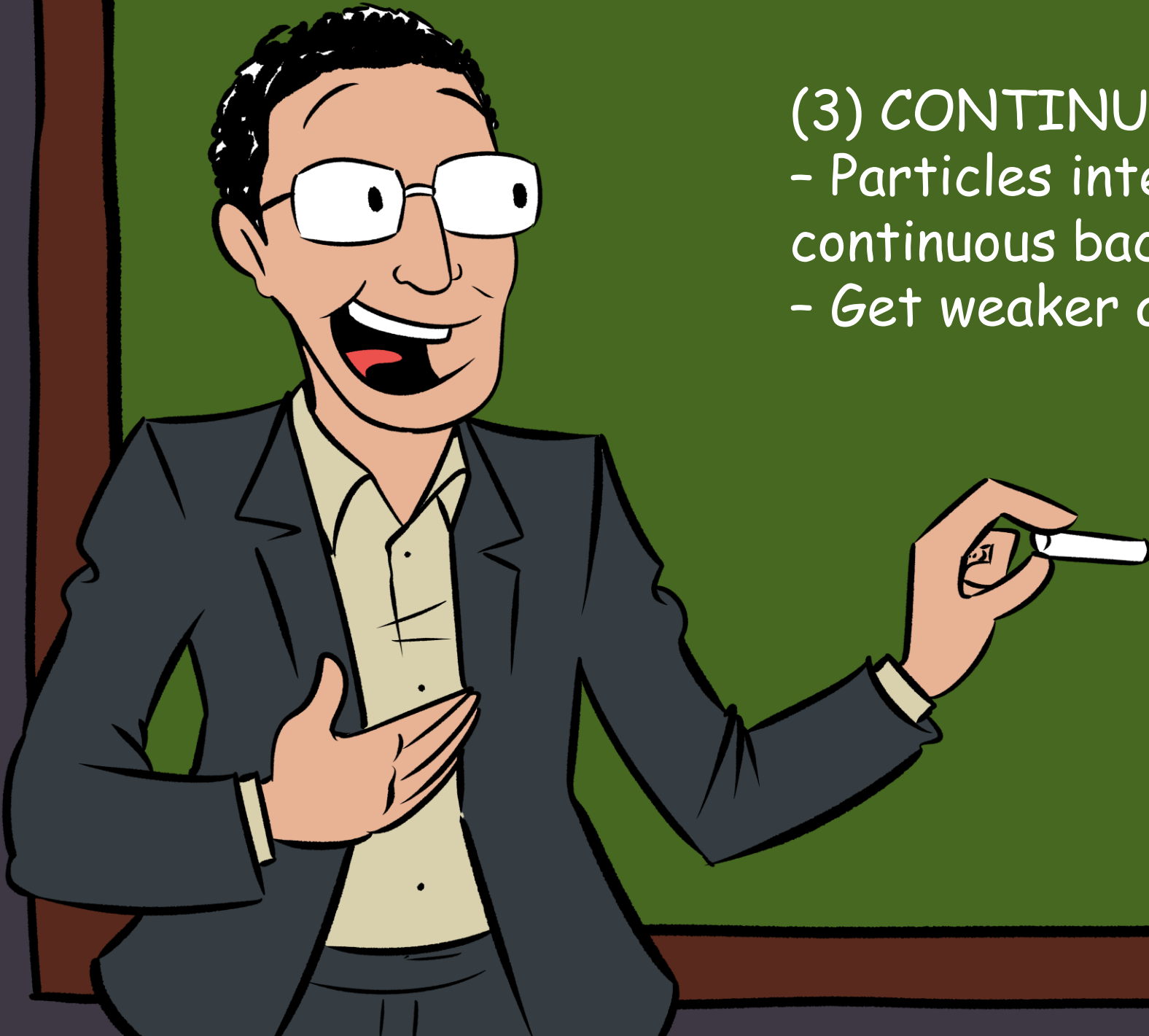
- Can push in many possible directions, but only if...
- The particles are touching (zero otherwise)

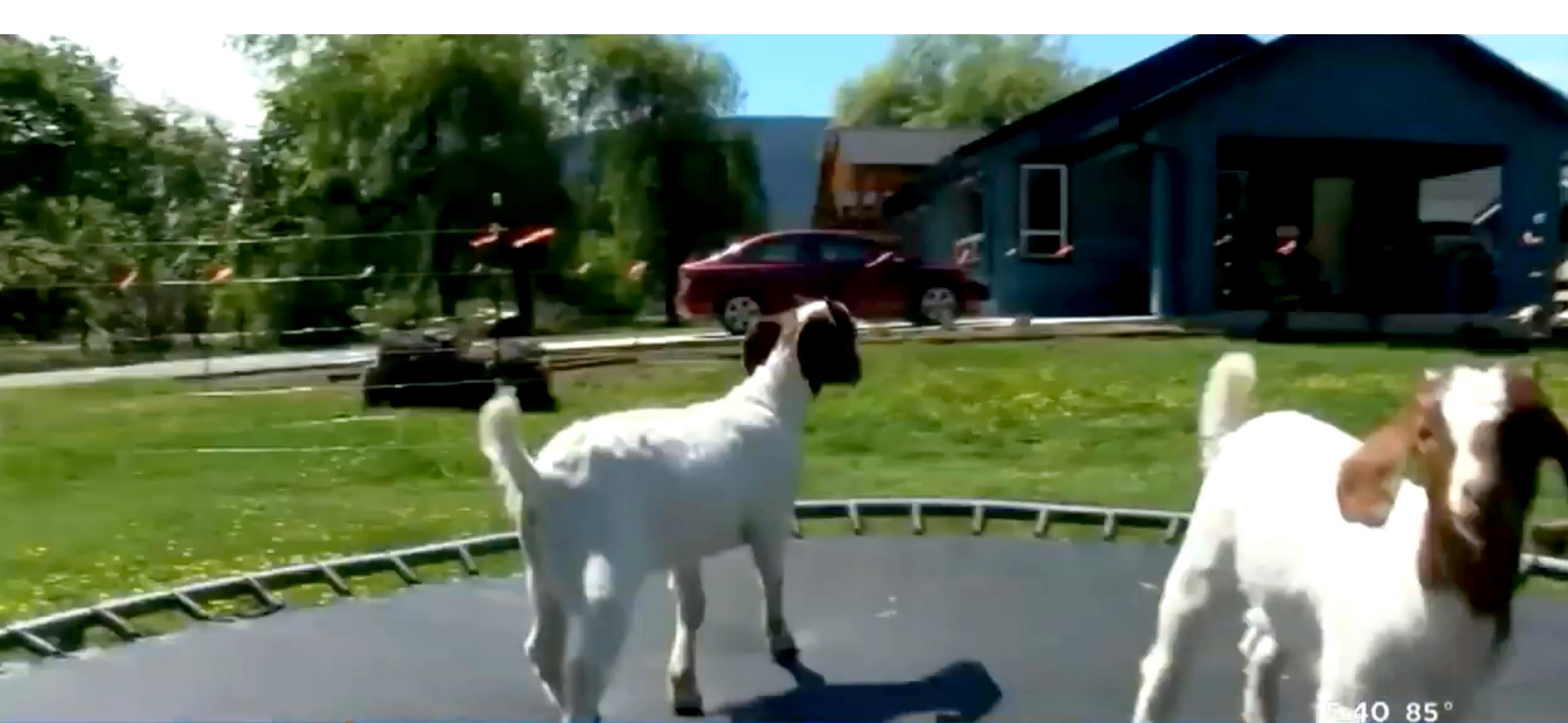


## A Few Types of Forces between Particles

- (3) CONTINUUM-MEDIATED FORCES:
- Particles interact indirectly through a continuous background medium
  - Get weaker as separation increases

*Video demo!*





40 85°

trending  
NOW

# Kids will be Kids

#GOATSONATRAMPOLINE #CANADA #BRITISHCOLOMBIA

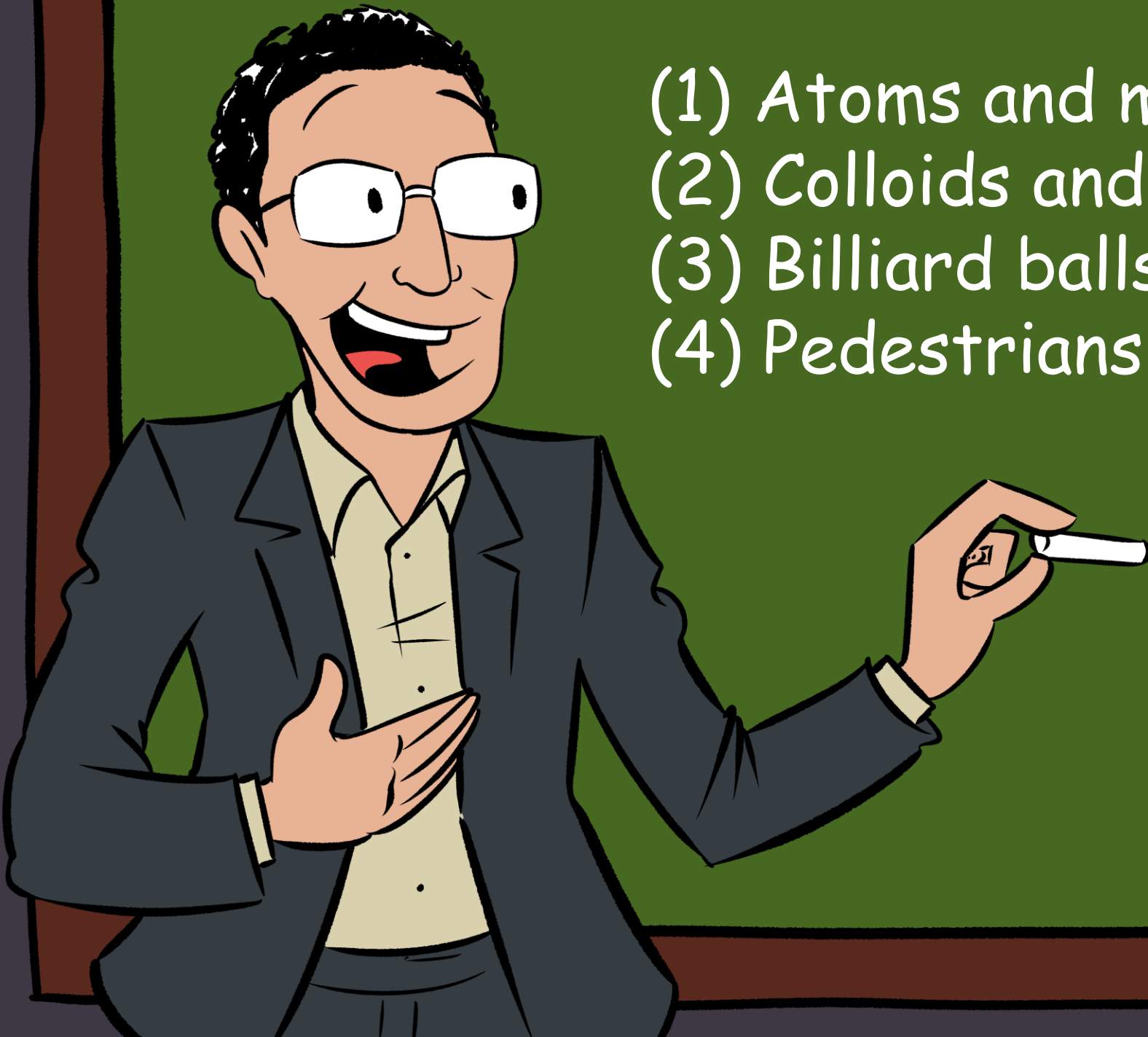


Pause (k)

