

# Toward one-dimensional turbulence subgrid closure for large-eddy simulation

Randy McDermott, Rod Schmidt,  
Alan Kerstein, Phil Smith

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Sandia National Laboratories  
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# The C-SAFE ASCI problem

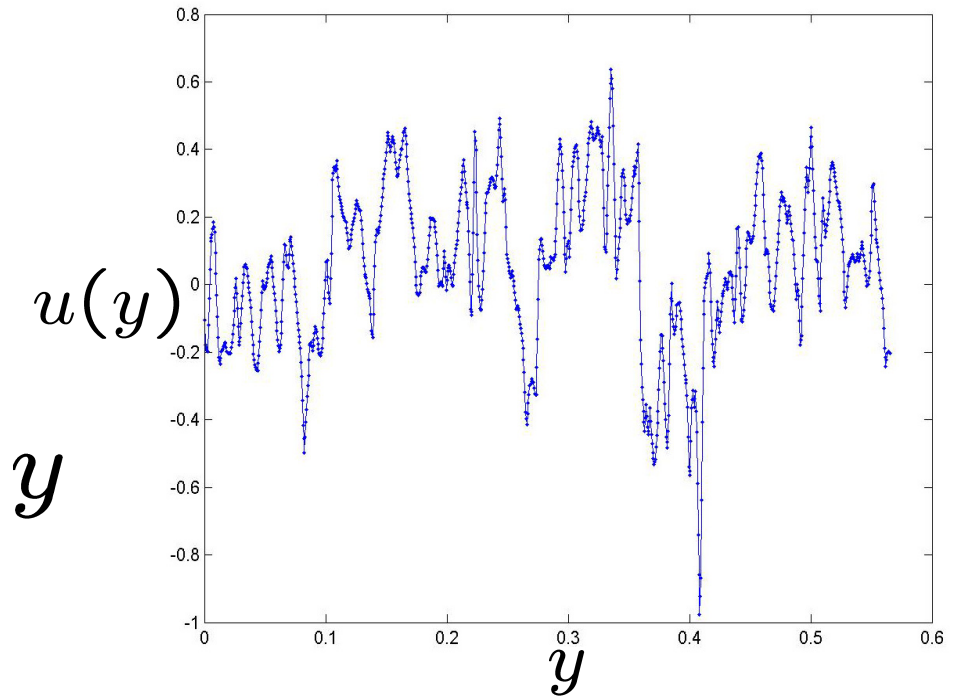
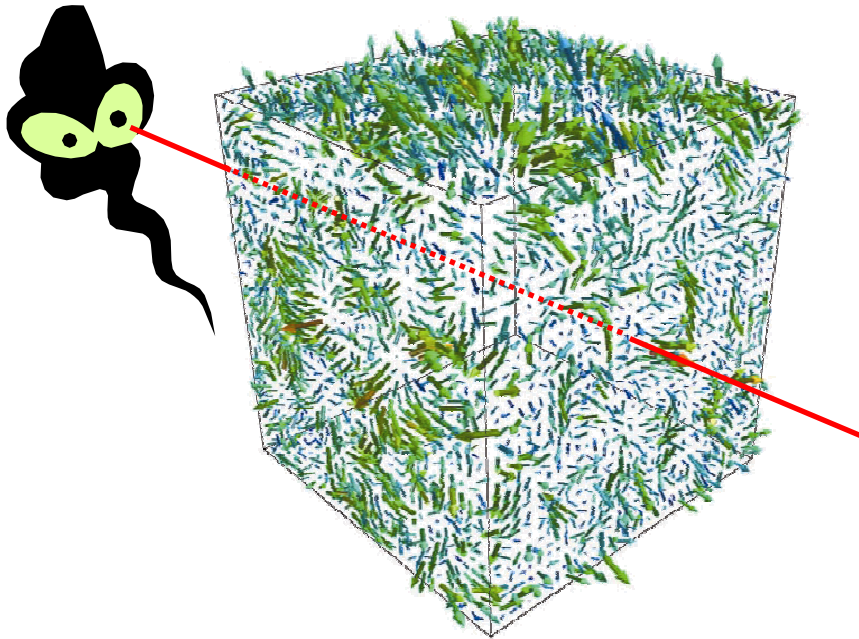


- multi-material
- radiation
- soot
- chemistry
- subgrid heterogeneity
- turbulence
  - subgrid energy production
  - subgrid stresses
  - intermittency
  - backscatter
  - anisotropy

