

Transitional Flow in a Stenosed Carotid Artery

CSGF Final Presentation

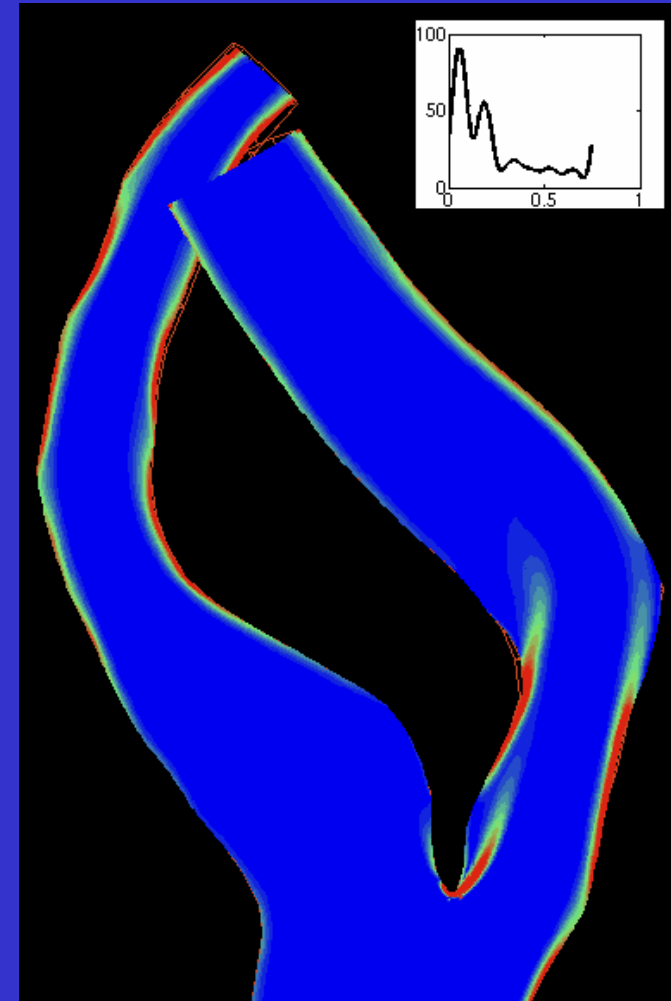
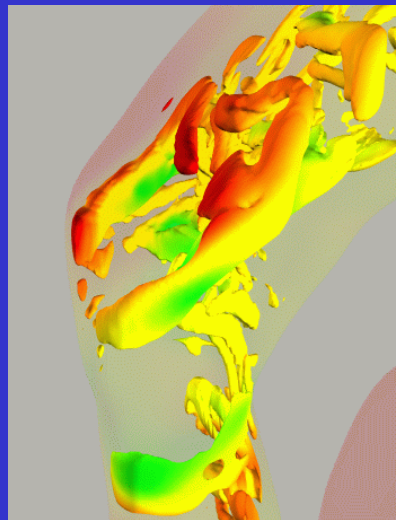
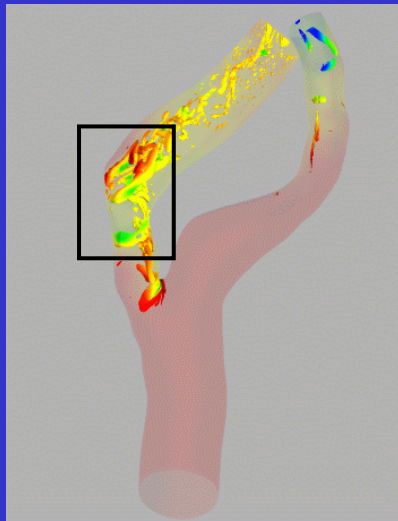
Date: 6/21/2005

Seung E. Lee, MIT

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Paul F. Fischer, Argonne National Lab

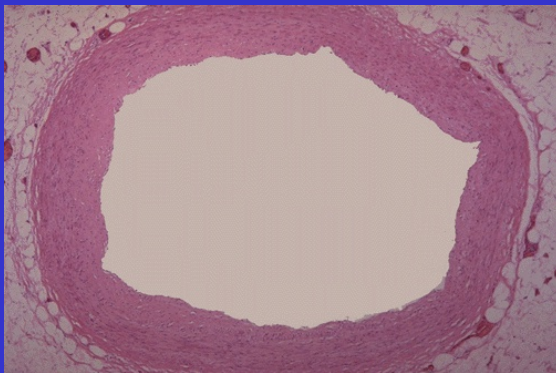


Outline

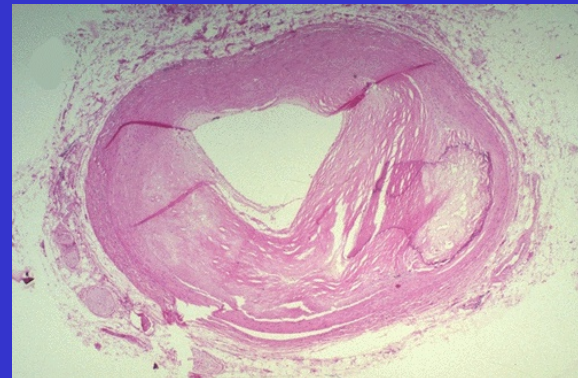
- **Introduction**
 - **Background**
 - **Motivation**
- **Hexahedral Mesh generation**
 - Simple O-grid mesh
 - High quality hexahedral mesh
- **Pulsatile simulation in stenosed carotid**
 - Introduction
 - Method
 - Result
- **Validation**
- **Conclusion**

Introduction

- Fluid mechanics of blood is shown to be important in arterial disease localization and progression [Giddens *et al.* 1993]
- Wall shear stress (WSS) - Localization of atherosclerosis [Ku *et al.* 1985, Zarins *et al.* 1987]
- Flow oscillation, arterial wall vibration, and etc. [Glagov *et al.* 1988]
- We are especially interested in bifurcation geometries



Normal



Severe stenosis

- Many studies were done in normal (healthy) arterial bifurcations using both experimental and numerical simulations [Ku *et al.* 1987, Steinman *et al.* 1996]
- Diseased vessel may introduce disturbed (transitional) flow
- Disturbed (transitional) flow within vasculature may introduce additional health risks [Golledge *et al.* 2000]
 - Heart attack
 - Stroke
- Due to expensive computational cost of transitional flow, not many diseased bifurcations were studied
 - Idealized stenosed geometry [Long *et al.* 2001]
 - Severely stenosed on 2D projection [Stroud *et al.* 2002]

Objective

- Develop a methodology to translate a set of *in vivo* medical images to numerical solution of a full 3D pulsatile transitional flow

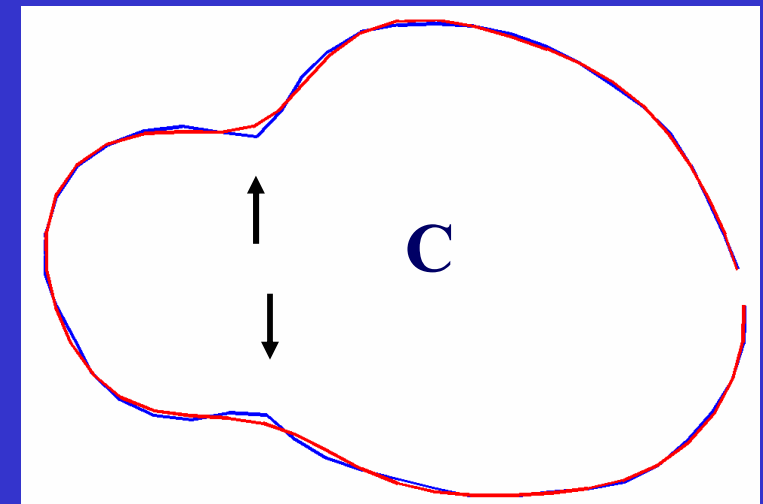
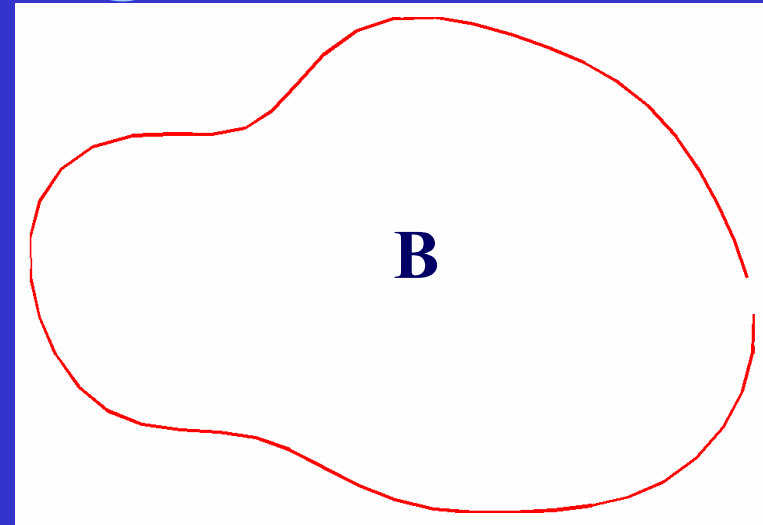
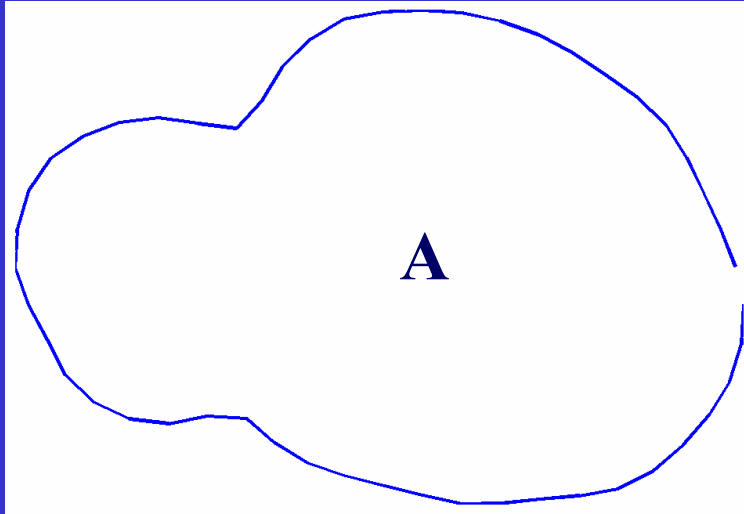
Numerical Method

- **Spectral element method, "Nekton"** [Patera 84, Maday & Patera 89]
 - High-order spectral elements ($N \sim 5-15$)
 - 3rd-order accurate in time
- **Minimal numerical dissipation/dispersion**
- **Direct Numerical Simulation**
 - no turbulence modeling
 - does not require a separate model for different flow problems (carotid stenosis, coronary stenosis)
- **Only takes quad- (2D) or hex- (3D) based meshes**

