# Making Supernovae with Jets

## Chelsea Harris Sean Couch, Andrew Christlieb, Luke Roberts









## implementing high-order magnetohydrodynamics to explore jets in stellar explosions





the cool things I'm a part of







## implementing high-order magnetohydrodynamics to explore jets in stellar explosions





the cool things I'm a part of





# **MSU Department of Computational** Mathematics, Science, and Engineering

MSU<br/>MSUCMSE ... will enable application-driven computational modeling ("pull"),<br/>while also exposing disciplinary computational scientists to advanced<br/>tools and techniques ("push"), which will ignite new transformational<br/>connections in research and education.

...scientists who may reside in science, mathematics, engineering or **DOE CSGF** computational scientists develop a sense of commuted with the test of the sense of commuted with the sense of with the sense of commuted with the sense of computational scientists develop a sense of community that's often difficult to find in a single academic department.









# MSU Department of Computational Mathematics, Science, and Engineering







March 16

#### February 21







## Toward Exascale Astrophysics of Mergers and Supernovae





# TEANS



## implementing high-order magnetohydrodynamics to explore jets in stellar explosions





the cool things I'm a part of

making jets in a supernova





# supernovae: stellar explosions



# supernovae: stellar explosions

star ripped apart by shock in <1 second</li>
different explosion mechanisms
bright from radioactivity





# endpoints of stellar evolution

SDO/AIA 335

2011-09-07 22:55:53 UT



## endpoints of stellar evolution

2011-09-07 22:55:53 UT SDO/AIA 335





# endpoints of stellar evolution

## create & disperse heavy elements

SDO/AIA 335 2011-09-07 22:55:53 UT





## energize galaxies





# endpoints of stellar evolution

## create & disperse heavy elements

SDO/AIA 335 2011-09-07 22:55:53 UT



(/







## cosmological tools

## energize galaxies



## site of r-process elements?



# endpoints of stellar evolution

## create & disperse heavy elements





## energize galaxies



## elements heavier than Fe: neutron capture





#### solar system abundances (Asplund 2005)

Cowan+ 2019



## r-process: rapid neutron capture onto nuclei

 some elements/isotopes come only from r-process
 we have tracers!
 requires neutron-rich environment





Cowan+ 2019

# best candidates for r-process sites neutron star mergers supernovae













## Toward Exascale Astrophysics of Mergers and Supernovae





# TEANS





# WURP What's Up with the R-Process?







## core-collapse supernovae create neutron stars







## core-collapse supernovae create neutron stars





## ✓ Seen 1054 AD





## core-collapse supernovae create neutron stars





## ✓ Seen 1054 AD





































PNS

T~C









T~C

**PNS** 

Mösta+ 2017 solar  $10^{0} -$ B13 B12-sym Abundance 10-2 B12  $10^{-6}$ 50 100 150 200 0 mass number A





- seen in nature: long gammaray bursts associated with SNe
- magnetic confinement narrow jet
- stars have magnetic fields!
- need to amplify field over one billion times ... in ~10 ms.



# creating jets in core-collapse SNe

#### 0.00 ms



 $B_{\phi}$ 

#### Mösta+ 2015







- seen in nature: long gammaray bursts associated with SNe
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# creating jets in core-collapse SNe

#### 0.00 ms



 $B_{\phi}$ 

#### Mösta+ 2015





speed increases inward



speed increases inward



Balbus & Hawley (1991)

rotation



Balbus & Hawley (1991)

## magnetic field, B



Balbus & Hawley (1991)

## magnetic field, B



Balbus & Hawley (1991)

## magnetic field, B











**SIDE VIEW** 



weak magnetic field, B



**SIDE VIEW** 



Balbus & Hawley (1991)



weak magnetic field, B

**SIDE VIEW** 



Balbus & Hawley (1991)



weak magnetic field, B

![](_page_41_Figure_1.jpeg)

SIDE VIEW

Balbus & Hawley (1991)

![](_page_41_Figure_4.jpeg)

weak magnetic field, B

![](_page_42_Picture_1.jpeg)