Status: a cylinder in a fire

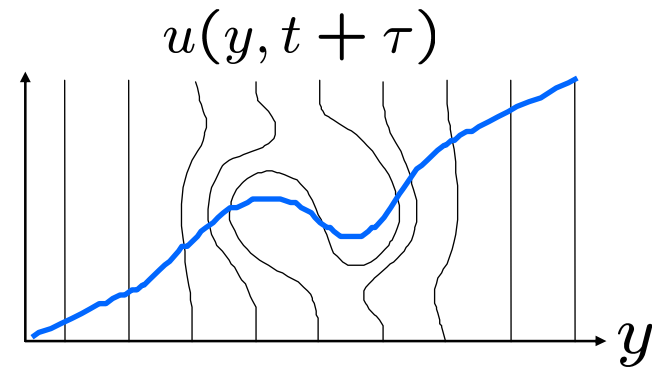
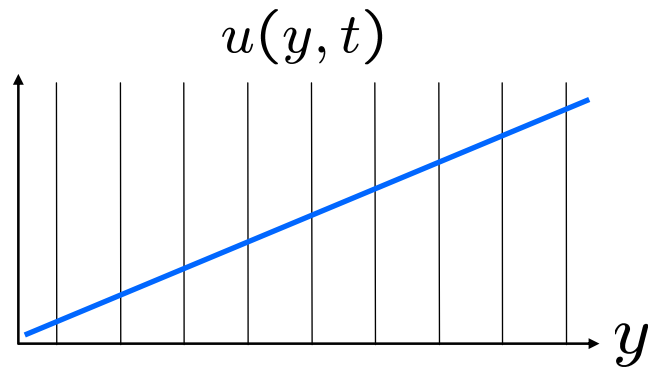


# One-dimensional turbulence

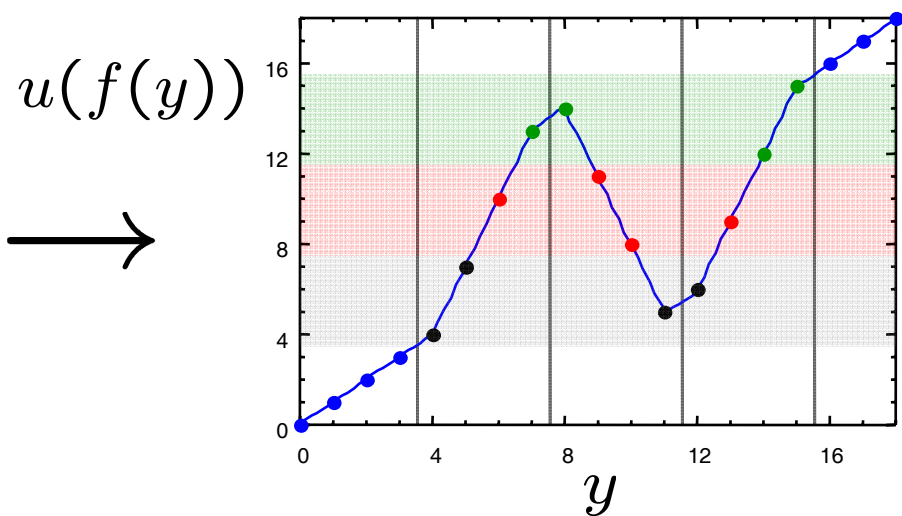
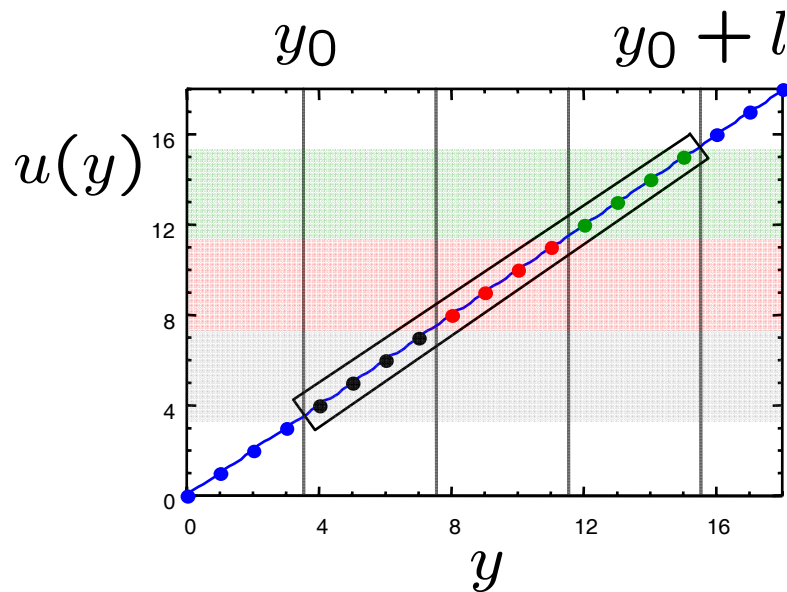


$$\frac{\partial u_i}{\partial t} = \nu \frac{\partial^2 u_i}{\partial y \partial y} + \text{eddy events}$$