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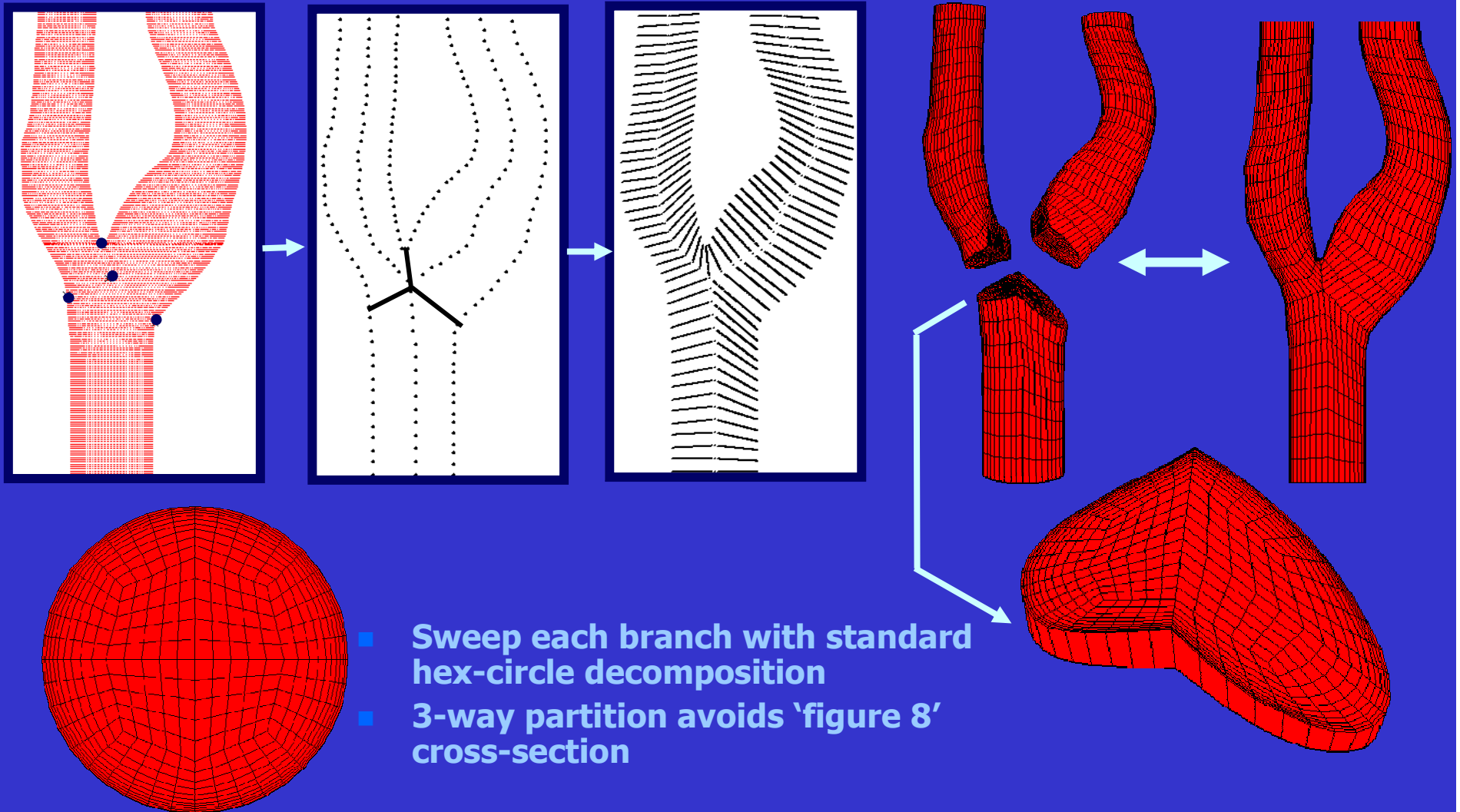
Fourier-based non-shrinking smoothing



- A) A cross-section from medical image
- B) Nonshrinking Smoothing
- C) Comparison
- Developed by Fischer

O-Grid Meshing Scheme

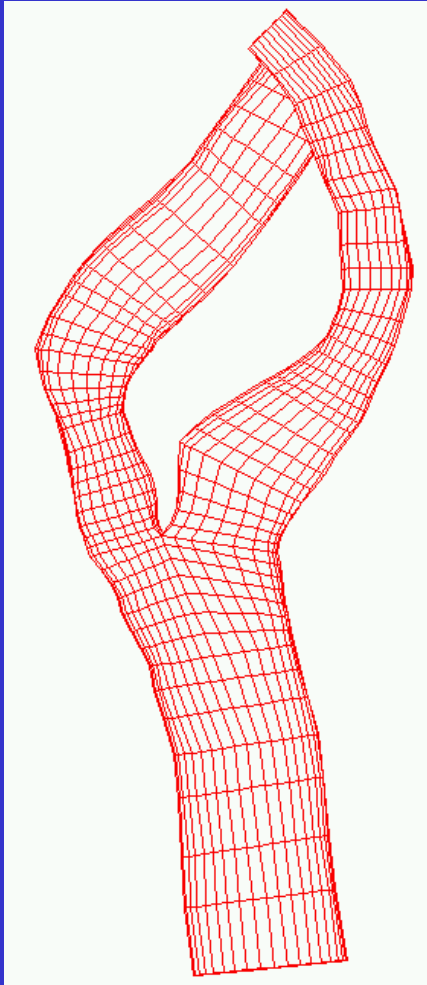
Partition bifurcation into 3 branches via user defined dividing sections



Mesh Generation Challenges

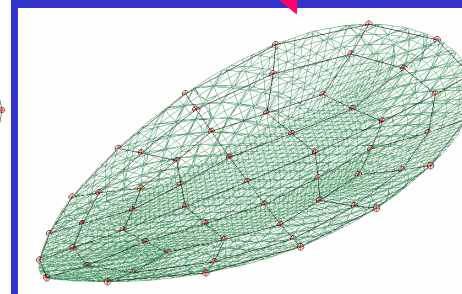
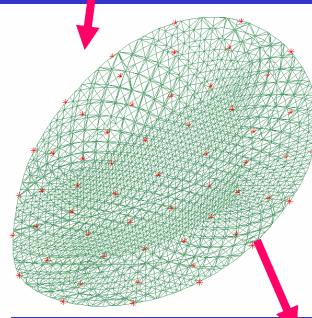
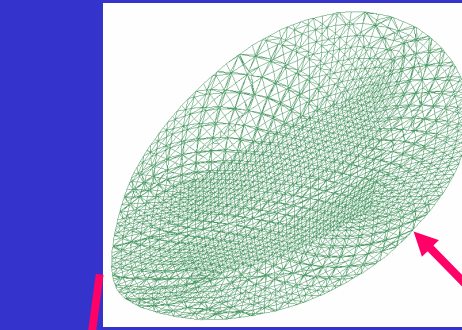
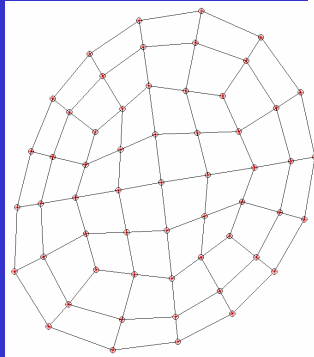
- **Need a mesh with a low number of elements**
- **Interior mesh geometry**
 - Interior element distribution can have a *huge* impact on matrix conditioning and iteration counts [Fischer *et al.* 2002]
- **Accurate surface representation & smoothing**
 - Wall shear stress is very sensitive to surface details

Meshing Based On Conduction Heat Solution

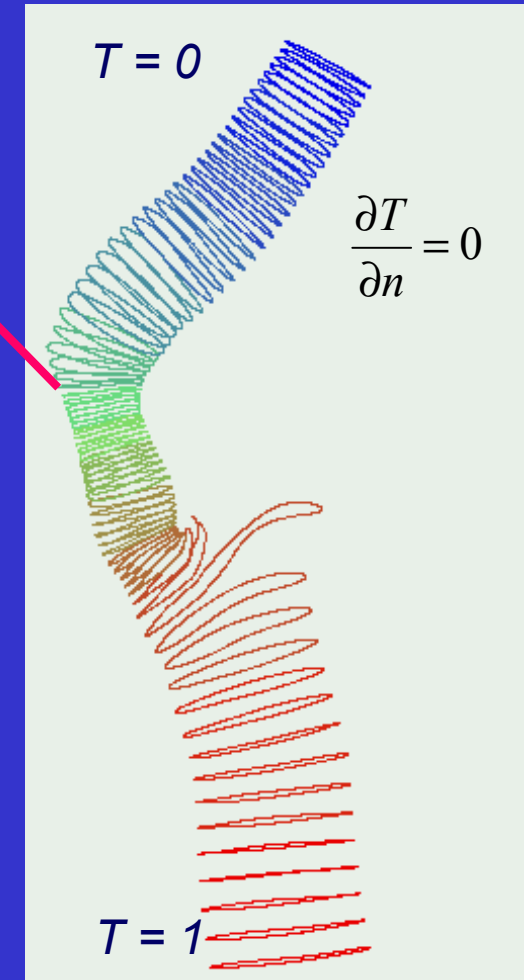


1) Preliminary mesh from commercial meshing software (ICEM-CFD)