## initial B (purely poloidal)

#### Balbus & Hawley (1991)

## final B (poloidal piece)

![](_page_42_Figure_5.jpeg)

amplification! (lines squeezed)

![](_page_43_Picture_1.jpeg)

## initial B (purely poloidal)

![](_page_43_Picture_3.jpeg)

#### Balbus & Hawley (1991)

## final B (poloidal piece)

![](_page_43_Picture_6.jpeg)

## implementing high-order magnetohydrodynamics to explore jets in stellar explosions

![](_page_44_Picture_1.jpeg)

![](_page_44_Picture_2.jpeg)

the cool things I'm a part of

![](_page_44_Picture_5.jpeg)

![](_page_44_Picture_6.jpeg)

![](_page_44_Picture_7.jpeg)

# resolution issue: modes start small

$$\frac{\partial}{\partial t} \begin{bmatrix} \rho \\ \rho \mathbf{u} \\ \mathcal{E} \\ \mathbf{B} \end{bmatrix} + \nabla \cdot \begin{bmatrix} \rho \mathbf{u} \\ \rho \mathbf{u} + \left(p + \frac{1}{2} \|\mathbf{B}\|^2\right) \|\mathbf{u} - \mathbf{B}\mathbf{B} \\ \mathbf{u} \left(\mathcal{E} + p + \frac{1}{2} \|\mathbf{B}\|^2\right) - \mathbf{B} (\mathbf{u} \cdot \mathbf{B}) \\ \mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{u} \end{bmatrix}$$

 $\nabla \cdot \mathbf{B} = \mathbf{0},$ 

$$p = (\gamma - 1) \left( \mathcal{E} - \frac{1}{2} \| \mathbf{B} \|^2 - \frac{1}{2} \rho \| \mathbf{u} \|^2 \right),$$

![](_page_45_Picture_4.jpeg)

![](_page_45_Picture_5.jpeg)

![](_page_45_Picture_6.jpeg)

# resolution issue: modes start small

$$\frac{\partial}{\partial t} \begin{bmatrix} \rho \\ \rho \mathbf{u} \\ \mathcal{E} \\ \mathbf{B} \end{bmatrix} + \nabla \cdot \begin{bmatrix} \rho \mathbf{u} \\ \rho \mathbf{u} + \left(p + \frac{1}{2} \|\mathbf{B}\|^2\right) \|\mathbf{u} - \mathbf{B}\mathbf{B} \\ \mathbf{u} \left(\mathcal{E} + p + \frac{1}{2} \|\mathbf{B}\|^2\right) - \mathbf{B} (\mathbf{u} \cdot \mathbf{B}) \\ \mathbf{u} \mathbf{B} - \mathbf{B} \mathbf{u} \end{bmatrix}$$

 $\nabla \cdot \mathbf{B} = \mathbf{0},$ 

$$p = (\gamma - 1) \left( \mathcal{E} - \frac{1}{2} \| \mathbf{B} \|^2 - \frac{1}{2} \rho \| \mathbf{u} \|^2 \right),$$

![](_page_46_Picture_4.jpeg)

e.g., Obergaulinger+ 2009

ρ∇Φ pv∙∇Φ

0

0

Ω : rotation profile (3D) N: buoyancy (Brunt-Väisälä frequency) R: differential rotation term

> equatorial:  $C = (N^2 + R)/\Omega^2 < 0$ unstable

scale of fastest growing mode:  $\lambda_{FGM} \sim |\vec{v}_A| [-(N^2 + R)]^{-1/2}$ 

$$\lambda_{\rm FGM} \sim 6.9 \, {\rm km} \left(\frac{b}{10^{15} \, {\rm G}}\right) \left(\frac{\rho}{2.5 \, 10^{13} \, {\rm g \, cm^{-3}}}\right)^{-\frac{1}{2}} \left(\frac{\Omega}{1900 \, {\rm s}^{-1}}\right)^{-\frac{1}{2}}$$

growth time ~10 ms

![](_page_46_Picture_12.jpeg)

# MHD in FLASH with Spark

![](_page_47_Figure_1.jpeg)