# The triplet map



$$u(y) \rightarrow u(f(y)) \quad f(y) = y_0 + \begin{cases} 3(y - y_0) & \text{for } y_0 \leq y \leq y_0 + \frac{1}{3}l \\ 2l - 3(y - y_0) & \text{for } y_0 + \frac{1}{3}l \leq y \leq y_0 + \frac{2}{3}l \\ 3(y - y_0) - 2l & \text{for } y_0 + \frac{2}{3}l \leq y \leq y_0 + l \\ y - y_0 & \text{otherwise} \end{cases}$$



# Eddy sampling: where, when, how big?

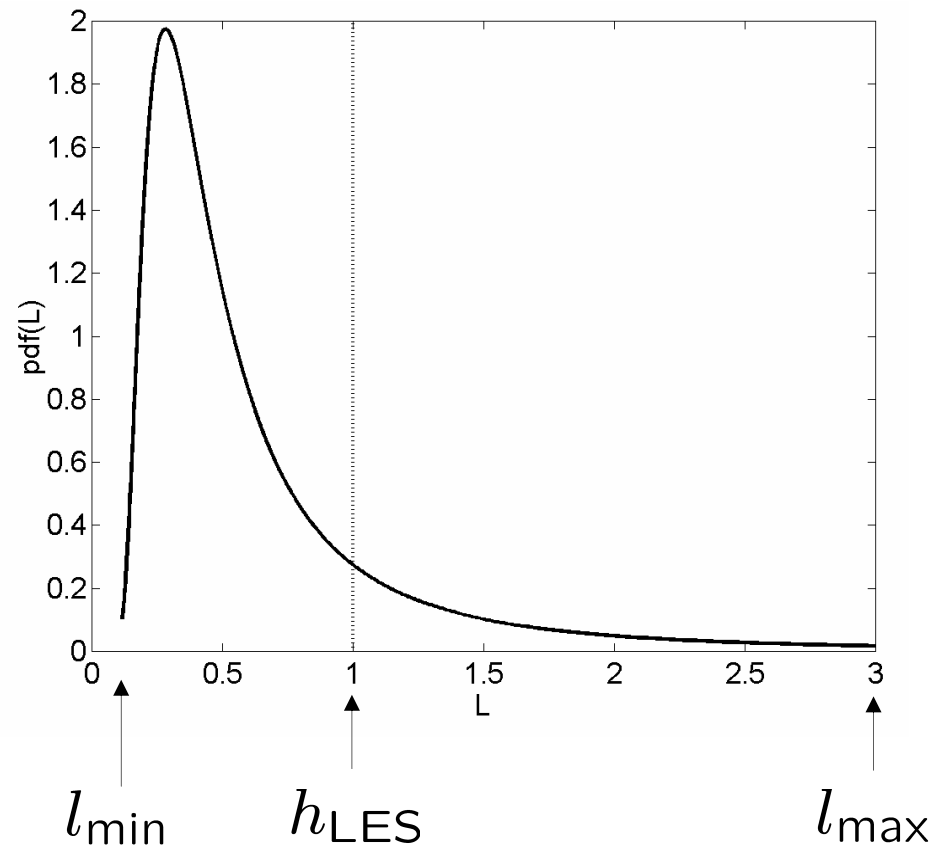
$$\lambda(t; y_0, l) \equiv \frac{1}{l^2 \tau(t; y_0, l)} [=] \frac{\text{events/time}}{\text{position} \times \text{length}}$$