Top View

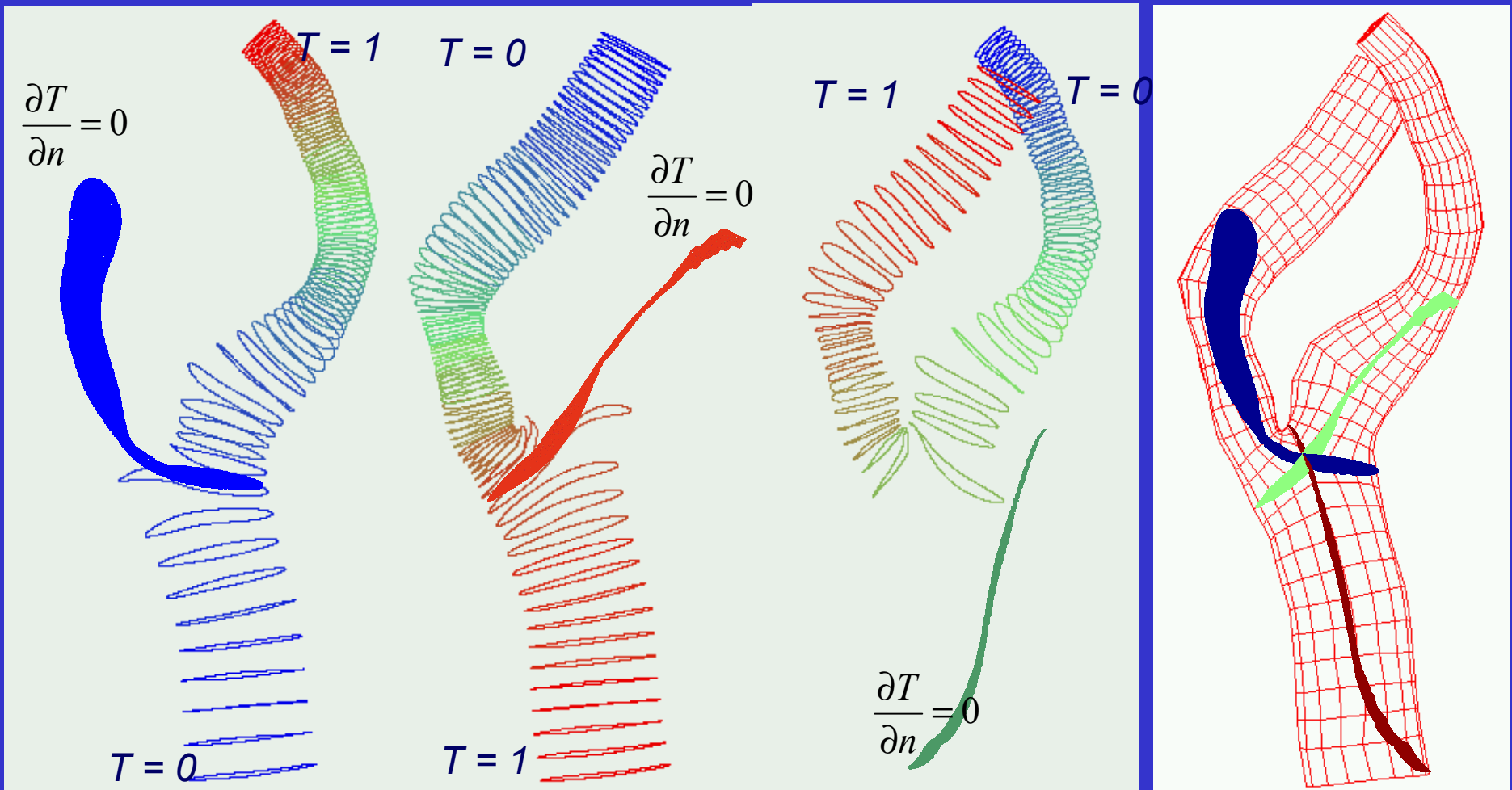


3) Define new meshing sections on the isosurface



2) Solve conduction heat transfer problem

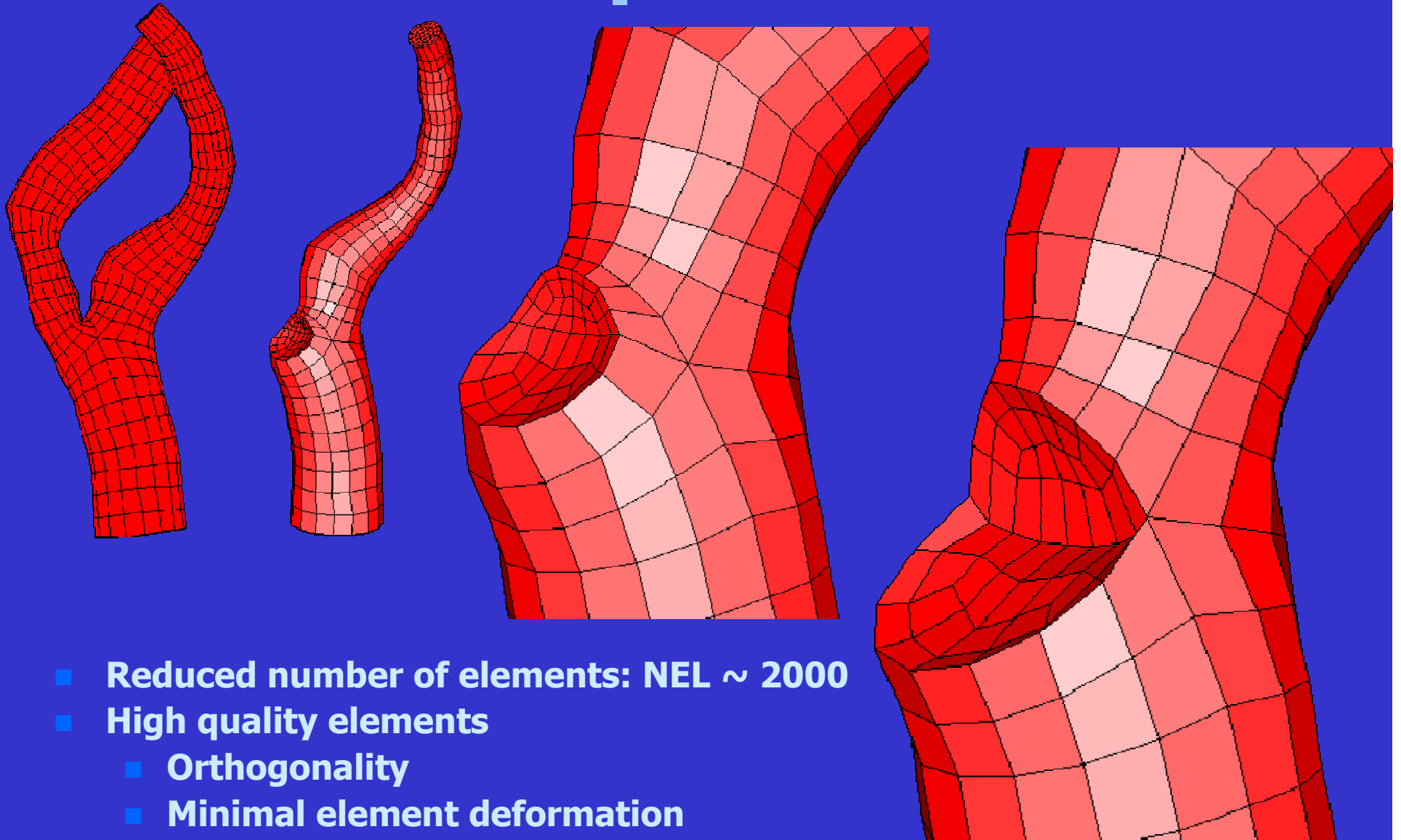
Meshing Stenosed Carotid



Three heat conduction solutions
Find the “principal” isosurfaces –
isosurface through the insulated branch

Automatically determine
Cutting surfaces

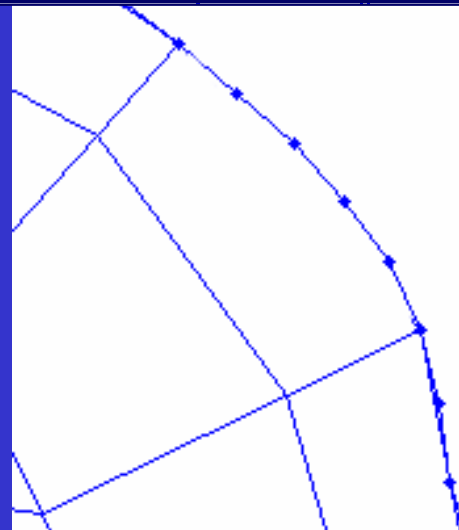
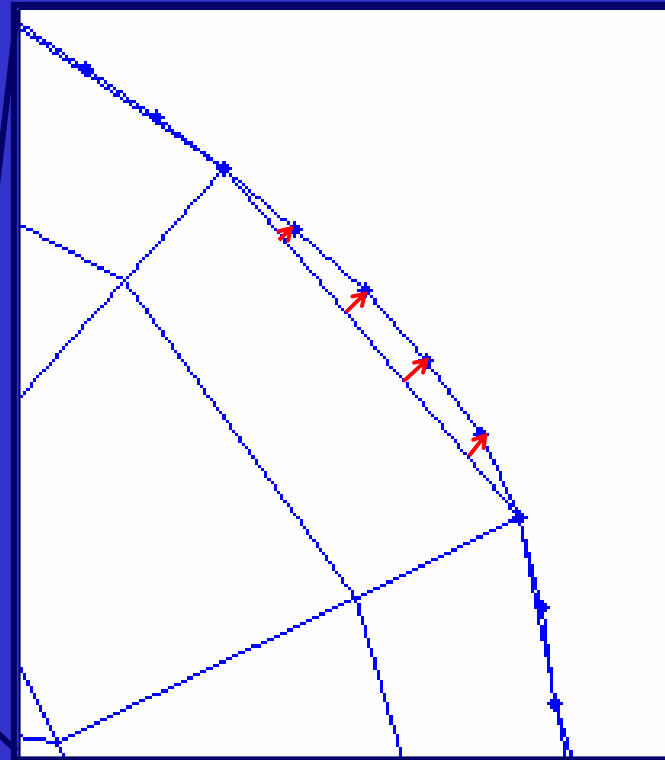
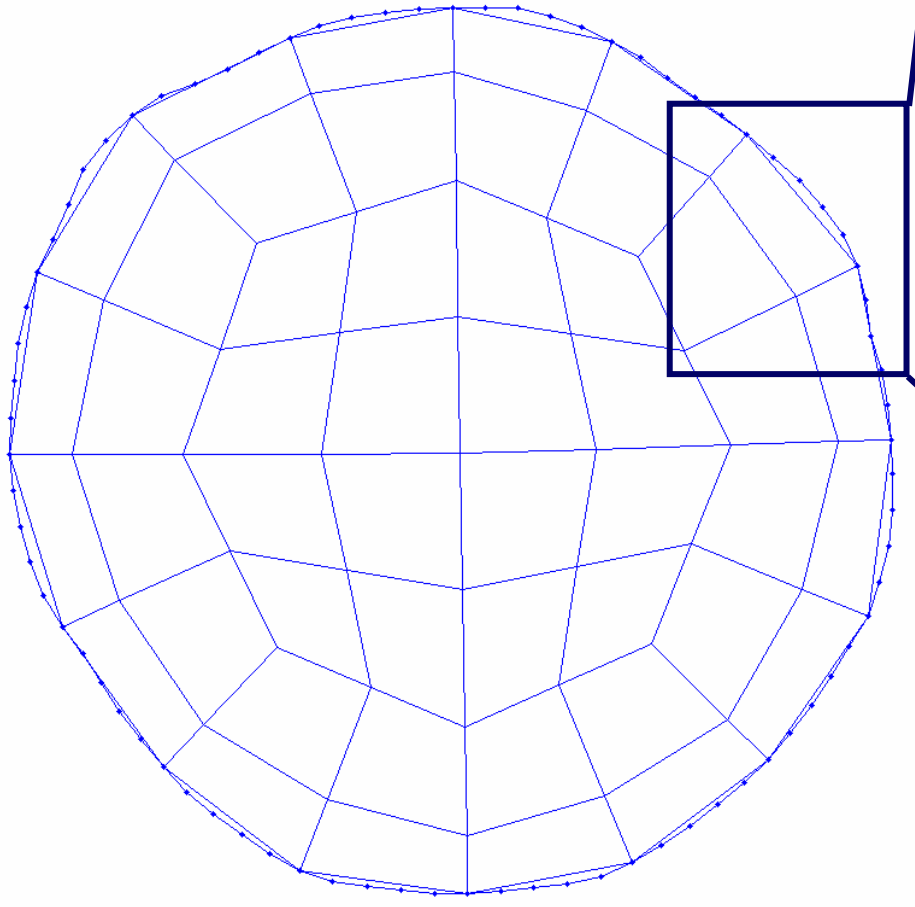
Mesh improvements



- **Reduced number of elements: NEL \sim 2000**
- **High quality elements**
 - **Orthogonality**
 - **Minimal element deformation**

How can we get away with such a crude mesh??