CBS  
Miami  
SUBSCRIBE

# Particle Simulations at Every Length Scale

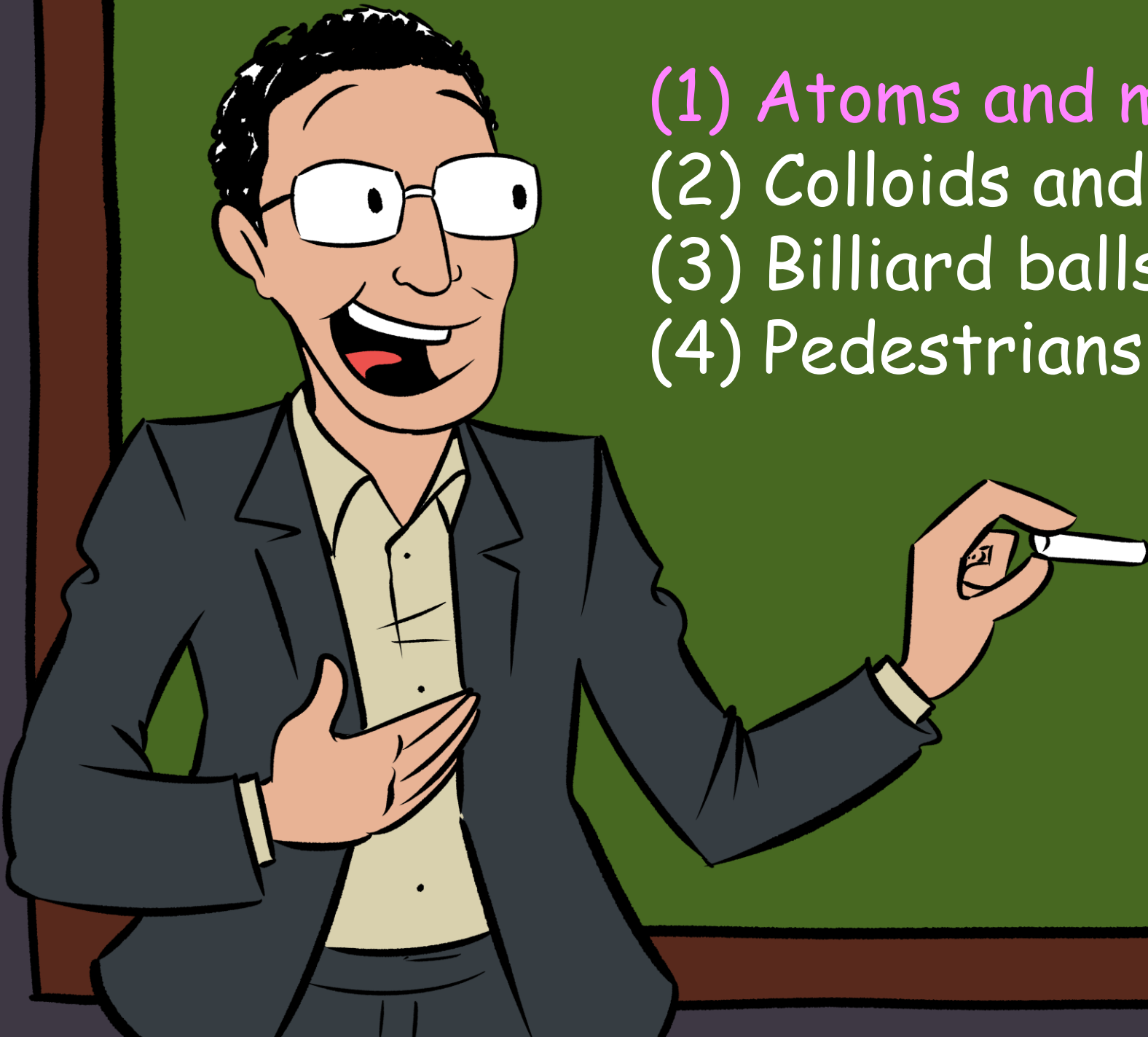
- (1) Atoms and molecules
- (2) Colloids and polymers
- (3) Billiard balls
- (4) Pedestrians



# Particle Simulations at Every Length Scale

- (1) Atoms and molecules
- (2) Colloids and polymers
- (3) Billiard balls
- (4) Pedestrians

- ✓ Forces are... **CENTRAL**
- ✓ Origins include...  
**QUANTUM MECHANICS**  
and **E&M**

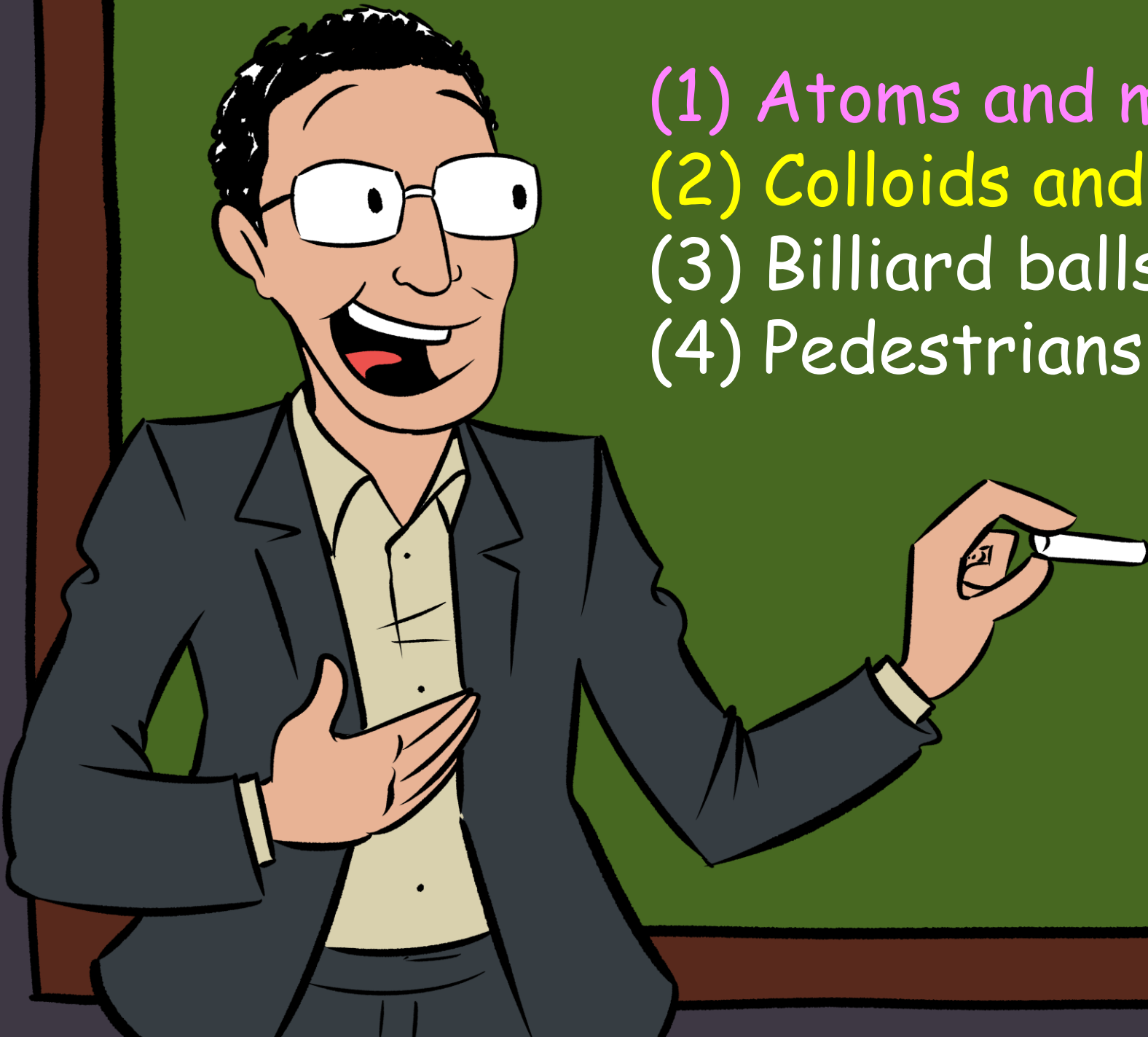




# Particle Simulations at Every Length Scale

- (1) Atoms and molecules
- (2) Colloids and polymers
- (3) Billiard balls
- (4) Pedestrians