eddy energetics

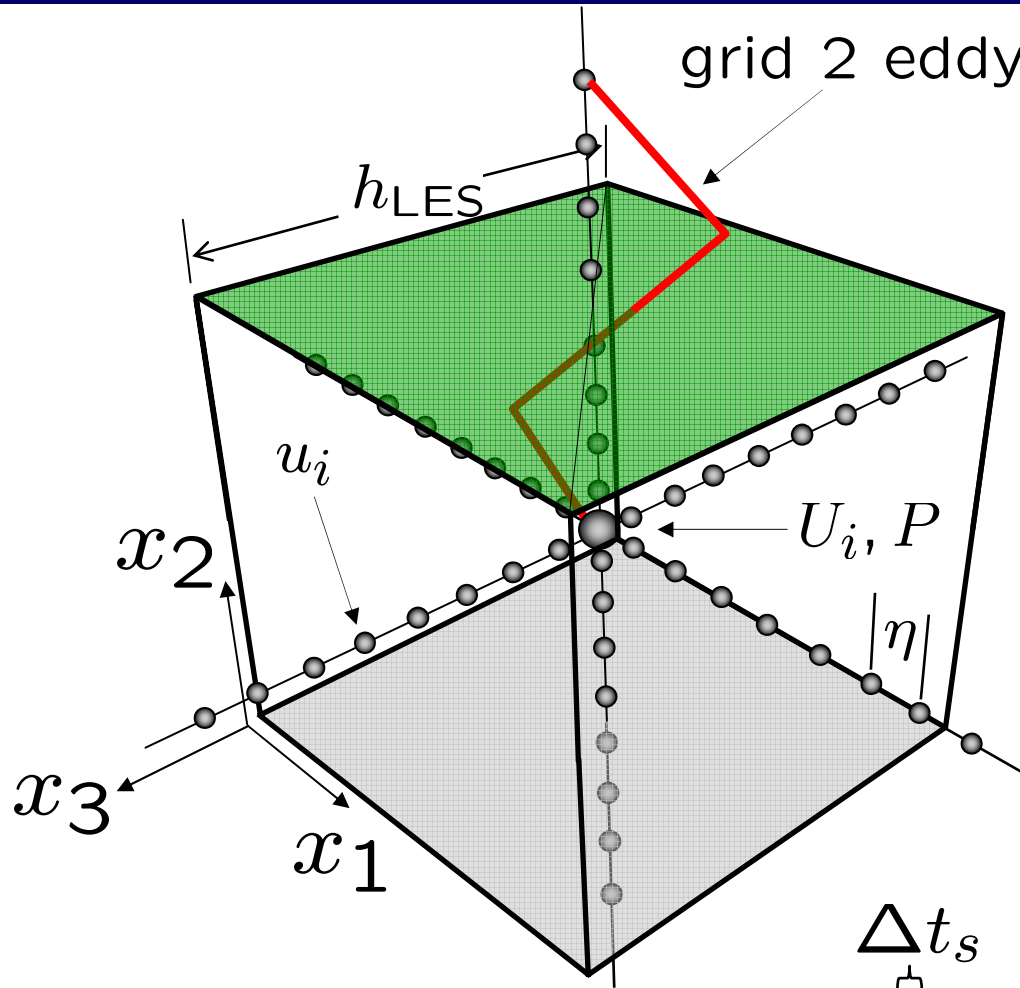
$$\frac{1}{2} m u^2 \sim \frac{1}{2} m \left( \frac{l}{\tau} \right)^2$$

model parameters

$$\frac{1}{\tau} = C \frac{\nu}{l^2} \sqrt{\text{Re}_l^2 - Z^2}$$



# LESODT



Algorithm:

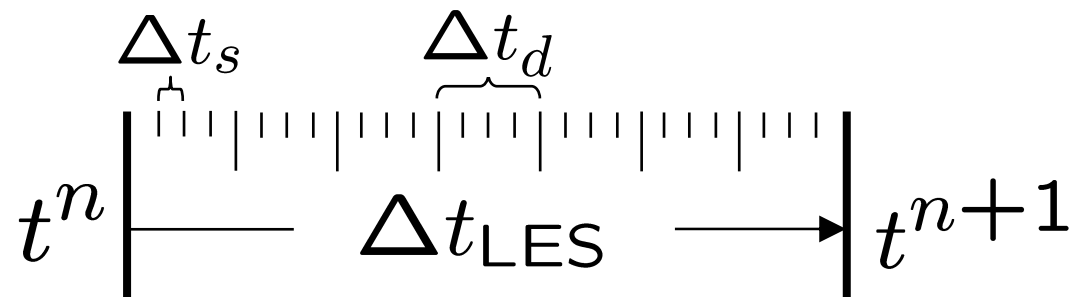
1.  $\bar{u}_i^n = U_i^n$

2. Obtain  $F_i^{\text{ODT}}$

3.  $\frac{dU_i}{dt} = F_i^{\text{NS}} + F_i^{\text{ODT}}$

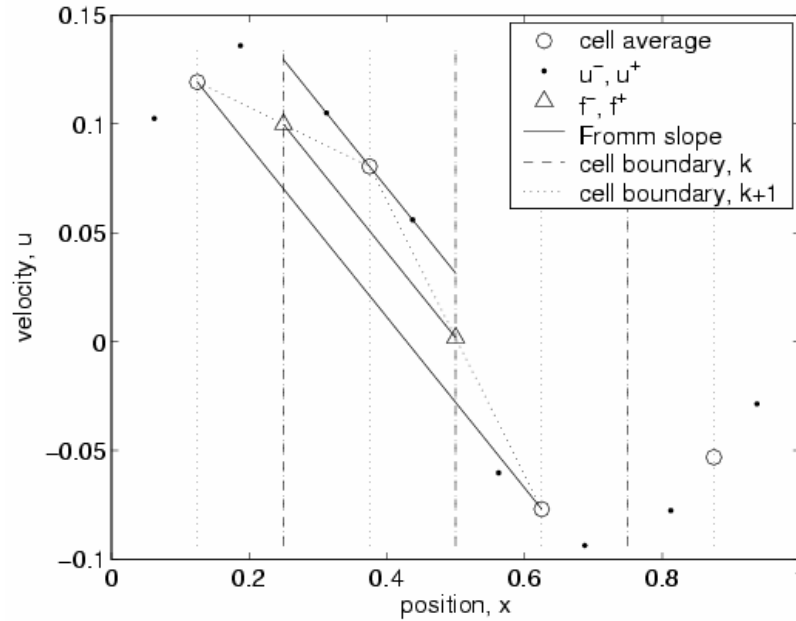
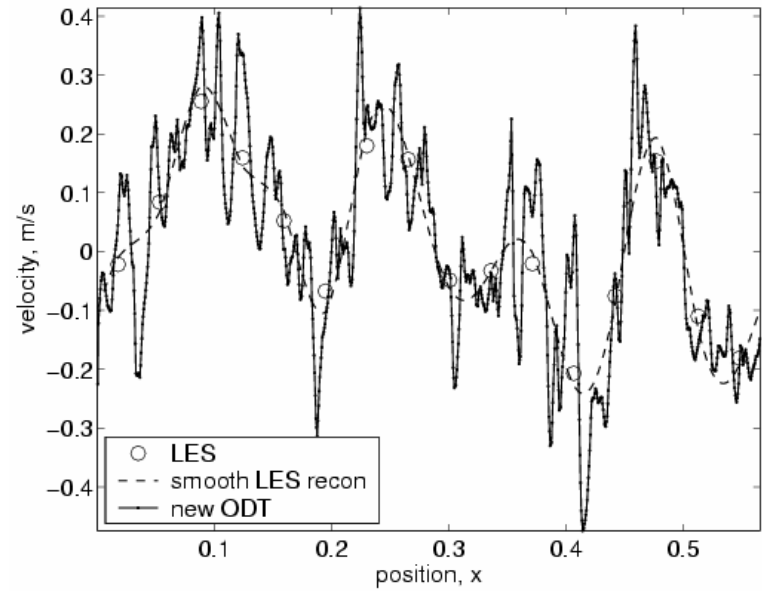
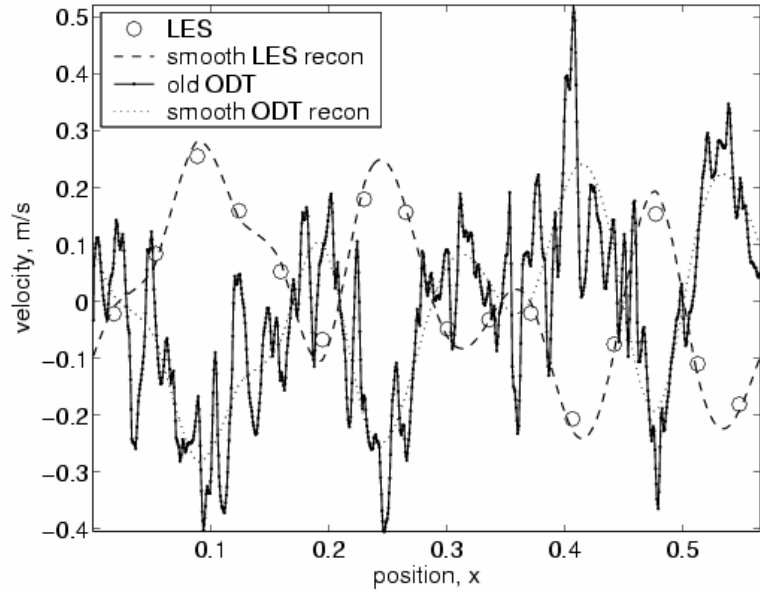
4. Reconstruct