- SEM can incorporate curved facets (smooth lumen surface)

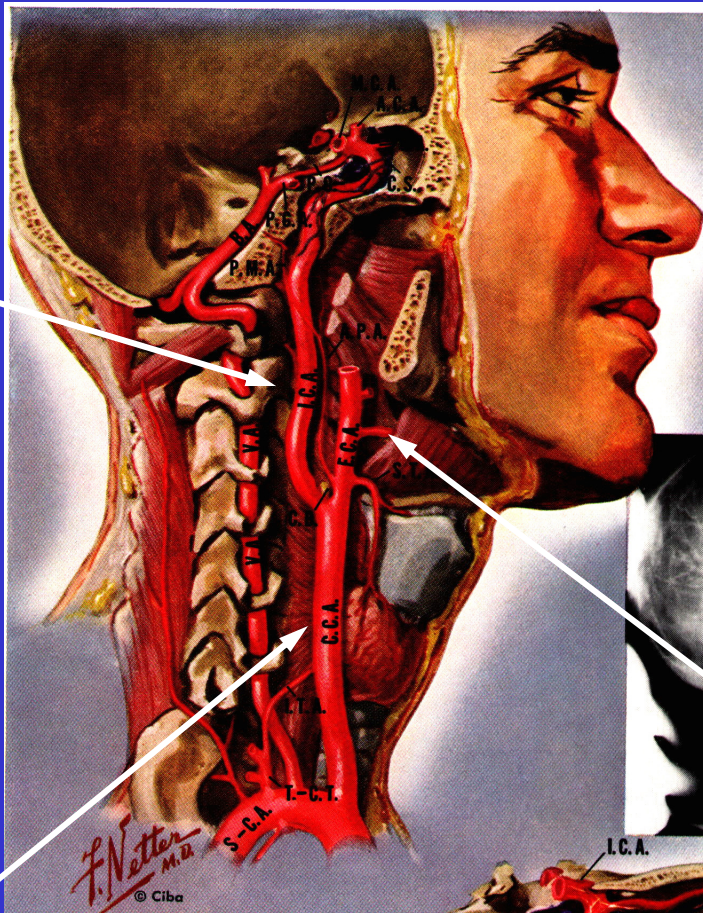


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The Carotid Artery Bifurcation

**Internal
Carotid**

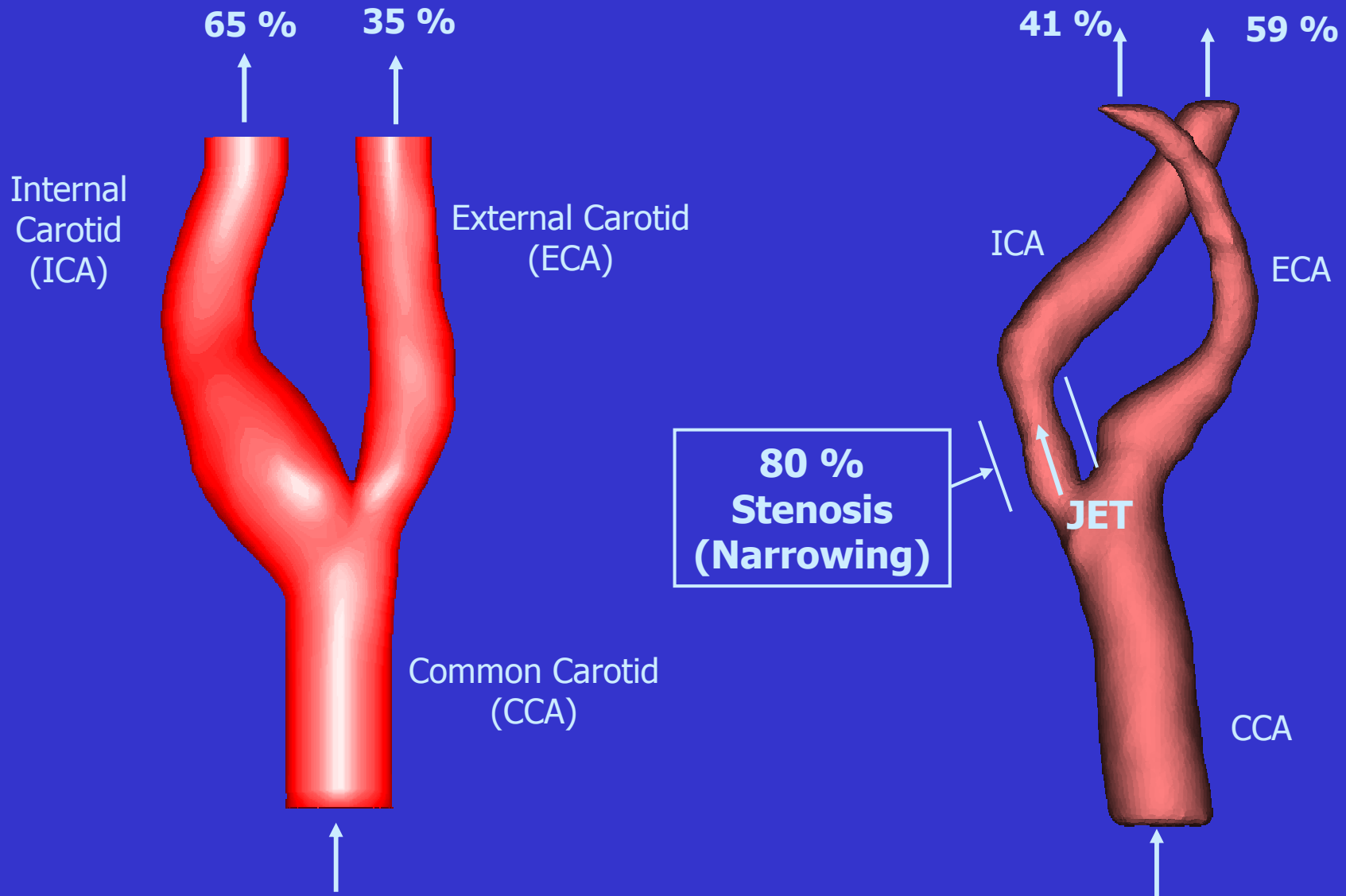


**Common
Carotid**

- Common Carotid Artery (CCA)
- Internal Carotid Artery (ICA) - Supplies blood to the brain
- External Carotid Artery (ECA) - Supplies blood to the face

**External
Carotid**

Healthy and severely stenosed carotid bifurcations

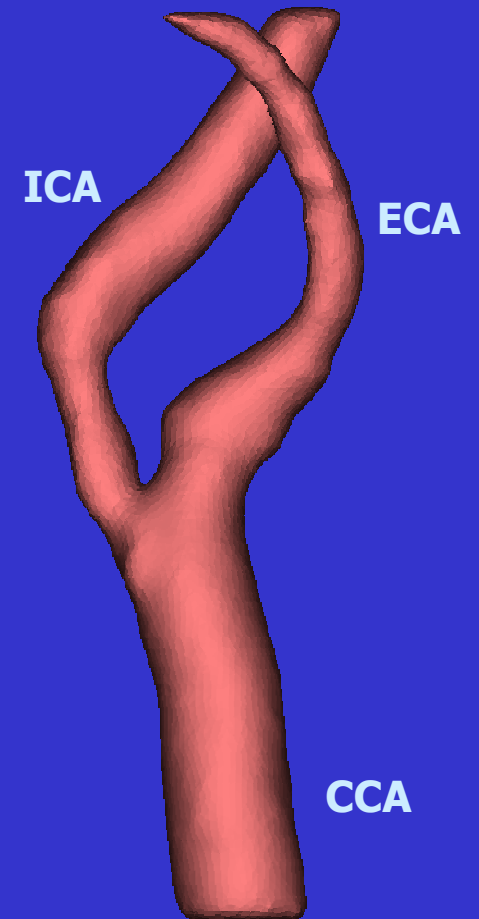
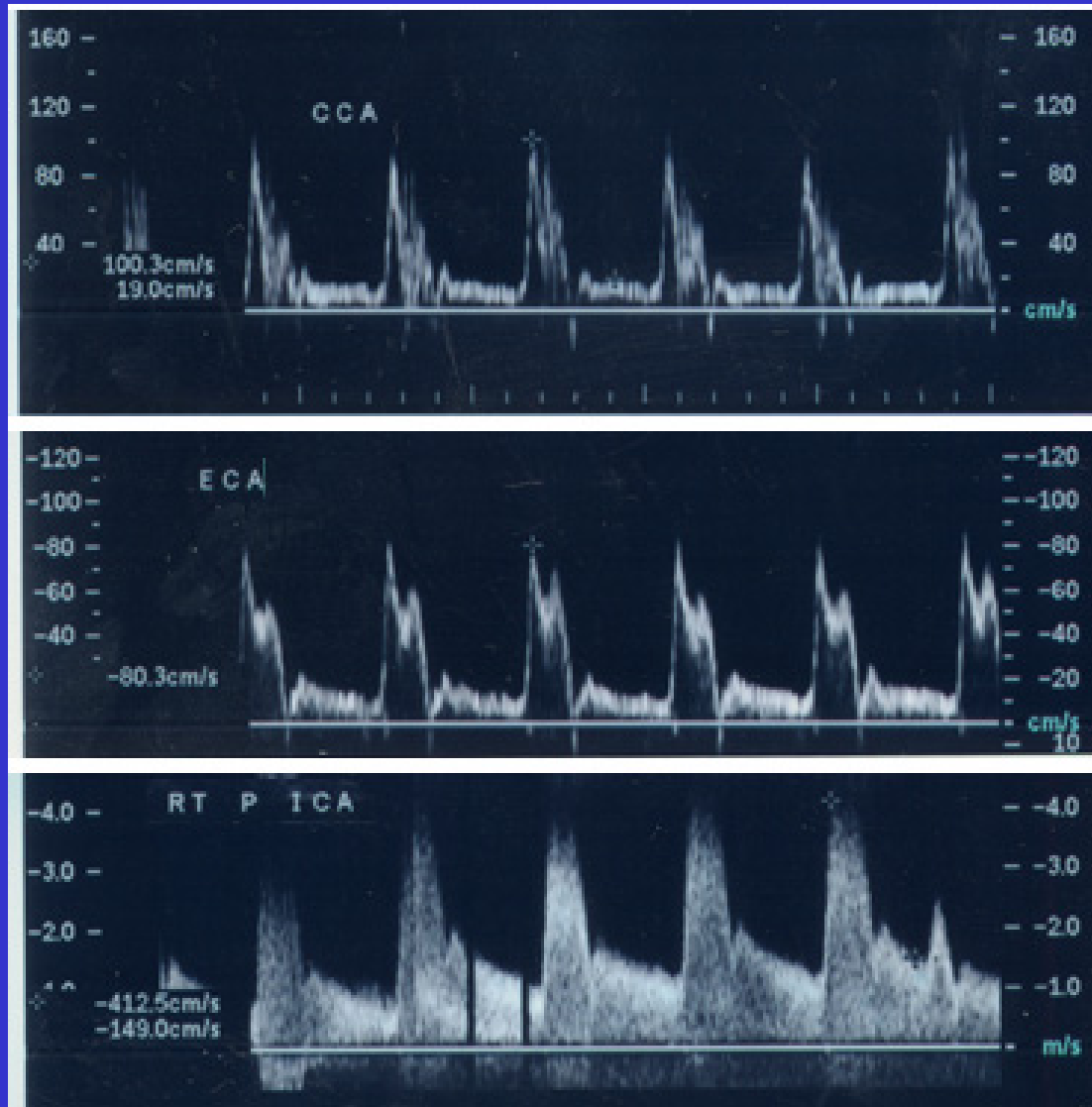