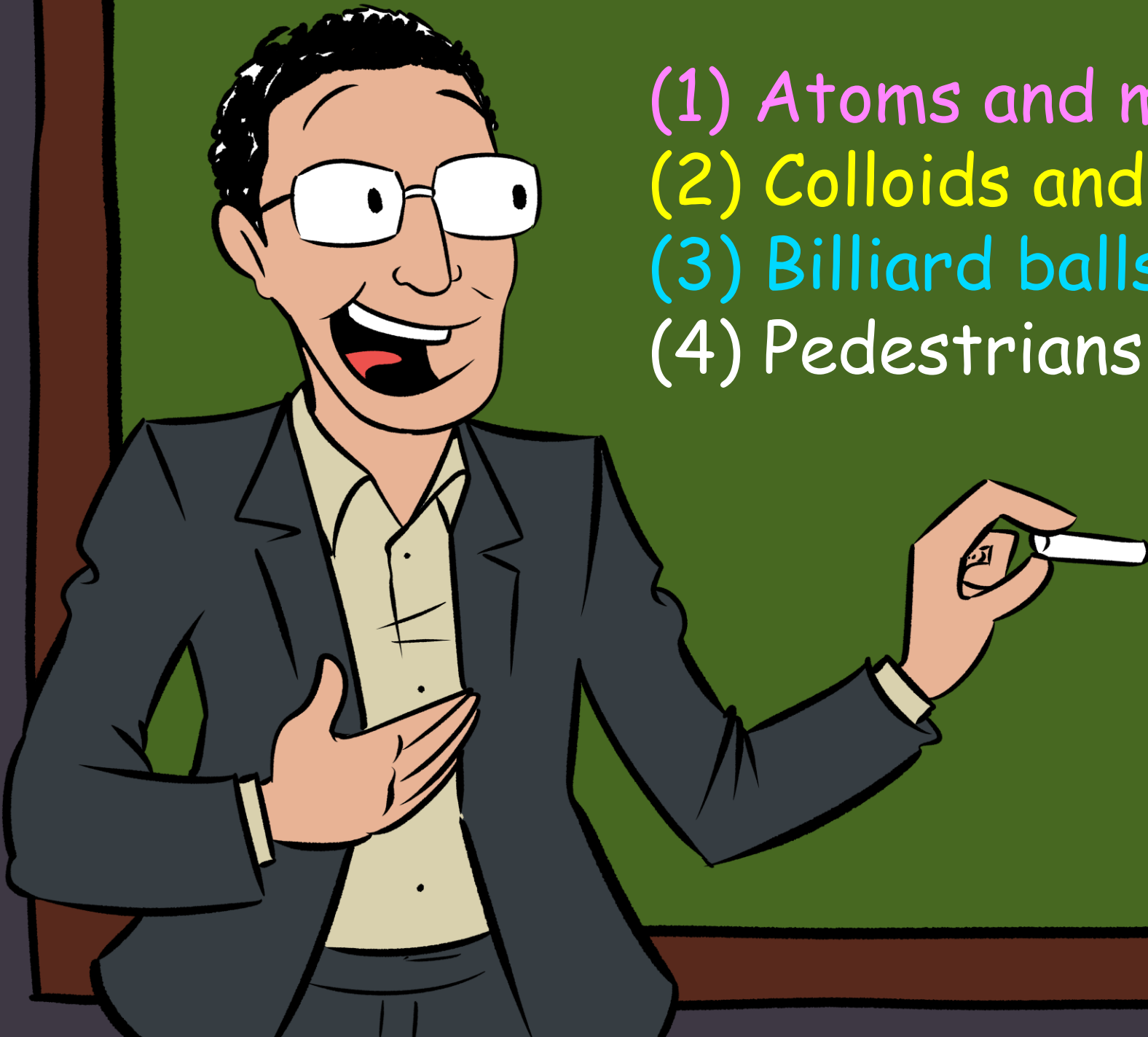
- ✓ Forces are... CENTRAL and CONTINUUM-MEDIATED
- ✓ Origins include...  
E&M, THERMODYNAMICS,  
and HYDRODYNAMICS



# Particle Simulations at Every Length Scale

- (1) Atoms and molecules
- (2) Colloids and polymers
- (3) Billiard balls
- (4) Pedestrians

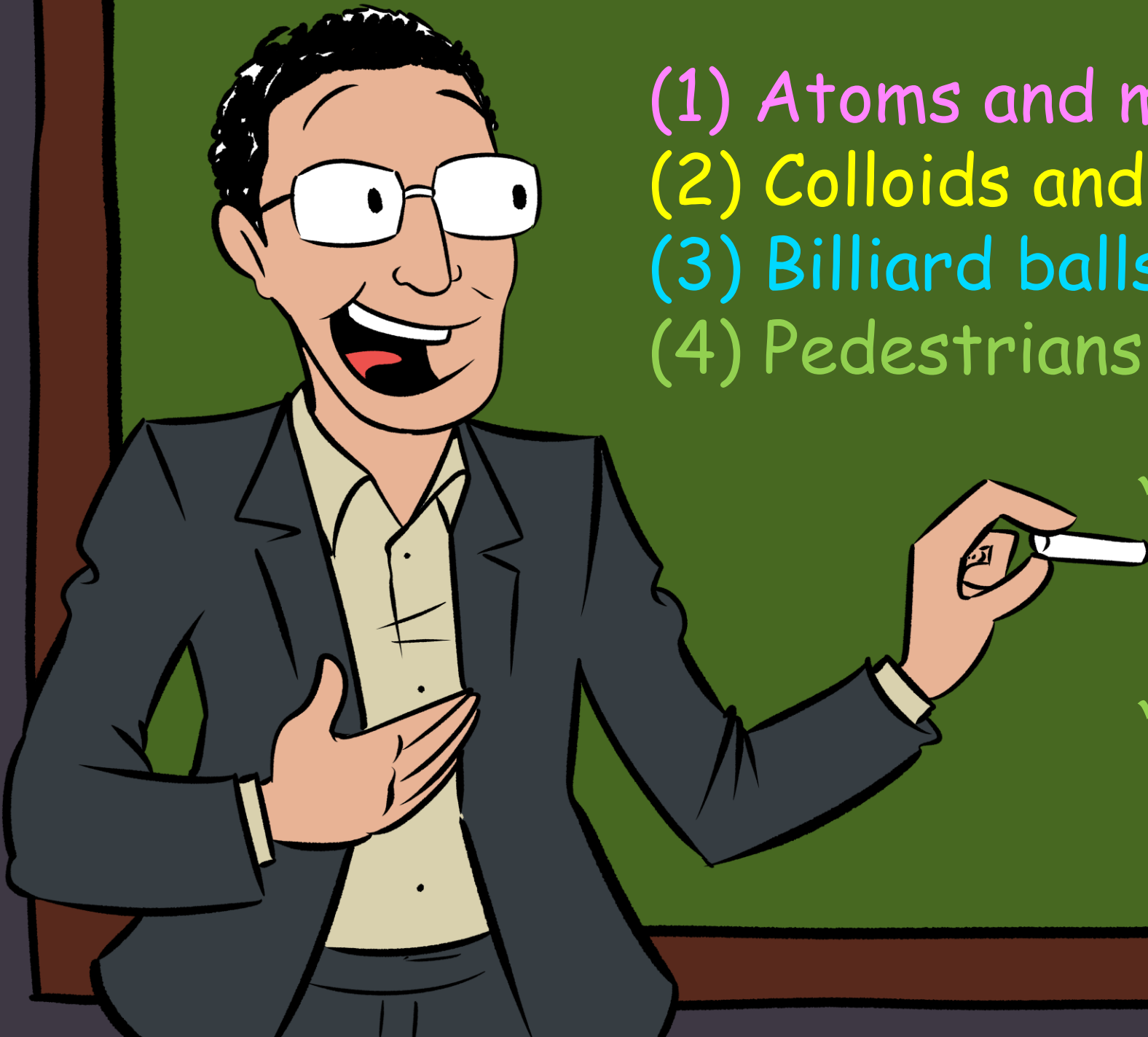
- ✓ Forces are... CONTACT
- ✓ Origins include...  
ELASTICITY and  
FRICTION



# Particle Simulations at Every Length Scale

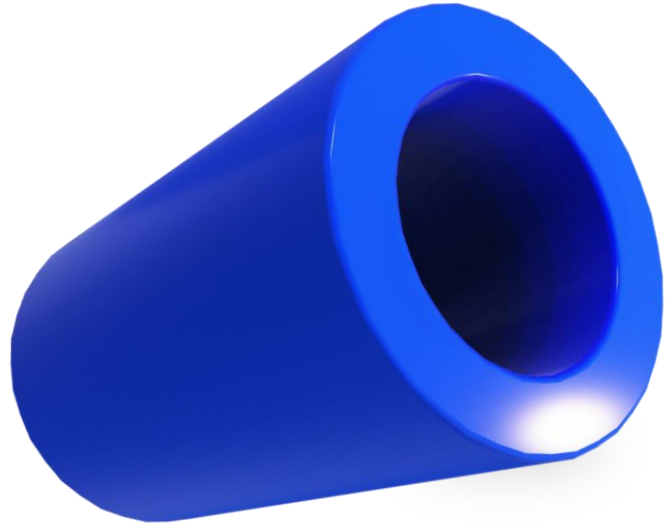
- (1) Atoms and molecules
- (2) Colloids and polymers
- (3) Billiard balls
- (4) Pedestrians

- ✓ Forces are... CONTACT and CENTRAL (and INTERNALLY SUPPLIED!)
- ✓ Origins include... FRICTION and PSYCHOLOGY and CAKE