#### FLASH - AMReX

![](_page_47_Figure_3.jpeg)

#### WENO reconstruction

![](_page_47_Figure_5.jpeg)

explicit Runge-Kutta

![](_page_47_Picture_7.jpeg)

![](_page_47_Picture_8.jpeg)

![](_page_47_Picture_9.jpeg)

# SparkJoy: high order version of Spark

![](_page_48_Figure_1.jpeg)

resolution (cells per length)

![](_page_48_Picture_3.jpeg)

![](_page_48_Figure_4.jpeg)

![](_page_48_Picture_5.jpeg)

## numerical resistivity creates turbulence

![](_page_49_Figure_1.jpeg)

kilometers from PNS

kilometers from PNS

![](_page_49_Picture_4.jpeg)

#### **Obergaulinger+ 2009**

kilometers from PNS

![](_page_49_Picture_7.jpeg)

## components of SparkJoy Helzel et al. (2013); Buchmuller et al. (2016)

![](_page_50_Picture_1.jpeg)

#### conserved variables

![](_page_50_Picture_3.jpeg)

![](_page_50_Figure_5.jpeg)

![](_page_50_Picture_6.jpeg)

![](_page_50_Picture_7.jpeg)

![](_page_50_Figure_9.jpeg)

explicit Runge-Kutta

![](_page_50_Picture_11.jpeg)

# current status: talk-killer bug

Warning: Unused dummy argument 'xyz' at (1) [-Wunused-dummy-argument] gr\_xyzToBlock.F90:54:0:

#### procID=proc

Warning: 'proc' is used uninitialized in this function [-Wuninitialized]