Healthy Carotid Bifurcation

Stenosed Carotid Bifurcation

Healthy carotid simulation done by Piersol, N. 2001 MS Thesis

Ultrasound velocity data



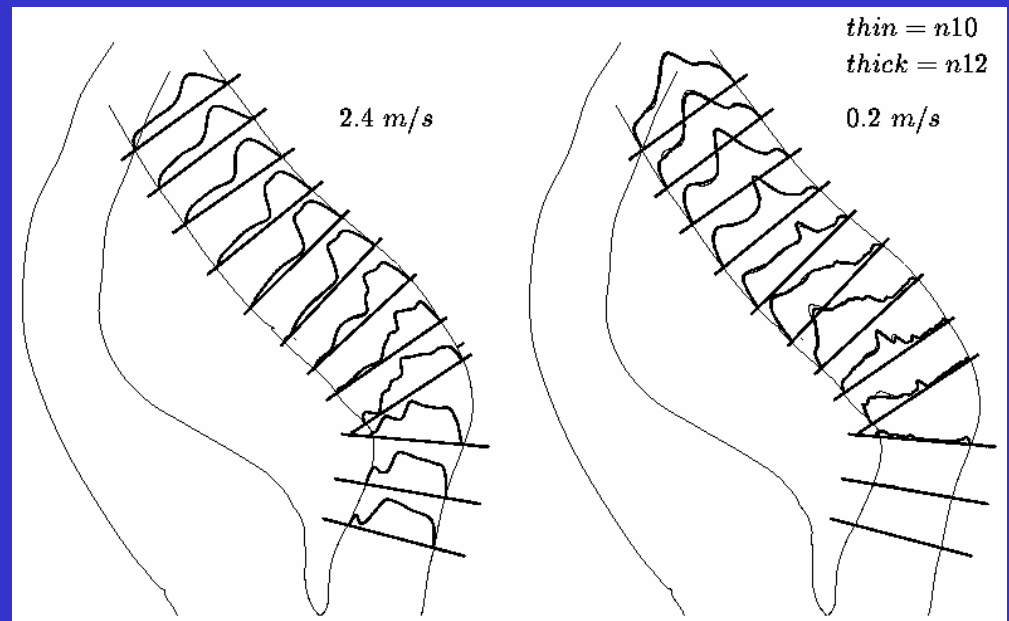
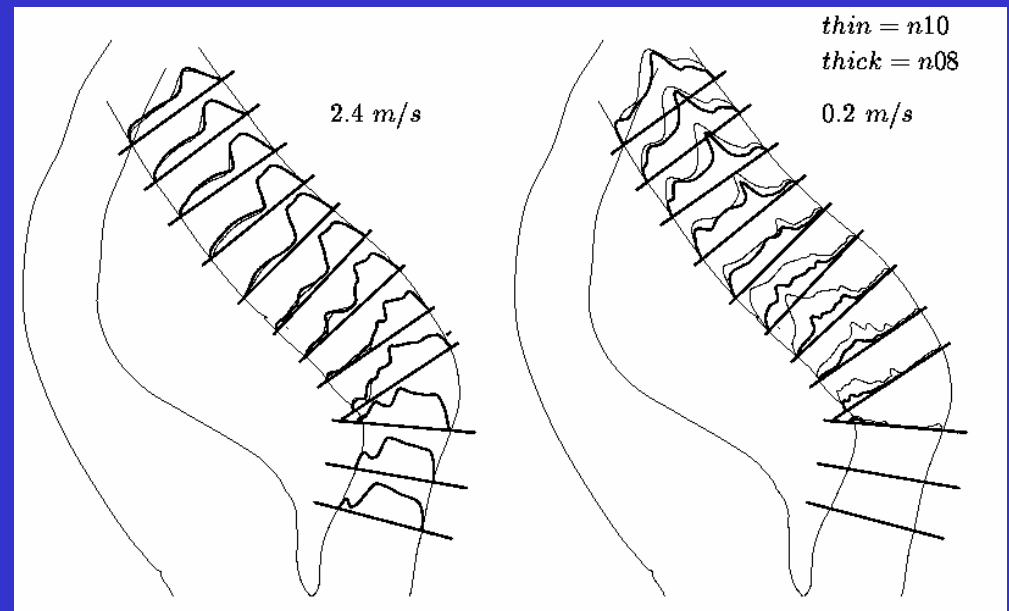
Grid independence test (Steady inlet)