**“P.S. Something old, something new,  
something borrowed, something blue.”**

# At the nanoscale, fluid slip is a big deal...

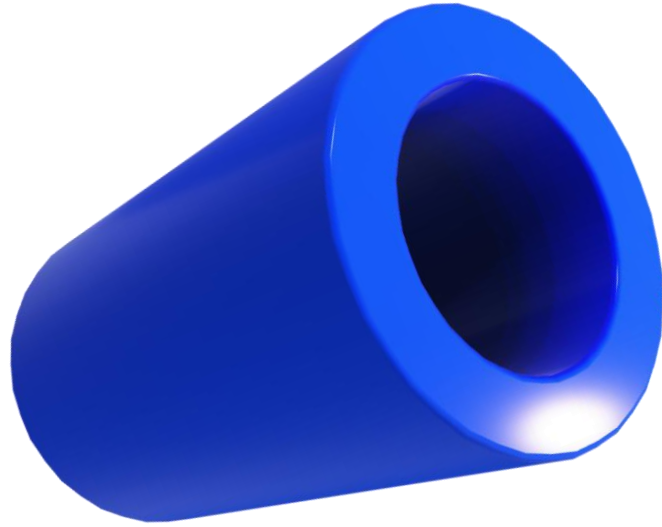


## Pipe Flow

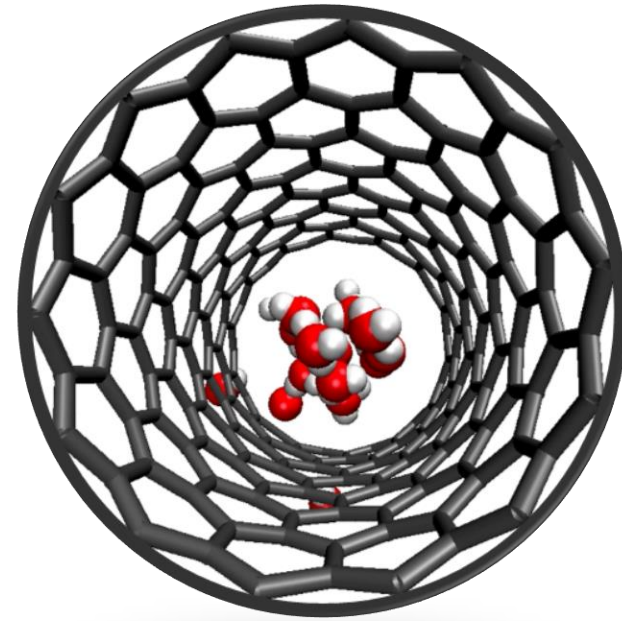
$$Q \sim R^4 \text{ (Hagen-Poiseuille, no slip)}$$

$$Q_{\text{slip}} \sim l_{\text{slip}} R^3 \text{ (additional flow due to slip)}$$

# At the nanoscale, fluid slip is a big deal...



Pipe Flow



$$Q \sim R^4 \text{ (Hagen-Poiseuille, no slip)}$$

$$Q_{\text{slip}} \sim l_{\text{slip}} R^3 \text{ (additional flow due to slip)}$$

$$\frac{l_{\text{slip}}}{R} \sim 1 \text{ (exciting and non-negligible slip phenomena appear)}$$

## NANOSCALE HYDRODYNAMICS

### Enhanced flow in carbon nanotubes

Mainak Majumder\*, Nitin Chopra\*,  
Rodney Andrews†, Bruce J. Hinds\*  
\*Chemical and Materials Engineering  
Department, University of Kentucky, Lexington,  
Kentucky 40506, USA  
e-mail: bhinds@engr.uky.edu  
†Center for Applied Energy Research, Lexington,  
Kentucky 40511, USA

LETTER

doi:10.1038/nature19315

### Massive radius-dependent flow slippage in carbon nanotubes

Eleonora Secchi<sup>1</sup>, Sophie Marbach<sup>1</sup>, Antoine Niguès<sup>1</sup>, Derek Stein<sup>1,2</sup>, Alessandro Siria<sup>1</sup> & Lydéric Bocquet<sup>1</sup>

### Fast Mass Transport Through Sub-2-Nanometer Carbon Nanotubes

Jason K. Holt<sup>1,\*</sup>, Hyung Gyu Park<sup>1,2,\*</sup>, Yinmin Wang<sup>1</sup>, Michael Stadermann<sup>1</sup>, Alexander B. Artyukhin<sup>1</sup>, Costas P. Grigoropoulos<sup>2</sup>, Aleksandr Noy<sup>1</sup>, Olga Bakajin<sup>1,†</sup>

<sup>1</sup> Chemistry and Materials Science Directorate, Lawrence Livermore National Laboratory, Livermore, CA 94550, USA.

<sup>2</sup> Department of Mechanical Engineering, University of California, Berkeley, CA 94720, USA.

† To whom correspondence should be addressed. E-mail: bakajin1@llnl.gov

\* These authors contributed equally to this work.

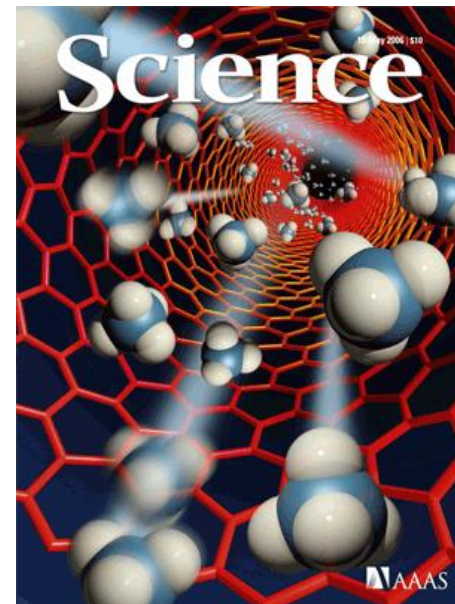
- Hide authors and affiliations

Science 19 May 2006:  
Vol. 312, Issue 5776, pp. 1034-1037  
DOI: 10.1126/science.1126298

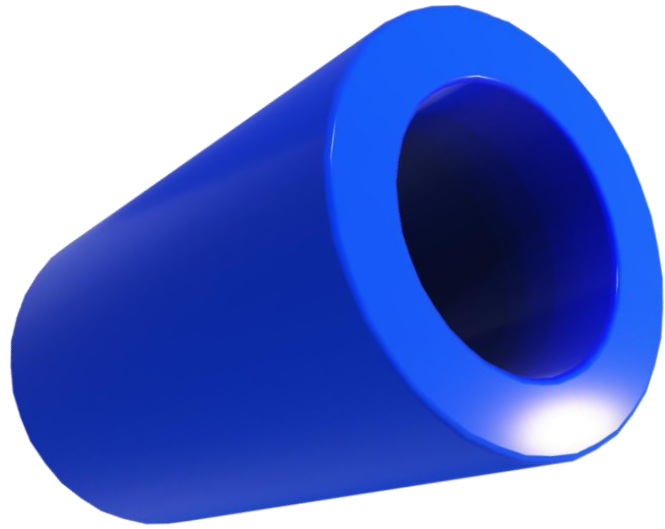
### Fluid flow in carbon nanotubes and nanopipes

M. Whitby & N. Quirke

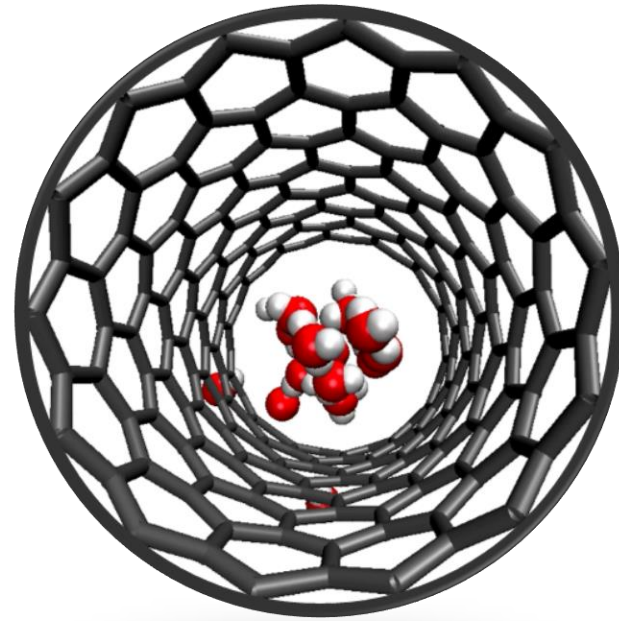
Nature Nanotechnology 2, 87-94(2007) | Cite this article



# At the nanoscale, fluid slip is a big deal...



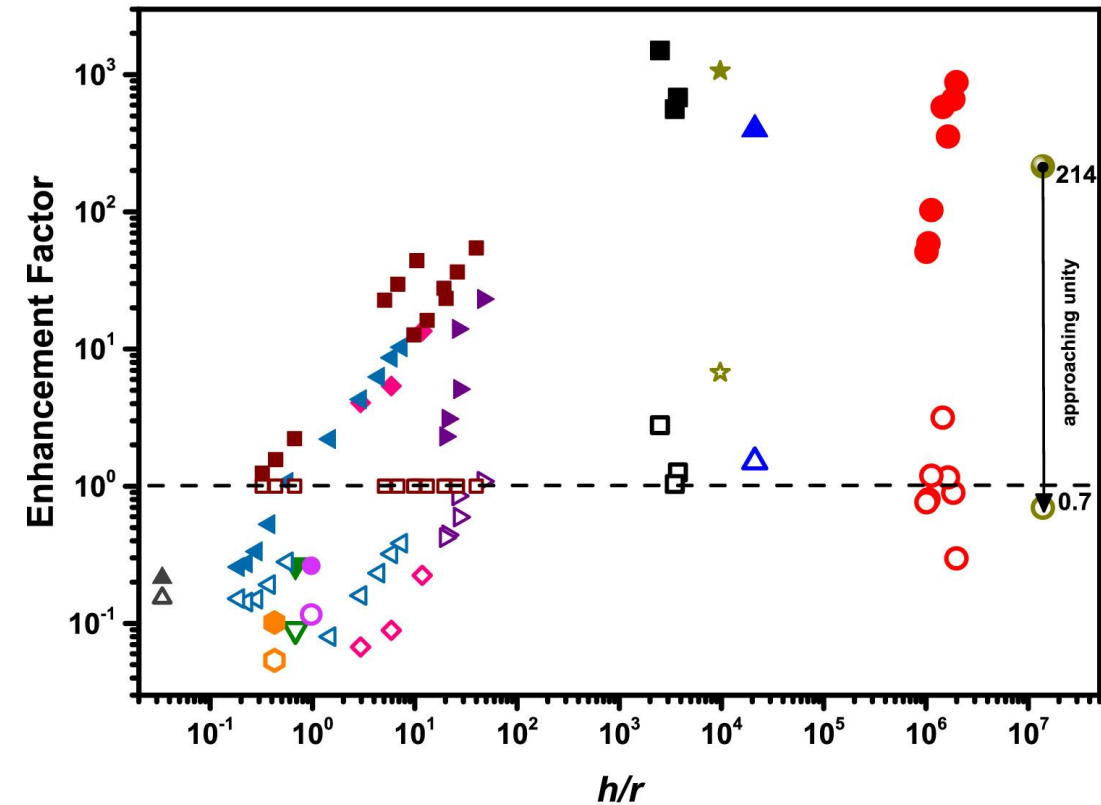
Pipe Flow



$$Q \sim R^4 \text{ (Hagen-Poiseuille, no slip)}$$

$$Q_{\text{slip}} \sim l_{\text{slip}} R^3 \text{ (additional flow due to slip)}$$