$$\bar{u}_i^{n+1} \neq U_i^{n+1} \rightarrow \bar{u}_i^{n+1} = U_i^{n+1}$$

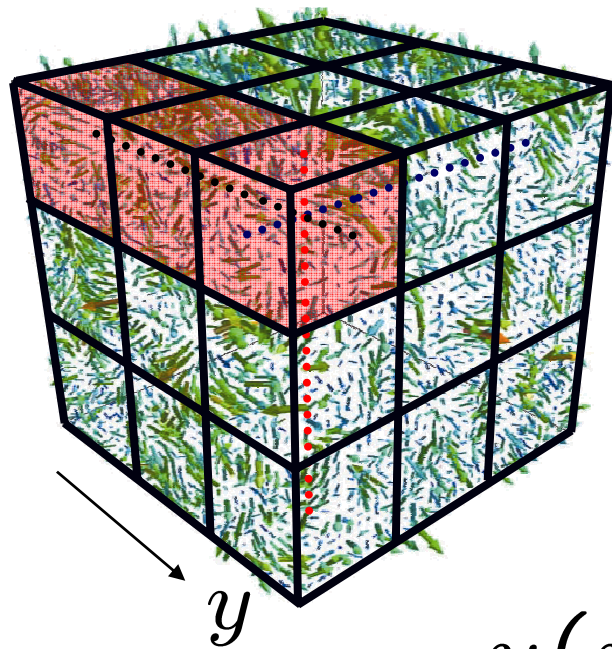




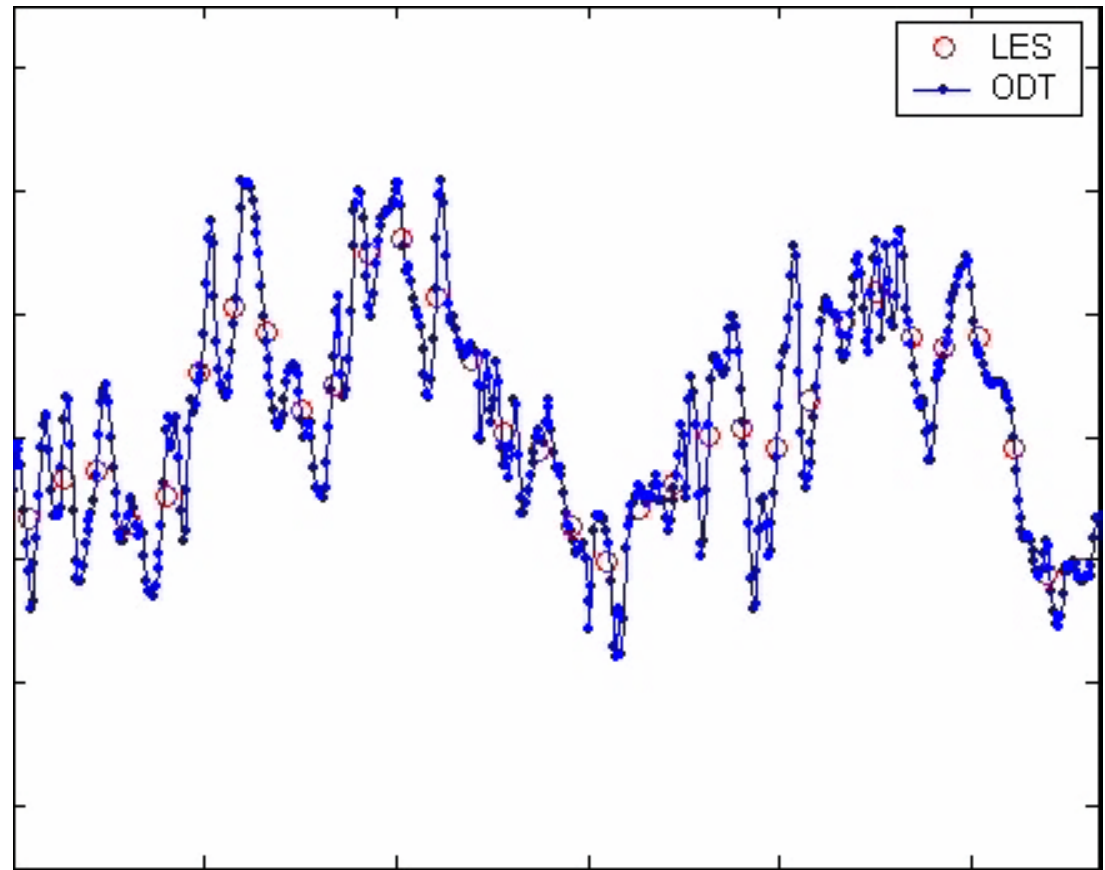