- Comparison between $N = 08$ and $N = 10$

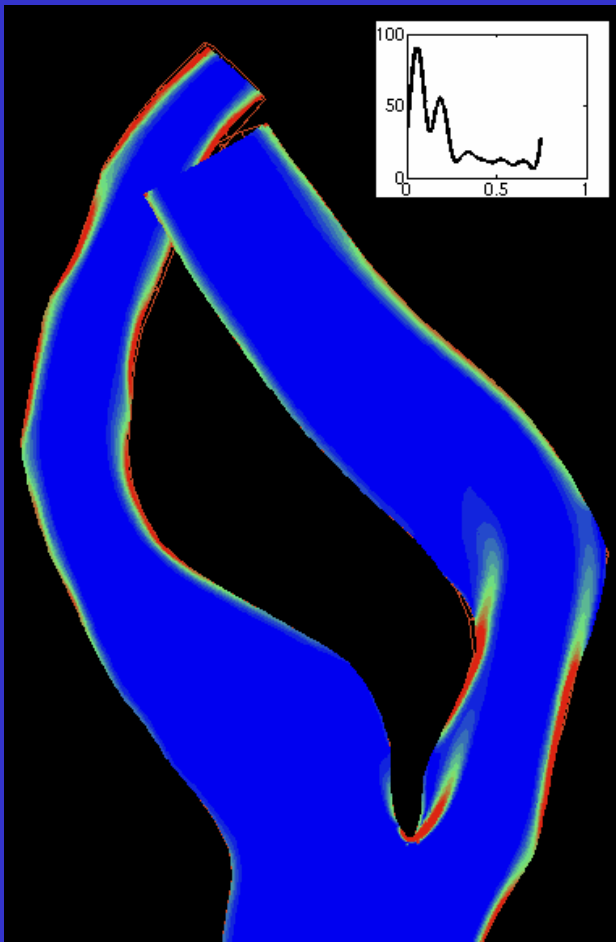
- Left = velocity
- Right = RMS

- Comparison between $N = 10$ and $N = 12$

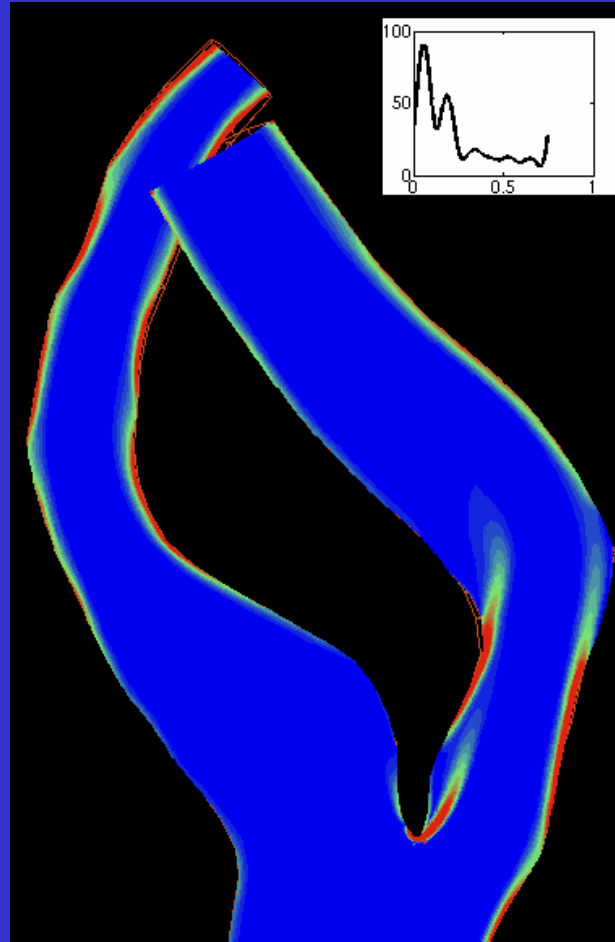
- Left = velocity
- Right = RMS



Vorticity Animation In Stenosed Carotid



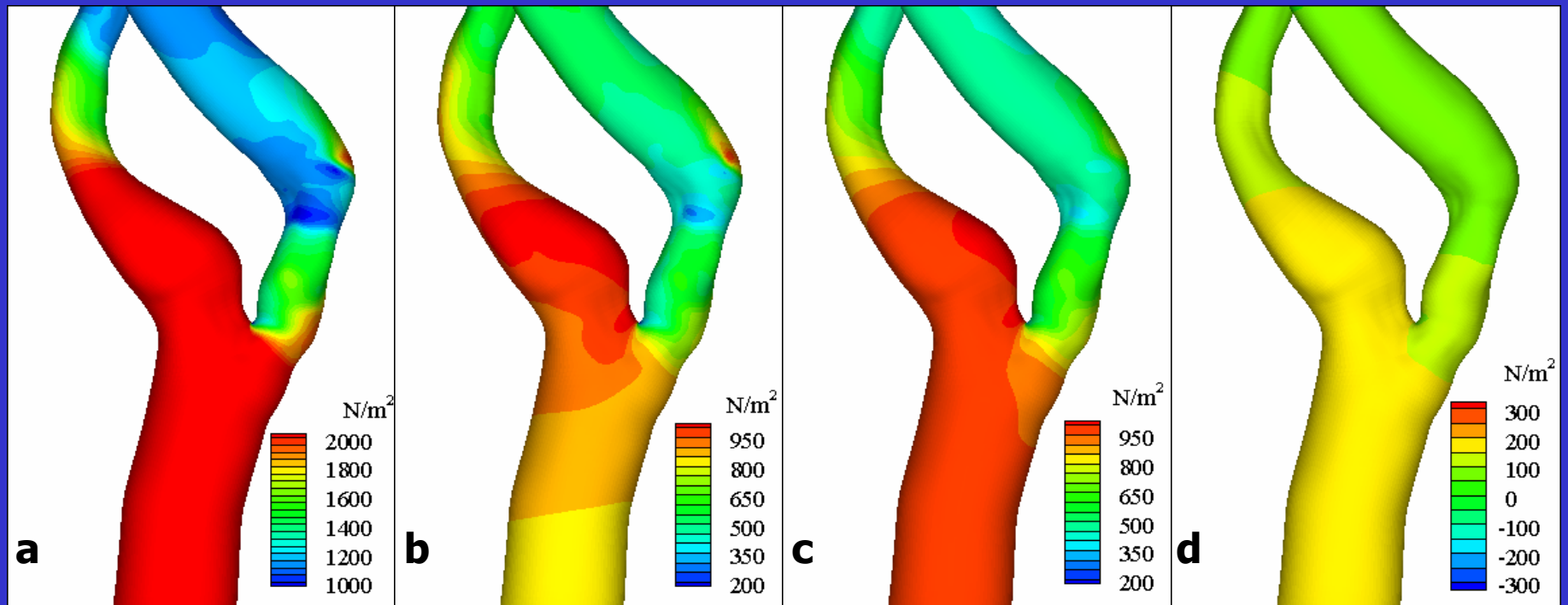
Vorticity at midplane



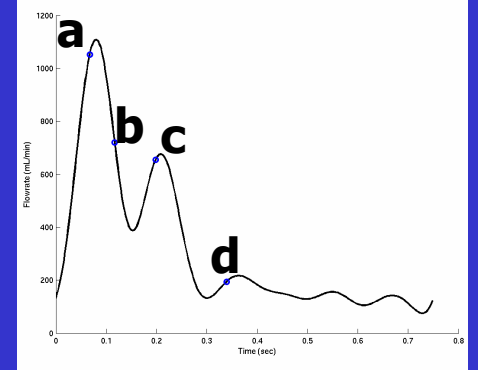
*Vorticity at midplane
Only first peak systole*

- Womersley inlet – flow waveform from Ultrasound
- Constant flow split specification – 59:41 (ICA:ECA)
- Rigid wall
- $N = 10$
- $K = 2544$
- Computation time = 11 hrs with 256 processors

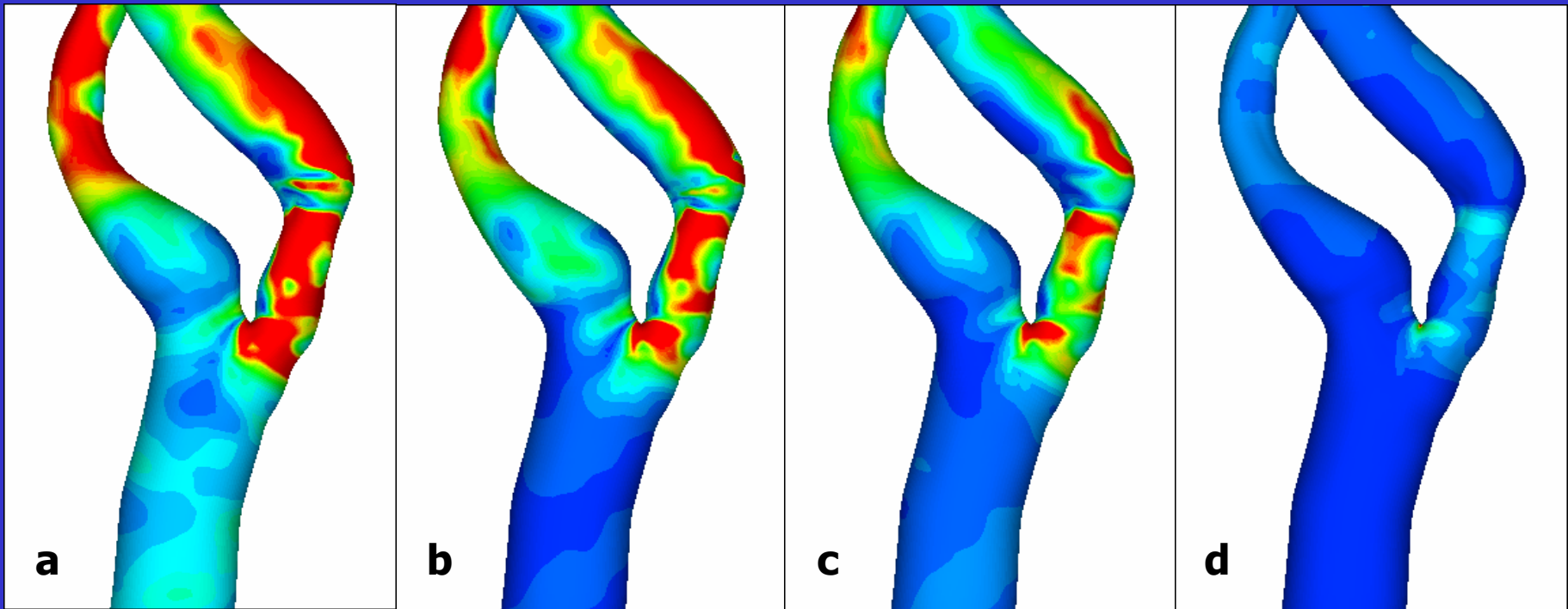
Pressure Distribution



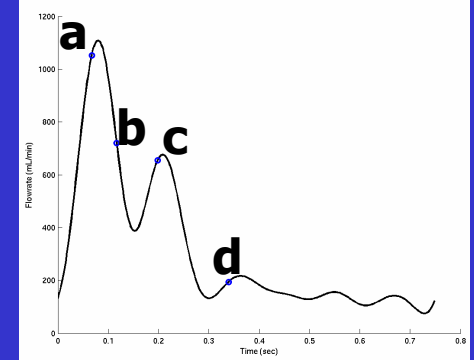
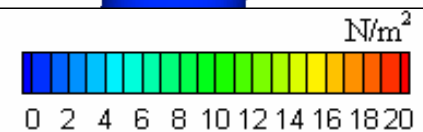
- Low pressure at the throat of stenosis
- Shown to cause collapsing of arterial wall [blah 2000]
- Correlate sharp pressure drop with plaque rupture vulnerability



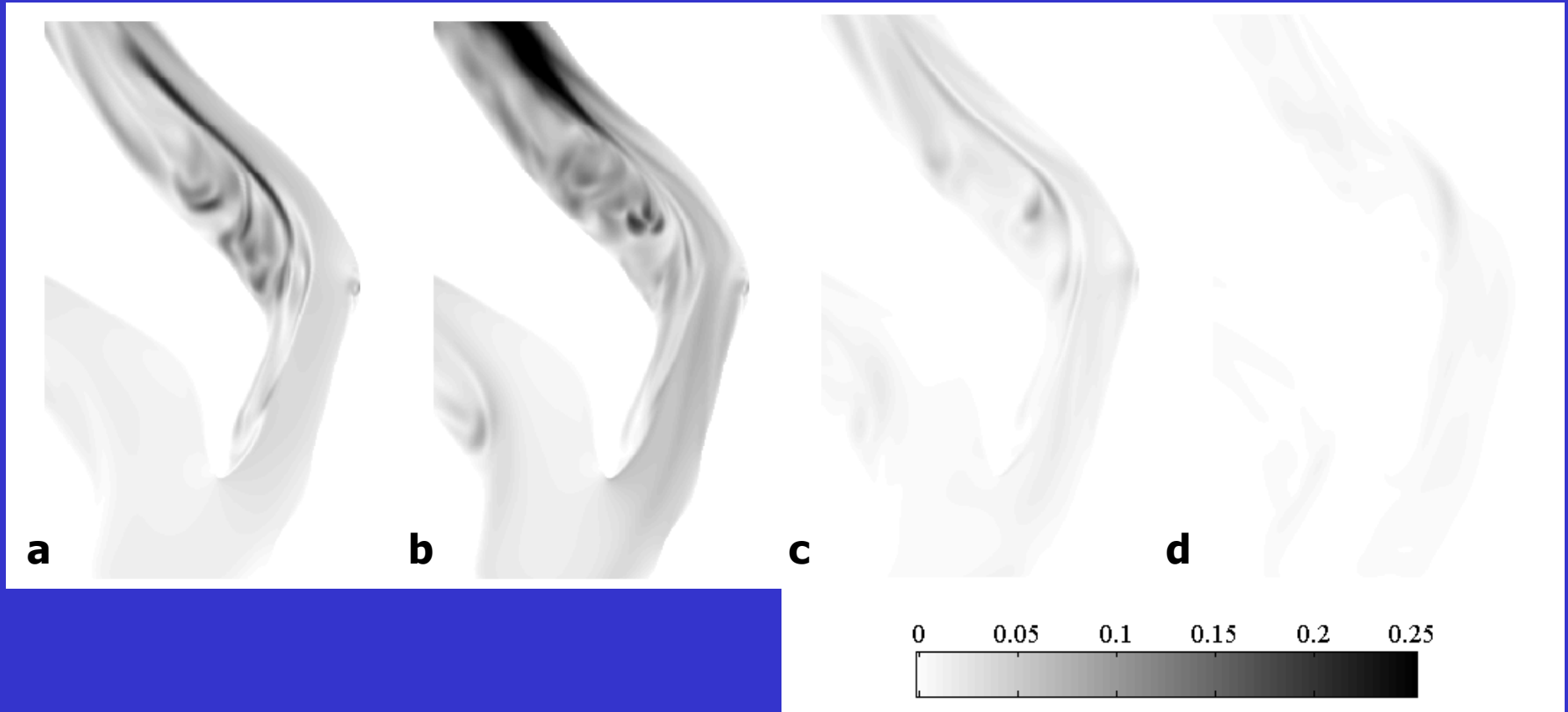
Wall Shear Stress Distribution



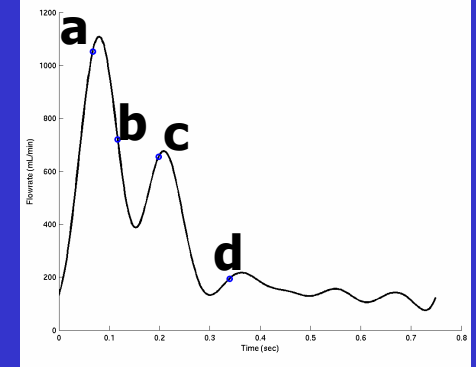
- Distribution of very high and very low WSS – typical value is around 1.5 N/m^2
- Disease progression
- Damage endothelial cells and red blood cells
- Fatigue plaque to cause rupture
- Trigger thrombosis
- Correlation study needed