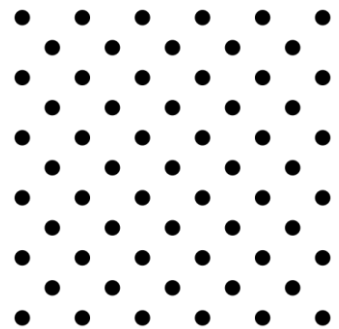
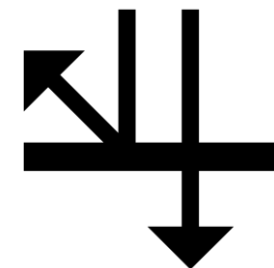
$$\frac{l_{\text{slip}}}{R} \sim 1 \text{ (exciting and non-negligible slip phenomena appear)}$$



- $Q_{\text{EXP}}/Q_{\text{HP}}$ , Holt *et al.*<sup>6</sup>
- $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Holt *et al.*<sup>6</sup>
- $Q_{\text{EXP}}/Q_{\text{HP}}$ , Qin *et al.*<sup>40</sup>
- $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Qin *et al.*<sup>40</sup>
- ▲  $Q_{\text{EXP}}/Q_{\text{HP}}$ , Kim *et al.*<sup>41</sup>
- △  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Kim *et al.*<sup>41</sup>
- ▼  $Q_{\text{EXP}}/Q_{\text{HP}}$ , O'Hern *et al.*<sup>19</sup>
- ▽  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , O'Hern *et al.*<sup>19</sup>
- ◆  $Q_{\text{EXP}}/Q_{\text{HP}}$ , Surwade *et al.*<sup>42</sup>
- ◇  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Surwade *et al.*<sup>42</sup>
- ◆  $Q_{\text{NEMD}}/Q_{\text{HP}}$ , Walther *et al.*<sup>43</sup>
- ◇  $Q_{\text{NEMD}}/Q_{\text{CHP}}$ , Walther *et al.*<sup>43</sup>
- ▲  $Q_{\text{NEMD}}/Q_{\text{HP}}$ , Suk *et al.*<sup>23</sup>
- △  $Q_{\text{NEMD}}/Q_{\text{CHP}}$ , Suk *et al.*<sup>23</sup>
- ★  $Q_{\text{EXP}}/Q_{\text{HP}}$ , Majumder *et al.*<sup>5</sup>
- ★  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Majumder *et al.*<sup>5</sup>
- ▼  $Q_{\text{EXP}}/Q_{\text{HP}}$ , Secchi *et al.*<sup>17</sup>
- ▽  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Secchi *et al.*<sup>17</sup>
- $Q_{\text{EXP}}/Q_{\text{HP}}$ , Bui *et al.*<sup>44</sup>
- $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Bui *et al.*<sup>44</sup>
- ▲  $Q_{\text{EXP}}/Q_{\text{HP}}$ , Qin *et al.*<sup>45</sup>
- △  $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Qin *et al.*<sup>45</sup>
- $Q_{\text{EXP}}/Q_{\text{HP}}$ , Yang *et al.*<sup>46</sup>
- $Q_{\text{EXP}}/Q_{\text{CHP}}$ , Yang *et al.*<sup>46</sup>
- $Q_{\text{NEMD}}/Q_{\text{HP}}$ , This work
- $Q_{\text{NEMD}}/Q_{\text{CHP}}$ , This work

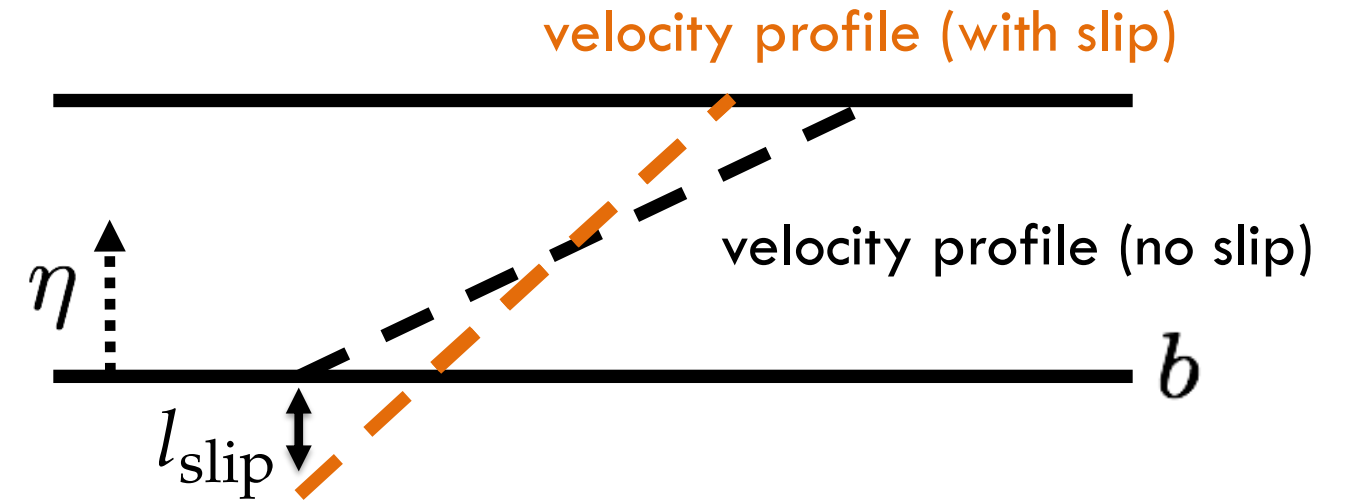
[Heiranian and Aluru, *ACS Nano* 2020, 14, 1, 272–281]

Applications galore (“something blue”)...



# “Business as usual” is the Navier slip condition...

- Assumption: Slip velocity is **linear** in the velocity gradient at the boundary.
- Slip length is the distance within the boundary at which the (extrapolated) velocity profile matches the boundary velocity.
- The Navier slip condition has been shown (rigorously) to hold **for dilute fluids**.
- **Key question: What is the appropriate slip condition for dense fluids?**



$$u_{\text{slip}} = l_{\text{slip}} \left. \frac{\partial u}{\partial \eta} \right|_b$$



# To model slip, Molecular-Kinetic Theory (MKT) is a jump in the right direction.

$$u_{\text{slip}} = \frac{2l_j}{\tau_j} \exp\left(-\frac{\alpha\varepsilon}{k_B T}\right) \sinh\left(\frac{l_j \mu}{2\sigma_{\text{FL}} k_B T} \dot{\gamma}\right)$$

Viscosity

Shear rate

[Wang and Hadjiconstantinou, *Phys. Rev. Fluids* 2019, 4(6), 064201]

[Wang and Hadjiconstantinou, *Phys. Rev. Fluids* 2017, 2(9), 094201]

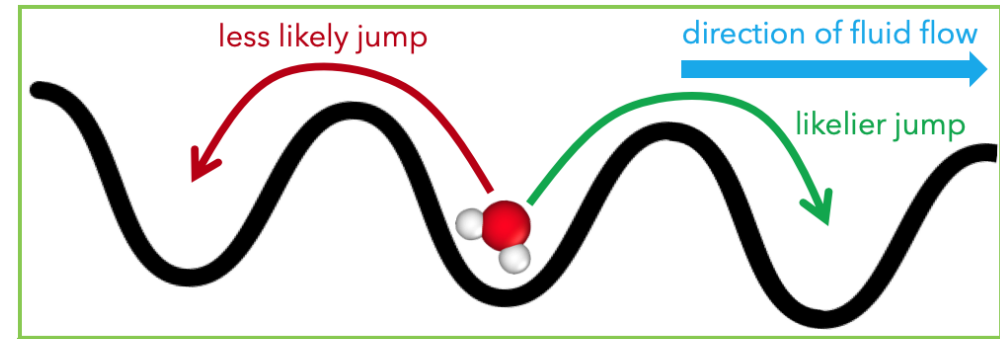
[Blake and Haynes, *J. Colloid Interface Sci.* 30 (1969)]

Length scale for jumps

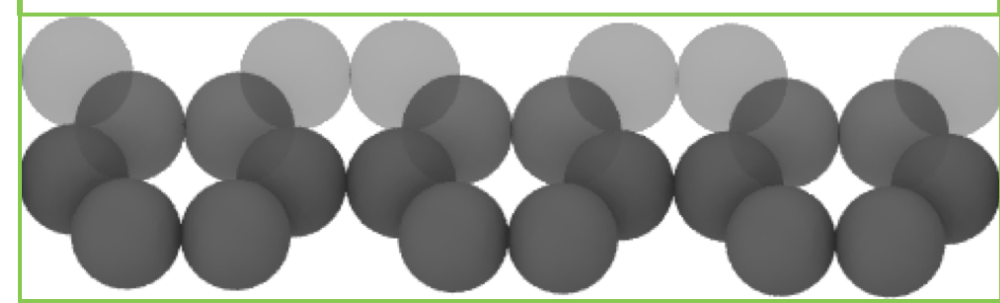
Fluid-solid interaction energy

Surface density of interfacial fluid layer

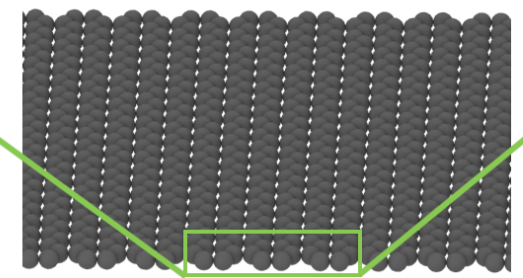
Time scale for jump attempts



periodic energy landscape



graphene (zoomed in)



graphene

In the appropriate limit, MKT recovers the Navier slip condition:

$$u_{\text{slip}} = l_{\text{slip}} \dot{\gamma}$$

$$l_{\text{slip}} = \frac{l_j^2 e^{-\alpha\varepsilon/(k_B T)} \mu}{\tau_j \sigma_{\text{FL}} k_B T}$$

Slip length directly linked to microscopic parameters!