# Reconstruction



# $32^3$ LES / 512 ODT



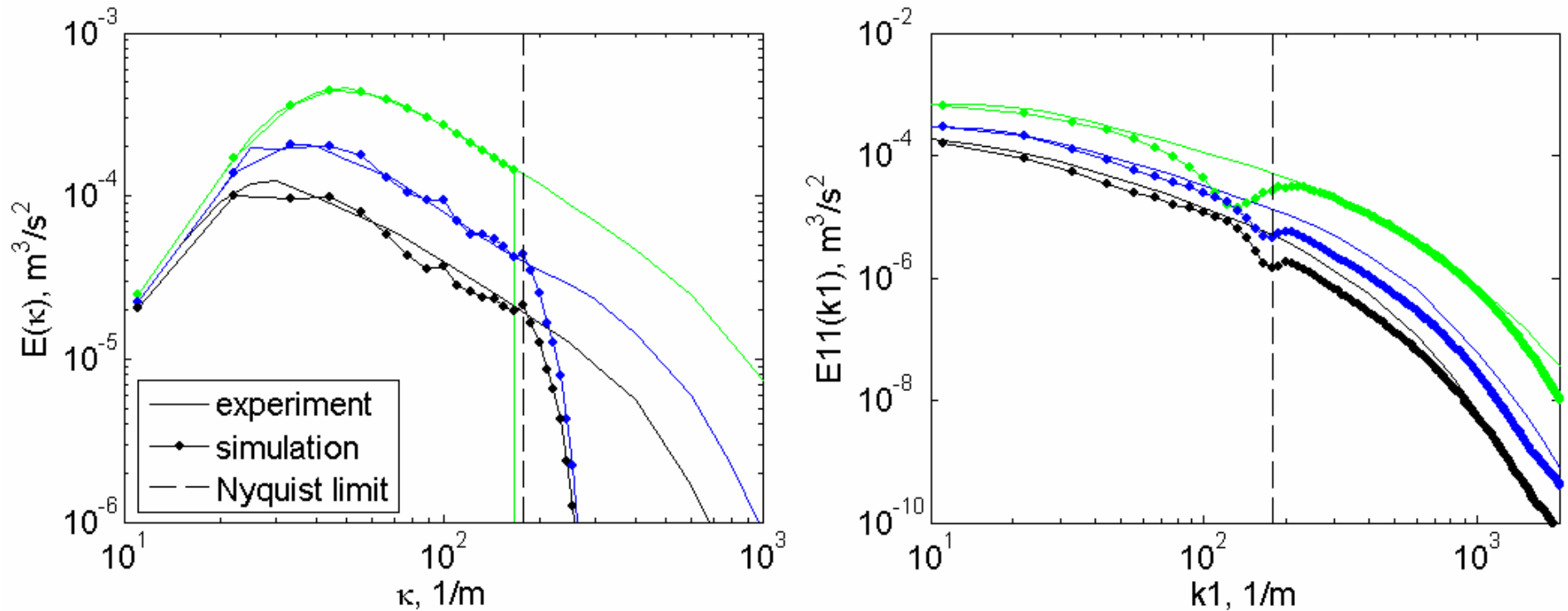
$u(y)$



$y$

# Spectral results

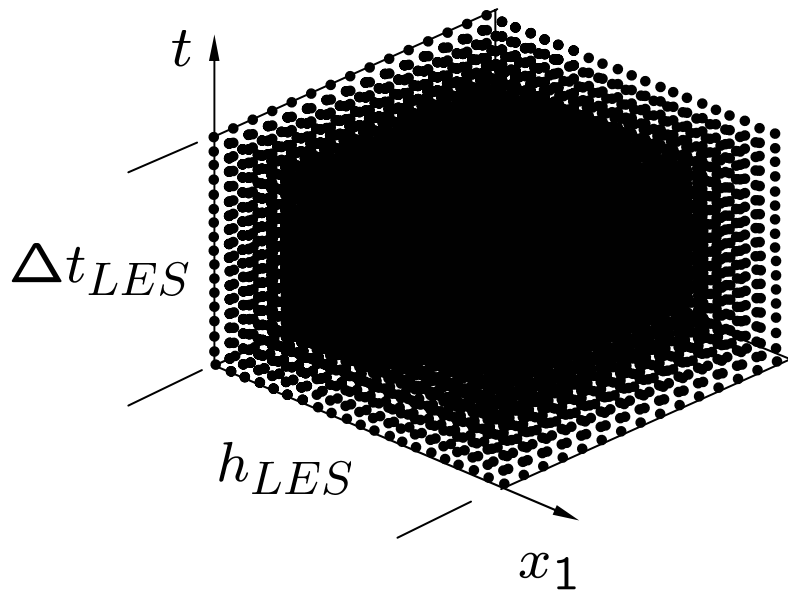
Comte-Bellot and Corrsin (1971)