Turbulence Intensity



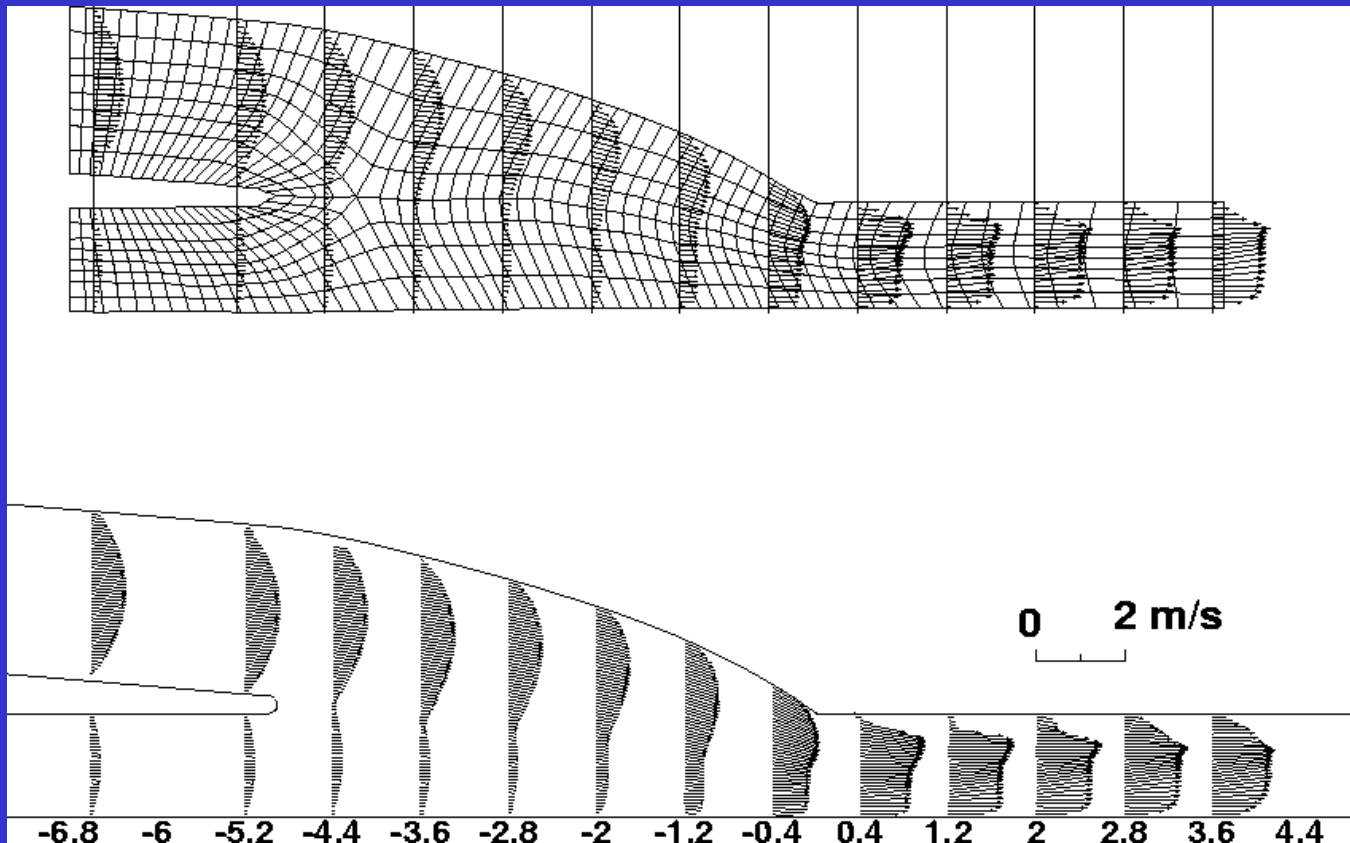
- High mixing intensity downstream of stenosis – activate platelet
- High mixing intensity in the recirculation zone



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AV Graft Velocity Comparison (Inlet Re = 1060 & outlet Re = 1900)

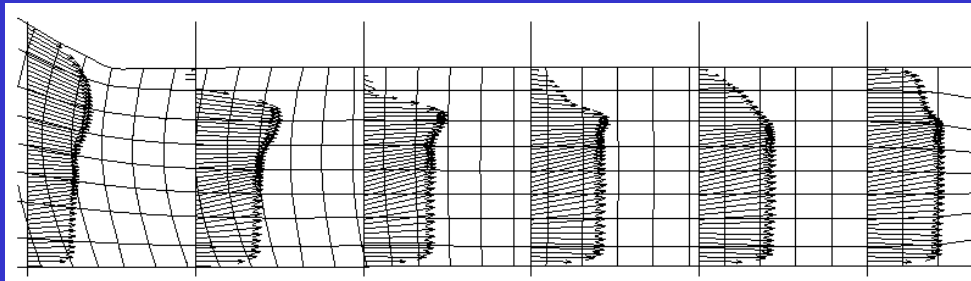


Numerical

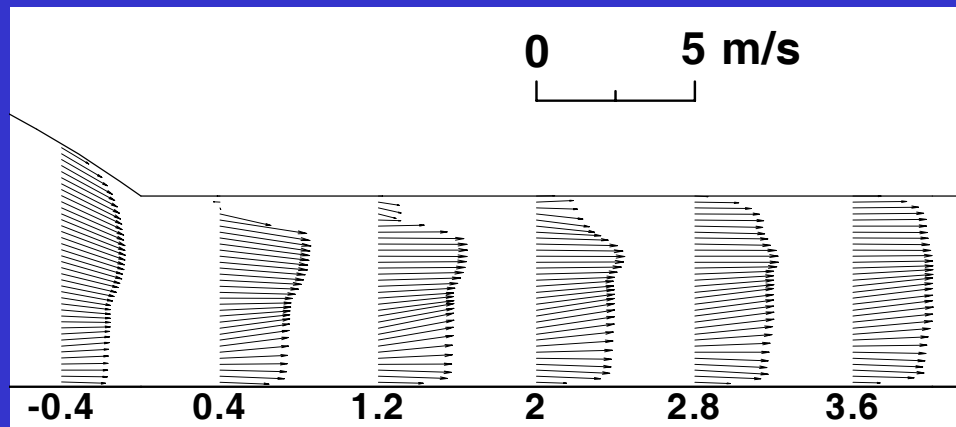
Experimental

Comparison with LDA measurements (Arslan 99)
Steady Flow - Re = 1060

AV Graft Average Velocity Comparison (Inlet Re = 1820 & outlet Re = 3200)



Numerical



Experimental

Velocity profile scaled to *in vivo* values.

Conclusion

- We have develop a methodology to translate a set of *in vivo* medical images to numerical solution of a transitional flow in a stenotic bifurcation
- Patient-specific, full cardiac cycle transitional flow calculation obtainable in 12 hours with 256 processors
- Quantification of flow parameters in stenosed carotid
- Consistent with experimental and other numerical observations

Future Goal

- Further research to correlate arterial disease with hemodynamic parameters
- Non-invasive way to quantify Hemodynamic parameter
 - Diagnostic tool
 - Predictive tool

Ooh...



Check out the vortex shedding frequency off of distal end of your stenosed internal carotid and magnitude of turbulence shearing... **You definitely need an endarterectomy within next 23.7 days...**

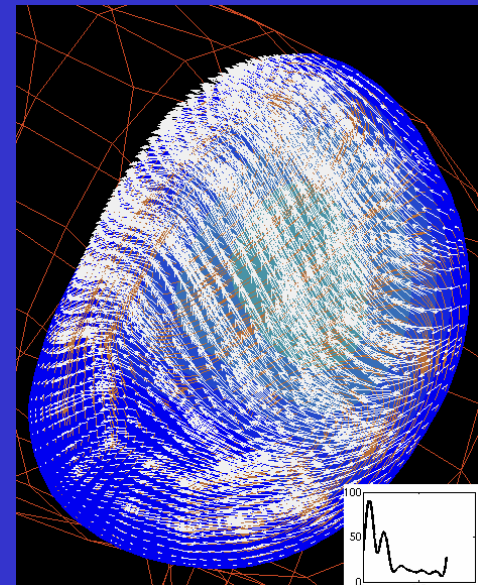
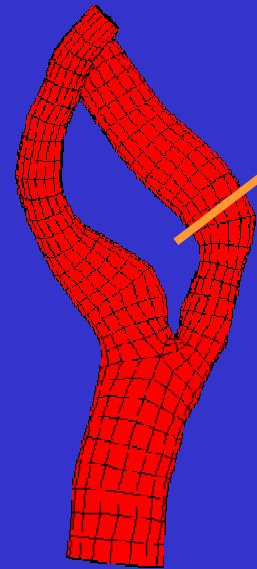
Acknowledgements

- Francis Loth, PhD
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 - UIC Graduate Fellowship
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 - CSGF

- A very special thanks to...