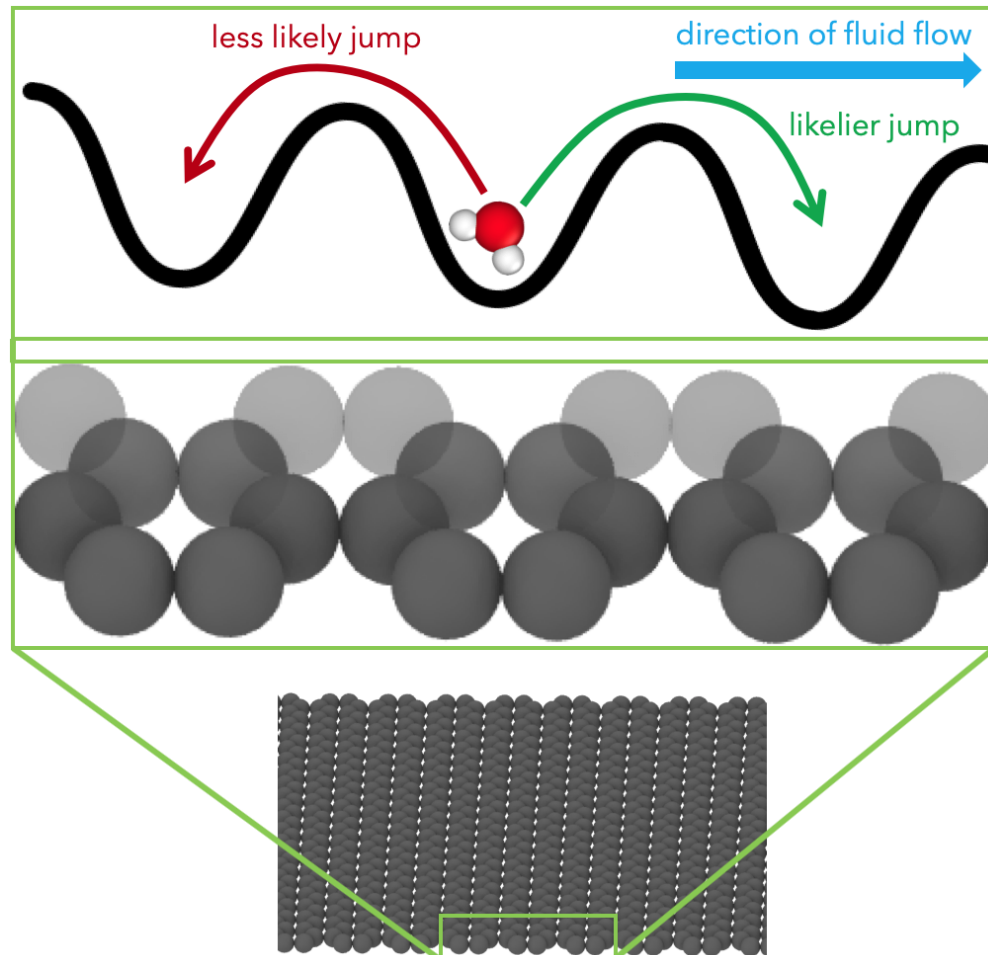
# To model slip, Molecular-Kinetic Theory (MKT) is a jump in the right direction.

$$u_{\text{slip}} = \frac{2l_j}{\tau_j} \exp\left(-\frac{\alpha\varepsilon}{k_B T}\right) \sinh\left(\frac{l_j \mu}{2\sigma_{\text{FL}} k_B T} \dot{\gamma}\right) \quad l_{\text{slip}} = \frac{l_j^2 e^{-\alpha\varepsilon/(k_B T)} \mu}{\tau_j \sigma_{\text{FL}} k_B T}$$

[Wang, under review]

[Wang and Hadjiconstantinou, *Phys. Rev. Fluids* 2019, 4(6), 064201]

[Wang and Hadjiconstantinou, *Phys. Rev. Fluids* 2017, 2(9), 094201]



**MKT has been validated against:**

**MD simulations**

**(in house and from literature)**

[Thompson and Troian, *Nature* 1997, 389]

[Martini, Hsu, Patankar, and Lichter, *Phys. Rev. Lett.* 2008, 100]



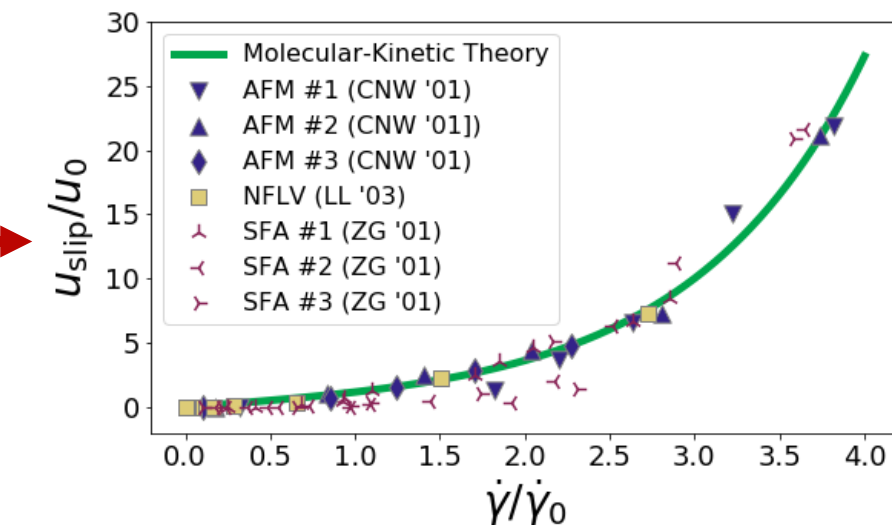
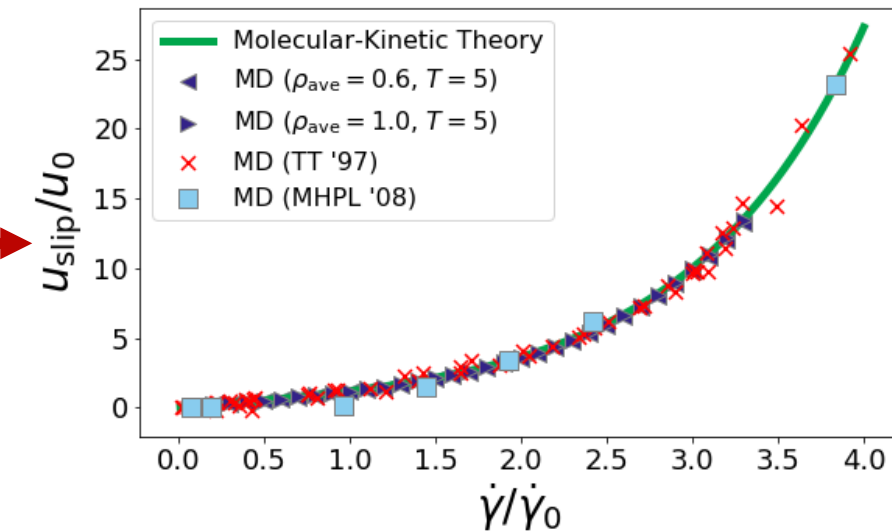
**and**

**experiments**

[Craig, Neto, and Williams, *Phys. Rev. Lett.* 2001, 87]

[Zhu and Granick, *Phys. Rev. Lett.* 2001, 87]

[Léger, *J. Phys.: Cond. Matt.* 2003, 15]



# Governing equations for pedestrian dynamics

$$\vec{F} = m \frac{\vec{v}_{\text{desired}} - \vec{v}_{\text{instantaneous}}}{\tau} - \vec{\nabla} U + \vec{R}$$

**The "selfish" term:** Each pedestrian has a desired velocity and tries to stick to that velocity (proportional control).

**The "social interaction" term:** Pedestrians experience forces that depend on spatial configuration relative to other pedestrians.

**The "random" term:** Each pedestrian is given a *tiny* random (Gaussian) kick to reduce stalling events.

$$U = U_{\text{far}} + U_{\text{near}}$$

**The "collision avoidance" term:** Pedestrians try to avoid each other in general, with a characteristic "personal space" set by  $d_0$ . **This is the focus of our work.**

$$U_{\text{far}}(d) = K e^{-d/d_0}$$

**The "brushing shoulders" term:** In the event two pedestrians are near contact, they experience a frictional force.

For more on social force models, see, e.g.  $\longrightarrow$

[Helbing and Molnar, *Phys. Rev. E* 1995, 51(5), 4282–4286]  
 [Helbing, Farkas, and Vicsek, *Nature* 2000, 407, 487–490]  
 [Koyama *et al.*, *Artif. Life Robot.* 2020, 25, 529–536]