gr_xy210b100x1190100101		x subintervals	=		
blkID=blk		y subintervals	=		
Warning: 'blk' is used uninitialize /opt/software/OpenMPI/2.1.2-GCC-6. =invalid,zero,overflow -fbounds-ch	ed in this function [-Wuninitialized] 4.0-2.28/bin/mpif90 -ggdb -c -O0 -fdefault-real-8 -fdefault-double-8 -pedantic -Wall -Waliasing -Wsurprising -Wconversion - eck -fimplicit-none -fstack-protector-all -ffree-line-length-none -I /opt/software/HDF5/1.8.20-foss-2018a/include -DH5 USE	Parameters computed :			
1000 -DNXB=20 -DNYB=20 -DNZB=1 -DN	_DIM=2 hy_joy_getFaceFlux.F90				
ny_Joy_getFaceFlux.F90:158:15:		ambient temperature	= 1.202		
<pre>maxBlkSize = MAXVAL(blkPhysSize</pre>	)	ambient int. energy	= 2.500		
Warning: Possible change of value prim2flx.F90:39:15:	in conversion from REAL(8) to INTEGER(4) at (1) [-Wconversion]	gas constant	= 83144		
real :: E,B2,UB,Ptot					
1 Warning: Unused variable 'b2' decl prim2flx.F90:26:6:	1 ning: Unused variable `b2' declared at (1) [-Wunused-variable] m2flx.F90:26:6:		refined: total leaf blocks =		
use Hydro_data, ONLY : hy_C_hyp		Finished with Grid_i	= nitDomain,		
Warning: Unused module variable 'hy_c_hyp' which has been explicitly imported at (1) [-Wunused-variable] prim2flx.F90:39:18:		Ready to call Hydro_i Hydro initialized	nit		
real :: E,B2,UB,Ptot		Gravity initialized			
1 Warning, Unused variable \ub' decl	ء <sup>[</sup> 1	Initial dt verified			
riemann.F90:84:16:	Warning: Unused dummy argument 'xyz' at (1) [-Wunused-dummy-argument] gr xyzToBlock.F90:54:0:	*** Wrote checkpoint *** Wrote plotfile to	file to out output07/i		
real :: Bn_gim, Psi_gim 1		Initial plotfile writ	ten		
Warning: Unused variable `bn_glm'	<pre>c procID=proc</pre>	Driver init all done			
fiemann.F90:78:37:	Manual Annual is used unisitislized in this function [ Maniaitislized]	*** Wrote plotfile to	output07/i		
real :: BxStar,ByStar,BzStar,Bn	gr xyzToBlock F90.55.0.	n t	dt (		
Warning: Unused variable `bn_hll'		1 1.0000E-03 2.	0000E-03 (		
riemann.F90:78:16:	blkID=blk	*** Wrote checkpoint	file to out		
real :: BxStar,ByStar,BzStar,Bn		*** Wrote plotfile to	output07/i		
ا Warning: Unused variable `bxstar'	Warning: 'blk' is used uninitialized in this function [-Wuninitialized]	2 3.0000E-03 4.	0000E-03 (		
riemann.F90:78:23:	/opt/software/openMP1/2.1.2-GCC-6.4.0-2.28/bin/mp1190 -ggdb -C -O0 -fdefault-real-8 -fdefault	*** Wrote checkpoint	file to out		
	1000 -DNXB=20 -DNZB=1 -DN DIM=2 hy joy getFaceFlux.F90	*** Wrote plotfile to	output07/i		
	hy_joy_getFaceFlux.F90:158:15:	3 7.0000E-03 8.	0000E-03 (		
		*** Wrote checkpoint	file to out		
	<pre>maxBlkSize = MAXVAL(blkPhysSize)</pre>	*** Wrote plotfile to	output07/i		
	L Warning: Possible change of value in conversion from REAL(8) to INTEGER(4) at (1) [-Woonversi	4 1.5000E-02 1.	5248E-02 (		
	prim2flx.F90:39:15:	*** Wrote checkpoint	file to out		
		*** Wrote plotfile to	output07/i		
	real :: E,B2,UB,Ptot	5 3.0248E-02 1.	3382E-02 (		
		*** Wrote checkpoint	file to out		
	Warning: Unused variable 'b2' declared at (1) [-Wunused-variable]	*** Wrote plotfile to	output07/1		
		6 4.3630E-02 1.	3250E-02 (		
	use Hydro_data, ONLY : hy_C_hyp	*** Wrote checkpoint	rile to out		
	1	756990 $-021$	2612E - 02		
	Warning: Unused module variable 'hy_c_hyp' which has been explicitly imported at (1) [-Wunuse prim2flx.F90:39:18:	*** Wrote checkpoint	file to out		
	real :: E,B2,UB,Ptot	Program received signa	1 SIGFPE, A		
	Warning: Unused variable 'ub' declared at (1) [-Wunused-variable]	0x000000000064f/f/ in	reconstruct		
	riemann.F90:84:16:	Missing separate debug	= coerr2p(1 infos, use:		
	real :: Bn glm, Psi glm	-41mlnx1-OFED.4.5.0.1.	0.45101.x86		
		4.6.45101.x86_64 libto	ol-ltdl-2.4		
	Warning: Unused variable 'bn_glm' declared at (1) [-Wunused-variable] riemann.F90:78:37:				
	real :: BxStar,ByStar,BzStar,Bn_hll,pStar,qStar				
	Warning: Unused variable 'bn_hll' declared at (1) [-Wunused-variable] riemann.F90:78:16:				

real :: BxStar,ByStar,BzStar,Bn\_hll,pStar,qStar

Warning: Unused variable 'bxstar' declared at (1) [-Wunused-variable] riemann.F90:78:23:

#### 1 1

221209764060E-008 0000000000004 225.000000000

0 0 49 49 no restart

out07/isenvor\_07\_hdf5\_chk\_0000 \*\*\*\* senvor\_07\_hdf5\_plt\_cnt\_0000 \*\*\*\*