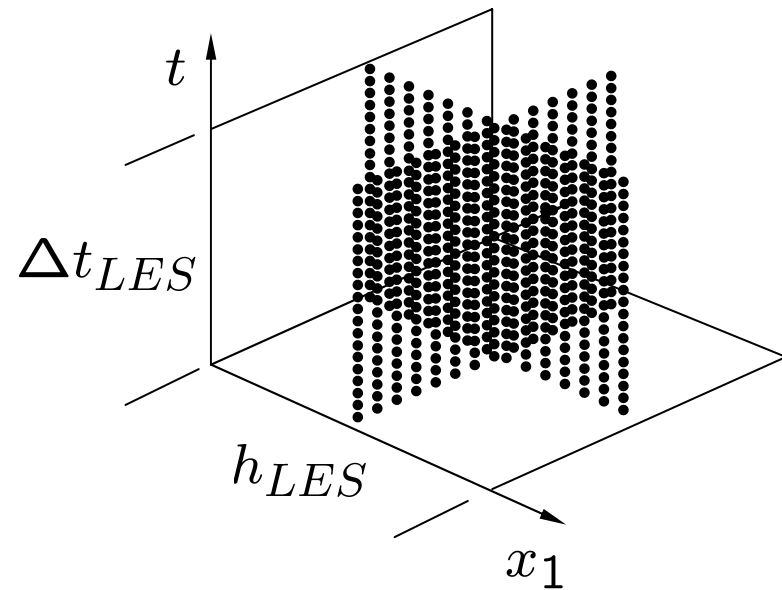
$$E_{11}(\kappa_1) = \int_{\kappa_1}^{\infty} \frac{E(\kappa)}{\kappa} \left(1 - \frac{\kappa_1^2}{\kappa^2}\right) d\kappa$$

# Computational work

DNS



LESODT

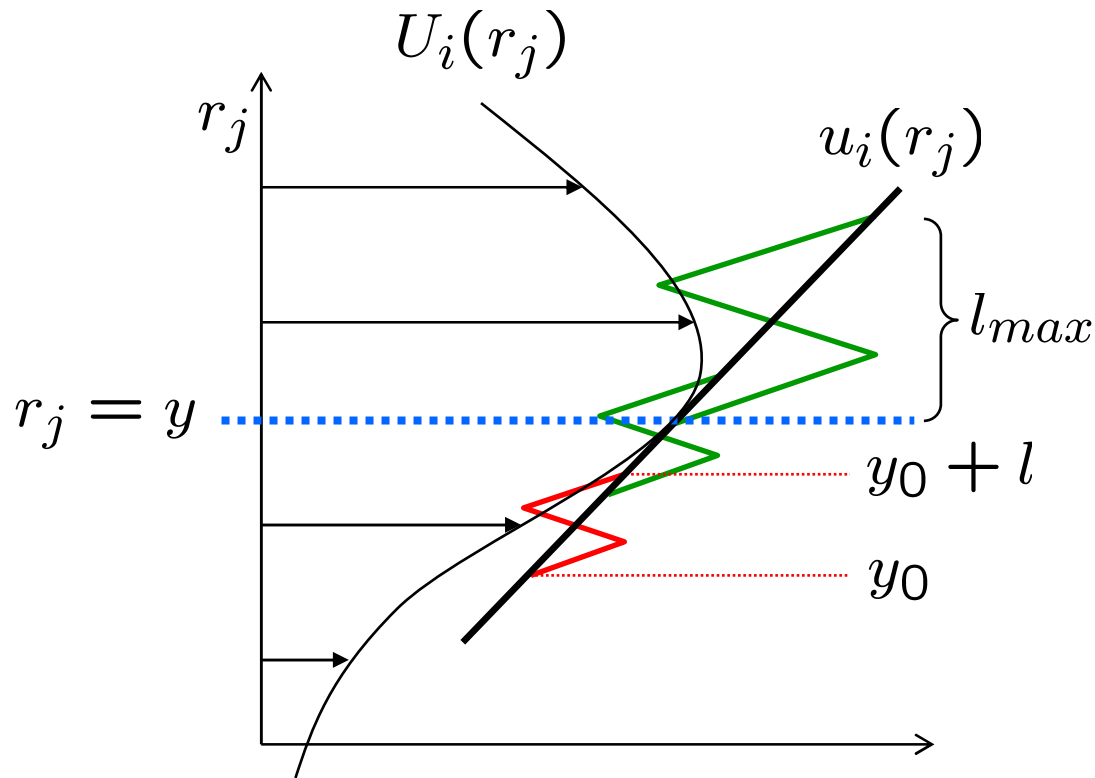


3D space:

$$\sim \left( \text{Re}^{\frac{3}{4}} \right)^4 = \text{Re}^3$$

$$\sim 3 \left( \text{Re}^{\frac{3}{4}} \right)^2 = 3 \text{Re}^{3/2}$$

# Ensemble mean closure



$$y_0 \leq y \leq y_0 + l$$

$$S_{ij}(y) \equiv \partial_r U_i|_{r_j=y}$$

$$\tau_{ij}^{sgs}(y) = -\frac{1}{27} (l_{max}^2 - l_{min}^2) |S(y)| S_{ij}(y)$$

# Closing remarks

- Parallel results in progress
- LESODT tool kit  
(<http://www.inscc.utah.edu/~randy>)

# Questions?

“Physicists come and go, and the problem of turbulence remains.”

~ A. Liebchaber (1988)