# How does the need for increased social distancing affect pedestrian flows in confined environments?

$$\frac{d_0}{d_{\text{walkway}}} \lesssim 1$$



$$\frac{d_0}{d_{\text{walkway}}} \sim 1$$

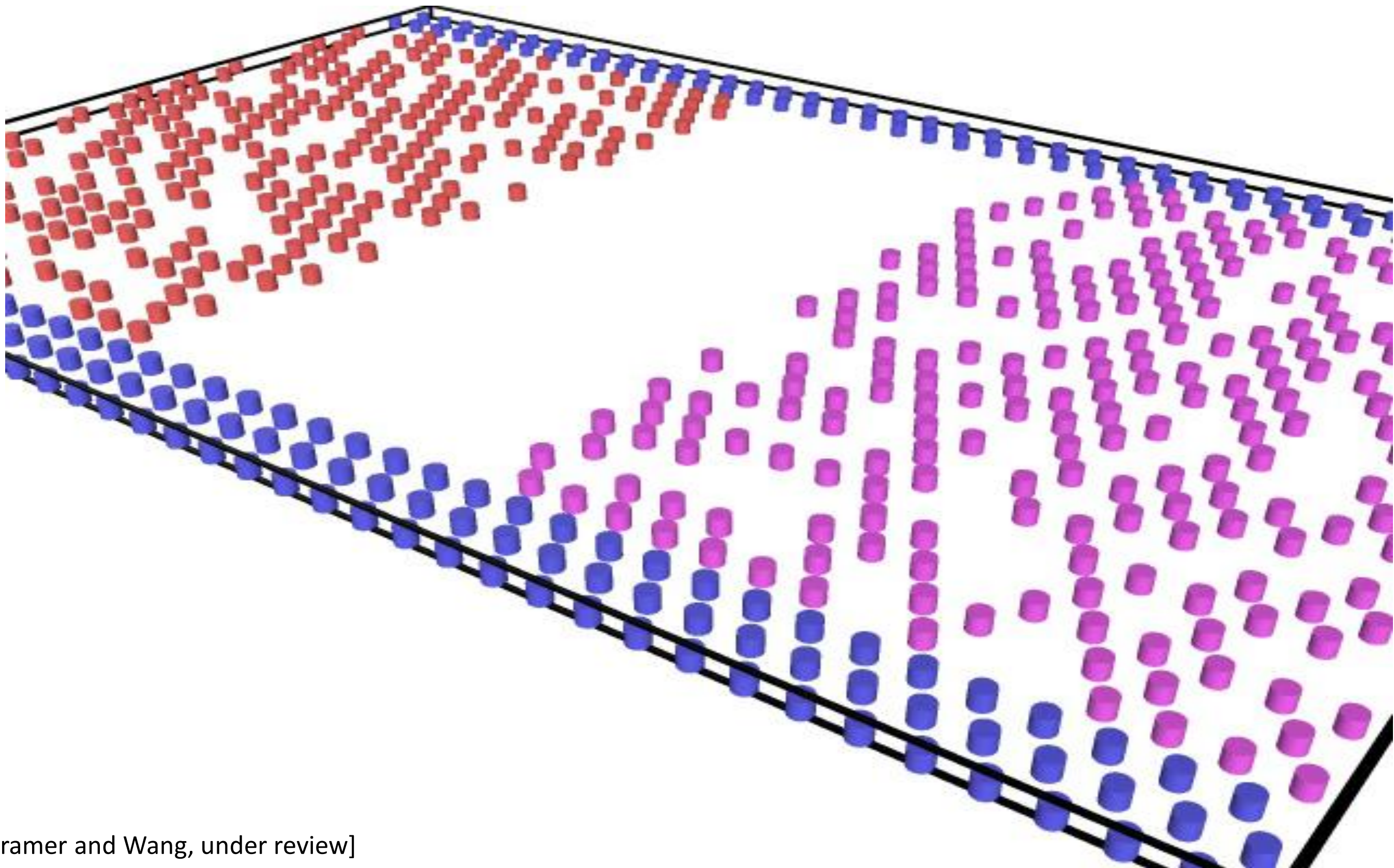


Pedestrians in Piura, Peru

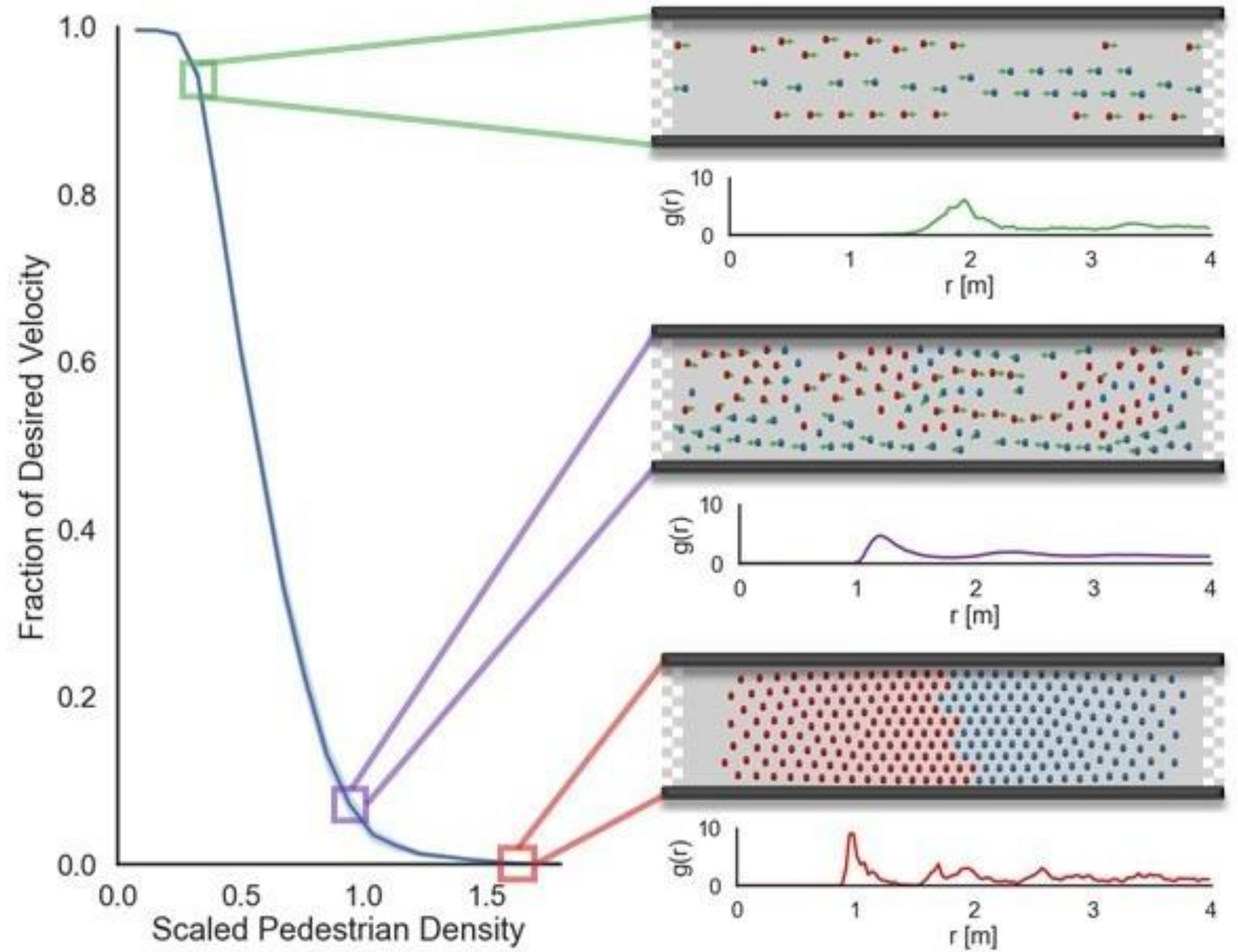


Himeji, Japan - April 06, 2020

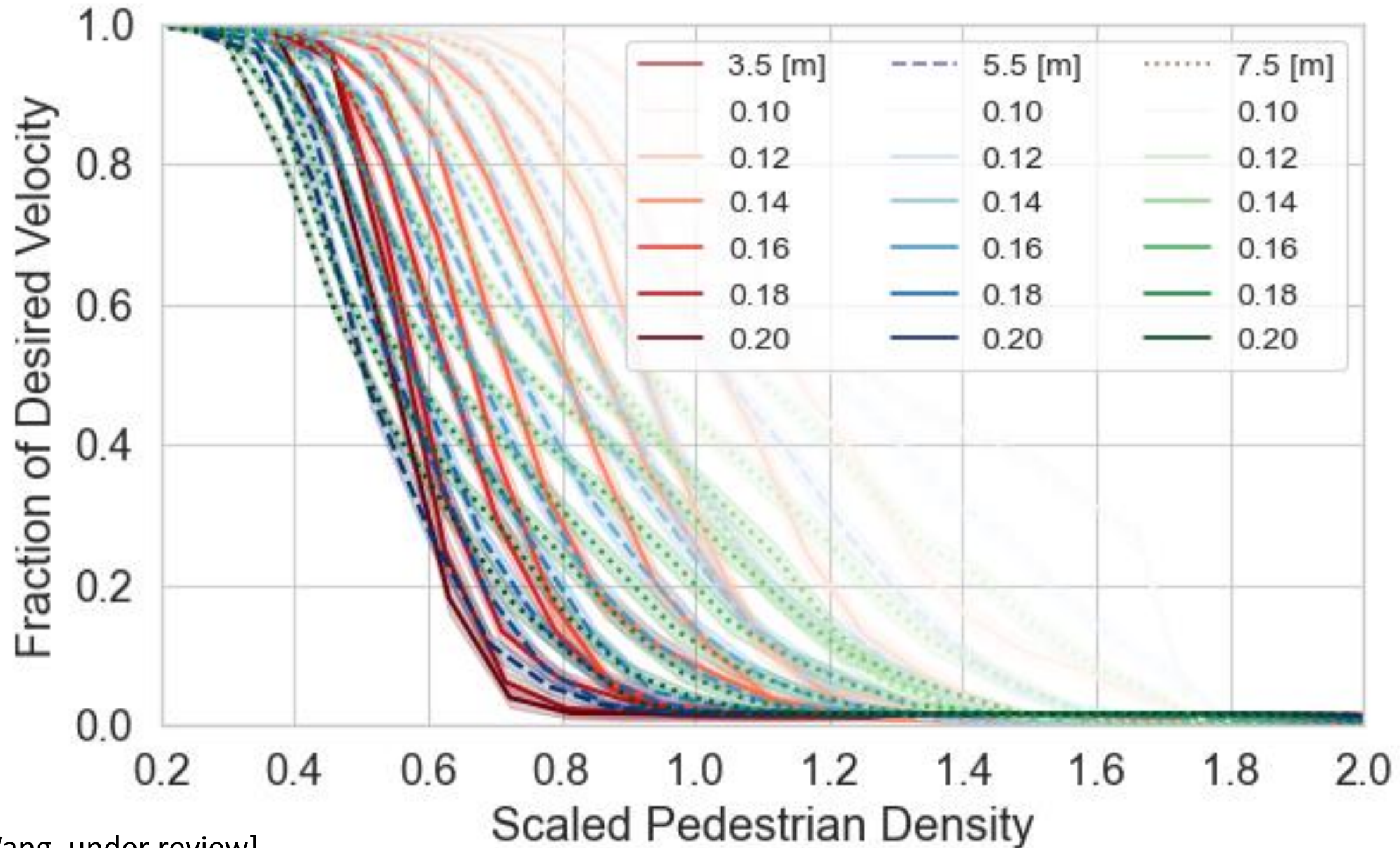




# More people, more problems...



... and more preference for social distance, more “problems” too...