envor\_07\_hdf5\_plt\_cnt\_0001 \*\*\*\* х, у, z) | dt\_hydro 5.036E+00, 4.607E+00, 0.000E+00) | 1.664E-02 ut07/isenvor 07 hdf5 chk 0001 \*\*\*\* envor 07 hdf5 plt cnt 0002 \*\*\*\* 5.036E+00, 4.607E+00, 0.000E+00) | 1.664E-02 out07/isenvor 07 hdf5 chk 0002 \*\*\*\* envor 07 hdf5 plt cnt 0003 \*\*\*\* 5.321E+00, 4.821E+00, 0.000E+00) | 1.663E-02 ut07/isenvor 07 hdf5 chk 0003 \*\*\*\* envor 07 hdf5 plt cnt 0004 \*\*\*\* 4.893E+00, 4.607E+00, 0.000E+00) | 1.525E-02 out07/isenvor 07 hdf5 chk 0004 \*\*\*\* envor 07 hdf5 plt cnt 0005 \*\*\*\* 5.536E+00, 4.893E+00, 0.000E+00) | 1.338E-02 out07/isenvor 07 hdf5 chk 0005 \*\*\*\* envor 07 hdf5 plt cnt 0006 \*\*\*\* 4.893E+00, 4.679E+00, 0.000E+00) | 1.325E-02 ut07/isenvor 07 hdf5 chk 0006 \*\*\*\* envor 07 hdf5 plt cnt 0007 \*\*\*\* 5.393E+00, 4.679E+00, 0.000E+00) | 1.261E-02 ut07/isenvor\_07 hdf5 chk 0007 \*\*\*\*

rithmetic exception.

(uplus=..., uminus=..., data1d=..., flat=1, size1d=40, ind=31, dx=0.071428571428571425) at reconstruct.F90:88

\*(1.+(abs(betaWeno(:,1)-betaWeno(:,3))/(betaWeno(:,1)+epsilon))\*\*2)

debuginfo-install glibc-2.17-260.el7\_6.3.x86\_64 hwloc-libs-1.11.2-2.el7.x86\_64 libibumad-43.1.1.MLNX20180612.87b4d9b-0.1.45101.x86\_64 libibverbs 64 libmlx4-41mlnx1-OFED.4.5.0.0.3.45101.x86\_64 libmlx5-41mlnx1-OFED.4.5.0.3.8.45101.x86\_64 libnl3-3.2.28-4.el7.x86\_64 librxe-41mlnx1-OFED.4.4.2. 2-22.el7\_3.x86\_64 numactl-libs-2.0.9-7.el7.x86\_64 opensm-libs-5.3.0.MLNX20181108.33944a2-0.1.45101.x86\_64

![](_page_51_Picture_16.jpeg)