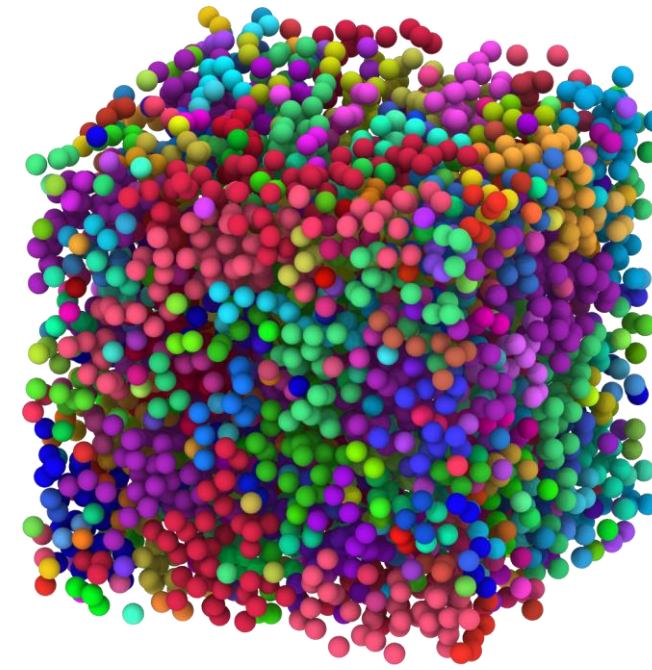


**“P.S. A picture is worth a thousand words.”**

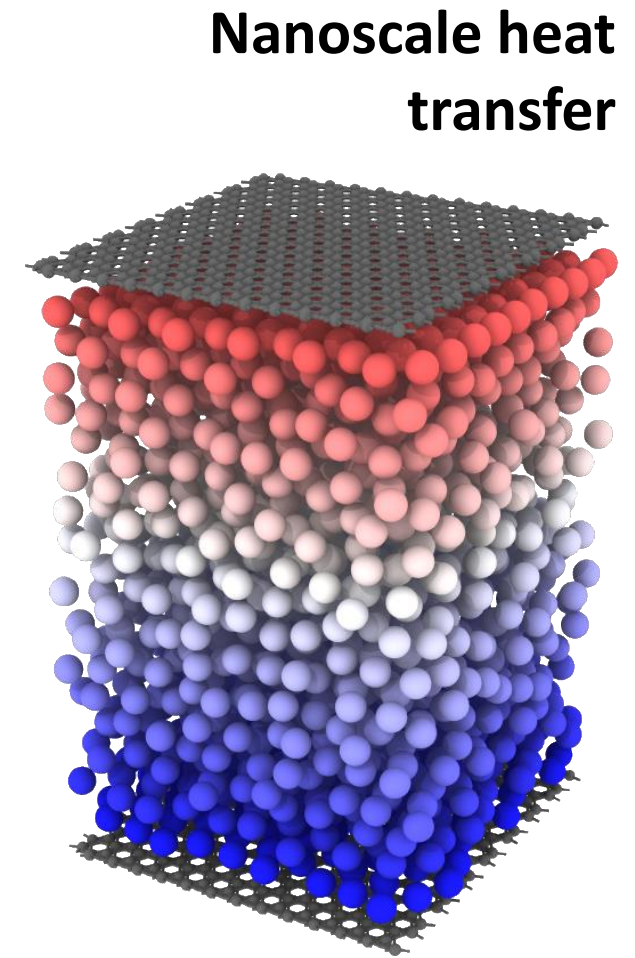


# Laboratory for Mechanics of Materials via Molecular and Multiscale Methods (M<sup>5</sup> Lab at CMU)

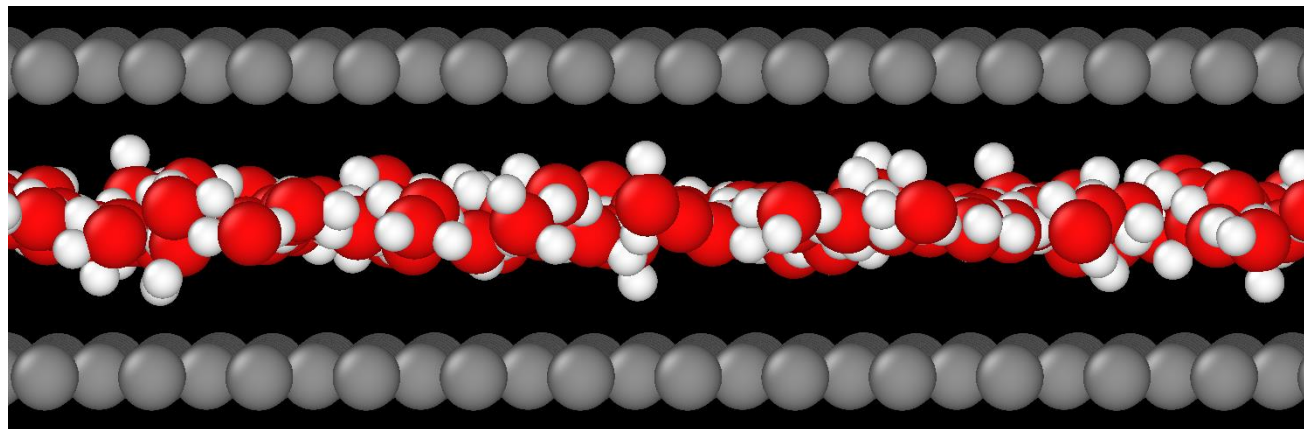
- Statistical physics and molecular-scale mechanics of fluids, polymers, soft matter, and active matter.
- Micro- and nanoscale transport phenomena.
- High-performance computational science and engineering (both theory- and data-driven).
- Molecular-scale design principles for sustainability.
- Physics of livable and equitable urban systems.



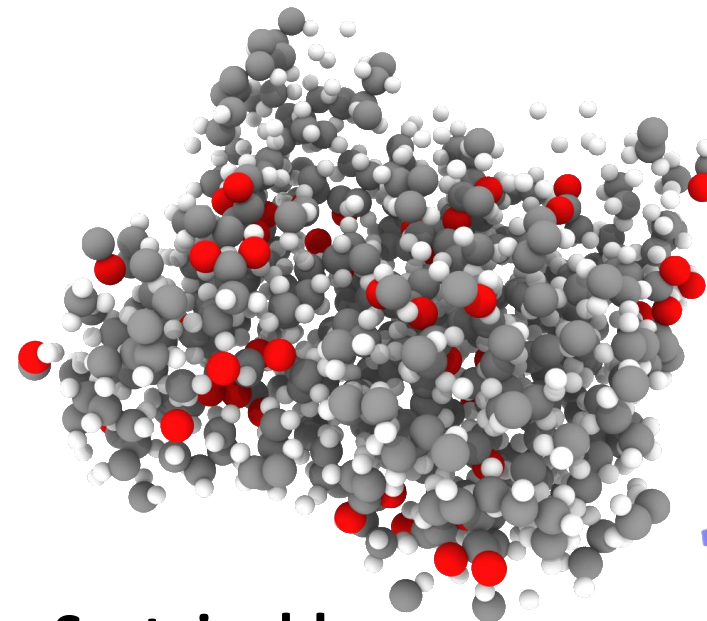
**Hydrodynamics of suspensions**



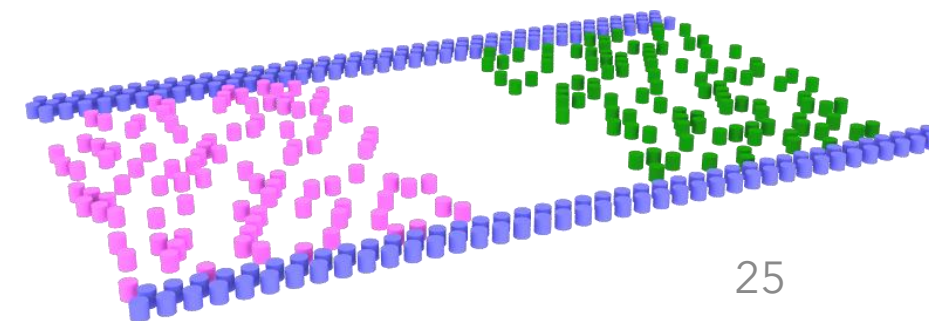
**Nanoscale heat transfer**



**Nanoscale hydrodynamics**



**Sustainable polymers**



**Pedestrian flows**

**“P.S. One good turn deserves another.”**

**P.S. Something old, something new,  
something borrowed, something blue.**

**P.S. A picture is worth a thousand words.  
(or at least 10 extra minutes of talk time :P)**

**P.S. One good turn deserves another.**



**Nicolas Hadjiconstantinou**  
MIT Mechanical Engineering

**Petros Koumoutsakos**  
ETHZ Computational  
Science

**Ju Li**  
MIT Nuclear Engineering



**Daniel Blankschtein**  
MIT Chemical Engineering

**Rohit Karnik**  
MIT Mechanical Engineering

**Stephen Gray**  
ANL Center for Nanoscale  
Materials

**Many thanks to the M<sup>5</sup> LAB team...**

- **Mehul Bapat (G)**
- **Vince Cheng (BS '24)**
- **Arman Ghaffarizadeh (G)**
- **Kelby Kramer ('22)**
- **Leo Li (G)**
- **Divya Rana (BS '23)**
- **Ryan Rusali (BS '21)**
- **Saptarshi Saha (G)**
- **Shuyuan Wang (MS '21)**
- **Diana Warren (BS '23)**
- **Chris Wu (G)**



**gjwang@cmu.edu**



**@GeraldJWang**

**M<sup>5</sup> LAB**

**Carnegie Mellon University**  
Civil & Environmental Engineering