	Warning: Unused dummy argument 'xy gr_xyzToBlock.F90:54:0:	z' at (1) [-Wunused-dummy-argument]				
	procID=proc					
	Warning: 'proc' is used uninitiali gr_xyzToBlock.F90:55:0:	zed in this function [-Wuninitialized]	x subir	ntervals	=	
	blkID=blk		y subir	ntervals	=	
	Warning: 'blk' is used uninitializ /opt/software/OpenMPI/2.1.2-GCC-6.	ed in this function [-Wuninitialized] 4.0-2.28/bin/mpif90 -ggdb -c -O0 -fdefault-real-8 -fdefault-double-8 -pedantic -Wall -Waliasing -Wsurprising -Wconversion - eck -fimilicit-rone -fetack-protector-all -ffree-line-length-rone -T (opt/software/HDF5/1 8 20-foes-2018a/include -DH5 USE	Paramet	ers compu	ted :	
	1000 -DNXB=20 -DNYB=20 -DNZB=1 -DN hy_joy_getFaceFlux.F90:158:15:		ambient	t temperat	ure =	1.2027
	maxBlkSize = MAXVAL(blkPhysSize		ambient gas con	: int. ene nstant	rgy = =	2.5000 831447
	Warning: Possible change of value prim2flx.F90:39:15:	in conversion from REAL(8) to INTEGER(4) at (1) [-Wconversion]	<b>)</b>			
	real :: E,B2,UB,Ptot 1 Warning: Unused variable \b2/ deal	ared at (1) [-Wunused-wariable]	iterat	ion, no.	not moved	=
	prim2flx.F90:26:6:	ared at (1) [-wullused-variable]	refined refined	i: total l d: total b	eaf blocks locks =	5 =
	use Hydro_data, ONLY : hy_C_hym 1 Warning: Unused module variable 'Y	v c hvp' which has been explicitly imported at (1) [-Wunused-variable]	Finish Ready t	ned with G	rid_initDo	omain, n
	prim2flx.F90:39:18:		Hydro i	initialize	d acd	
	real :: E,B2,UB,Ptot	r <b>1</b>	Initial	dt verif	ied	
	Warning: Unused variable 'ub' decl riemann.F90:84:16:	دا Warning: Unused dummy argument <b>`xyz'</b> at (1) [-Wunused-dummy-argument]	*** Wro	ote checkp	oint file	to outp
	real :: Bn_glm, Psi_glm	gr_xyzToBlock.F90:54:0:	*** W	to platfi	10 +0 00+0	
	1 Warning: Unused variable `bn_glm' riemann F90:78:37:	procID=proc	Initia Drive:			
	real :: BxStar,ByStar,BzStar,Br	Warning: 'proc' is used uninitialized in this function [-Wuninitialized]	*** W:			
	Warning: Unused variable 'bn_hll'	gr_xyzioBlock.F90:55:0:				
	riemann.F90:/8:10:	blkID=blk	*** W:			
	1 Warning: Unused variable 'bxstar' riemann.F90:78:23:	Warning: 'blk' is used uninitialized in this function [-Wuninitialized] /opt/software/OpenMPI/2.1.2-GCC-6.4.0-2.28/bin/mpif90 -ggdb -c -00 -fdefault-real-8 -fdefault =invalid,zero,overflow -fbounds-check -fimplicit-none -fstack-protector-all -ffree-line-lengt 1000 -DNVP-20 -DNVP-20 -DNVP-1 -DN DIM-2 by joy getEaceFlux E90	*** ₩: *** ₩:		_	
		hy_joy_getFaceFlux.F90:158:15:				
		maxBlkSize = MAXVAL(blkPhysSize)	*** W: *** W:			FV
		1 Warning: Possible change of value in conversion from REAL(8) to INTEGER(4) at (1) [-Wconversi	*** W			
		prim2flx.F90:39:15:	*** W:			
		real :: E,B2,UB,Ptot 1	*** W:	_		are
		Warning: Unused variable 'b2' declared at (1) [-Wunused-variable] prim2flx.F90:26:6:	*** W:		Cr	
		use Hydro_data, ONLY : hy_C_hyp	*** W: *** W:	_	-	
		1 Warning: Unused module variable 'hy_c_hyp' which has been explicitly imported at (1) [-Wunuse prim2flx.F90:39:18:	*** W:			
		real :: E,B2,UB,Ptot	Progra			<b>n</b> r
		Warning: Unused variable 'ub' declared at (1) [-Wunused-variable] riemann.F90:84:16:	0x0000 88 Missin			
		real :: Bn_glm, Psi_glm	-41mln:			
		Warning: Unused variable 'bn_glm' declared at (1) [-Wunused-variable] riemann.F90:78:37:			to	rr
		real :: BxStar,ByStar,BzStar,Bn_hll,pStar,qStar				
		Warning: Unused variable 'bn_hll' declared at (1) [-Wunused-variable] riemann.F90:78:16:				
		real :: BxStar,ByStar,BzStar,Bn_hll,pStar,qStar				
Γ		Warning: Unused variable 'bxstar' declared at (1) [-Wunused-variable] riemann.F90:78:23:				

# print \*, SELF

restart

07/isenvor\_07\_hdf5\_chk\_0000 \*\*\*\*

## longed stress

aluation of human interactions

icism over validation

rk/self blur (i.e. <u>creative</u>)

rible for mental health

ibibverbs ED.4.4.2.

![](_page_52_Picture_13.jpeg)

## implementing high-order magnetohydrodynamics to explore jets in stellar explosions

![](_page_53_Picture_1.jpeg)

![](_page_53_Picture_2.jpeg)

the cool things I'm a part of

![](_page_53_Picture_5.jpeg)

![](_page_53_Picture_6.jpeg)

![](_page_53_Picture_7.jpeg)