**Computational Science
Graduate Fellowship**





Coherent Vortical Structure

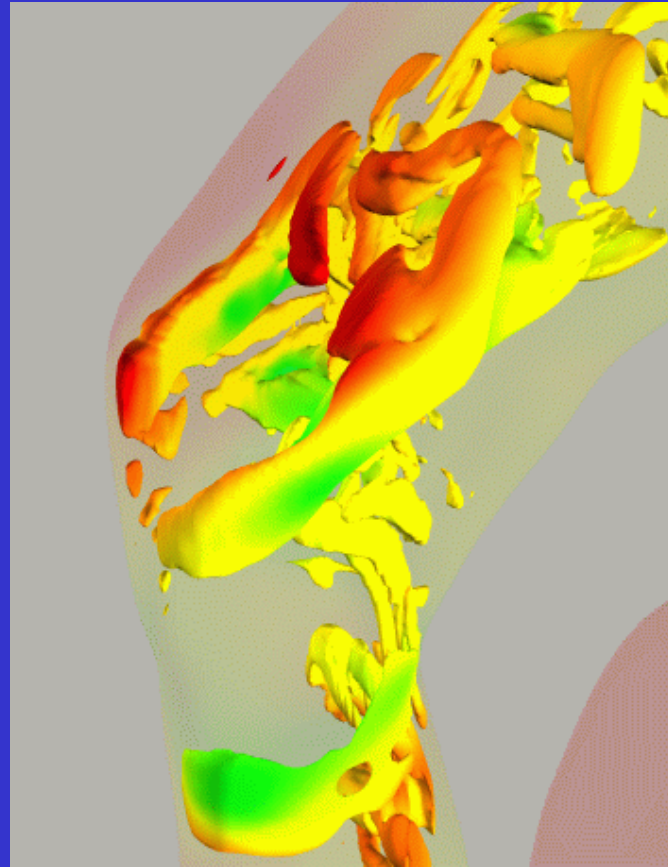
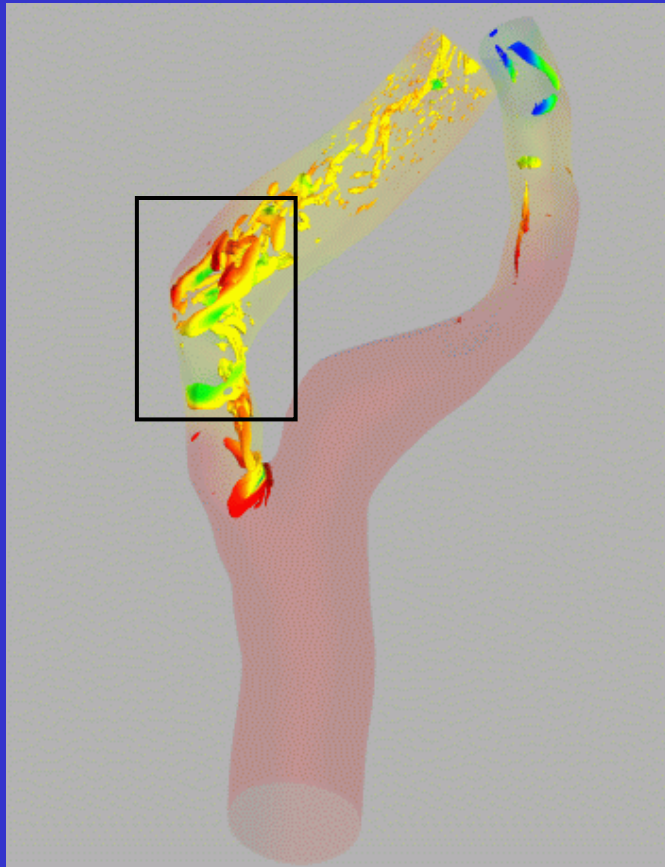
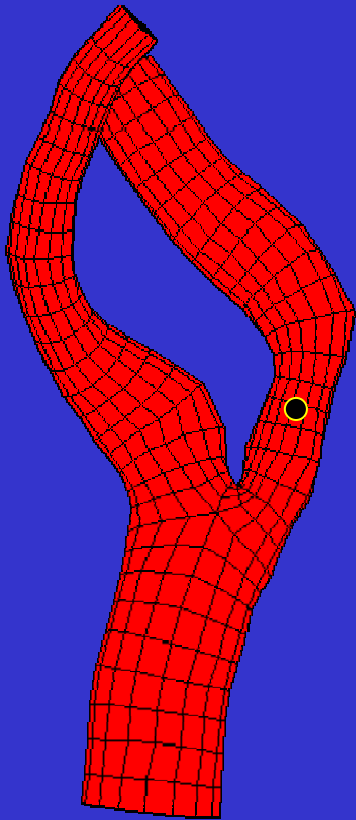
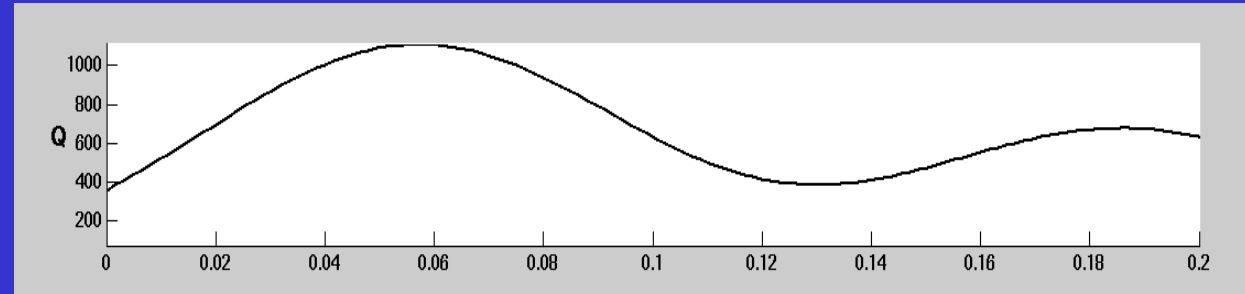


Image created by ANL Visualization Lab using the λ_2 criterion of Jeong & Hussain (JFM'95)

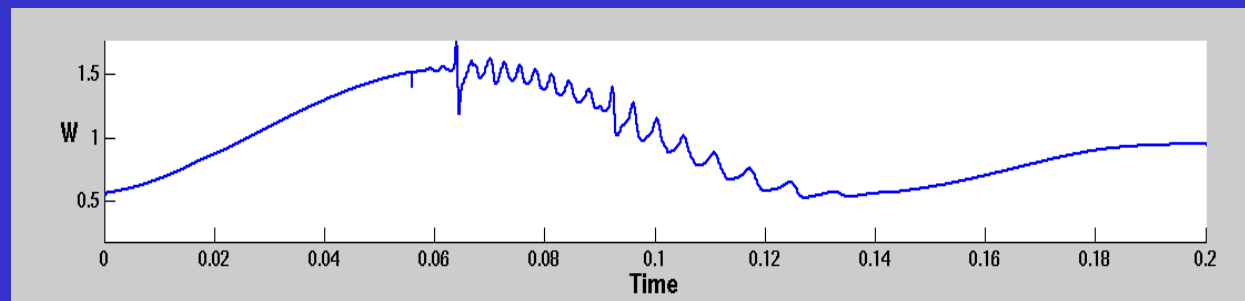
Velocity Time Trace in ICA



Inlet flow waveform

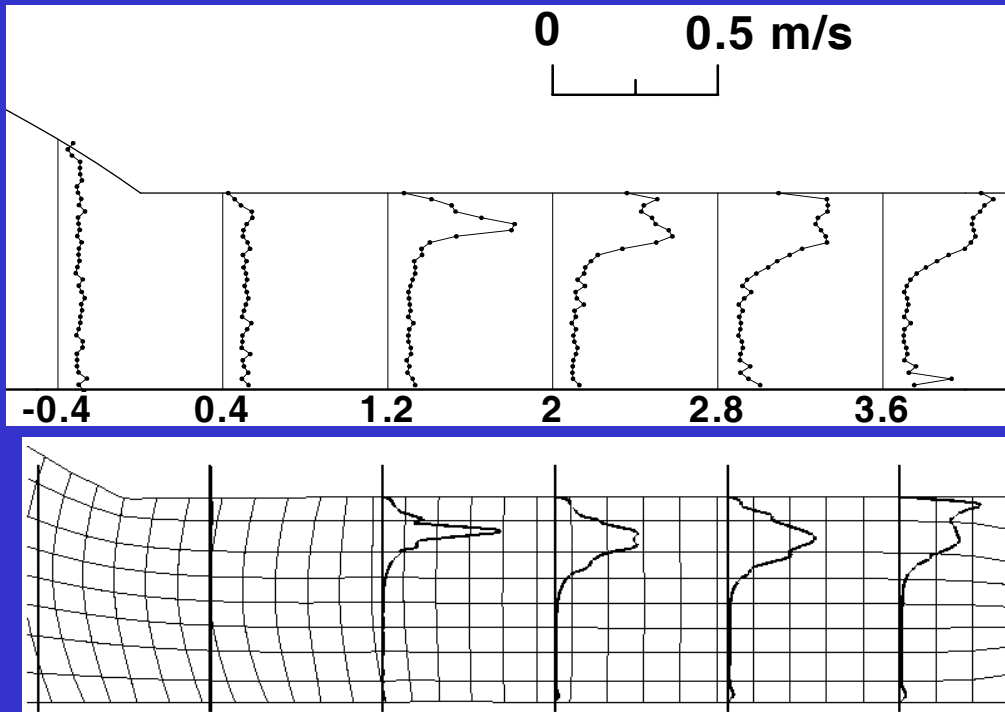


Z-component velocity



- Velocity fluctuation ~ 300 Hz
 - Within audible band (100 – 500 Hz)
- Time step used, $dt = 1e-5$, is much less than $1/300$

Urms (Re=1820)

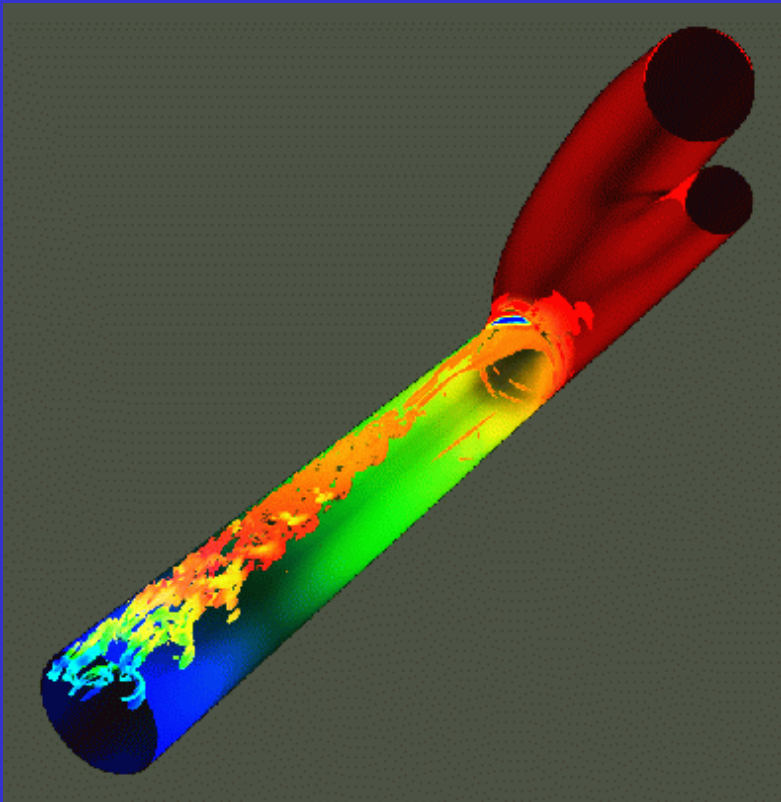


Experimental

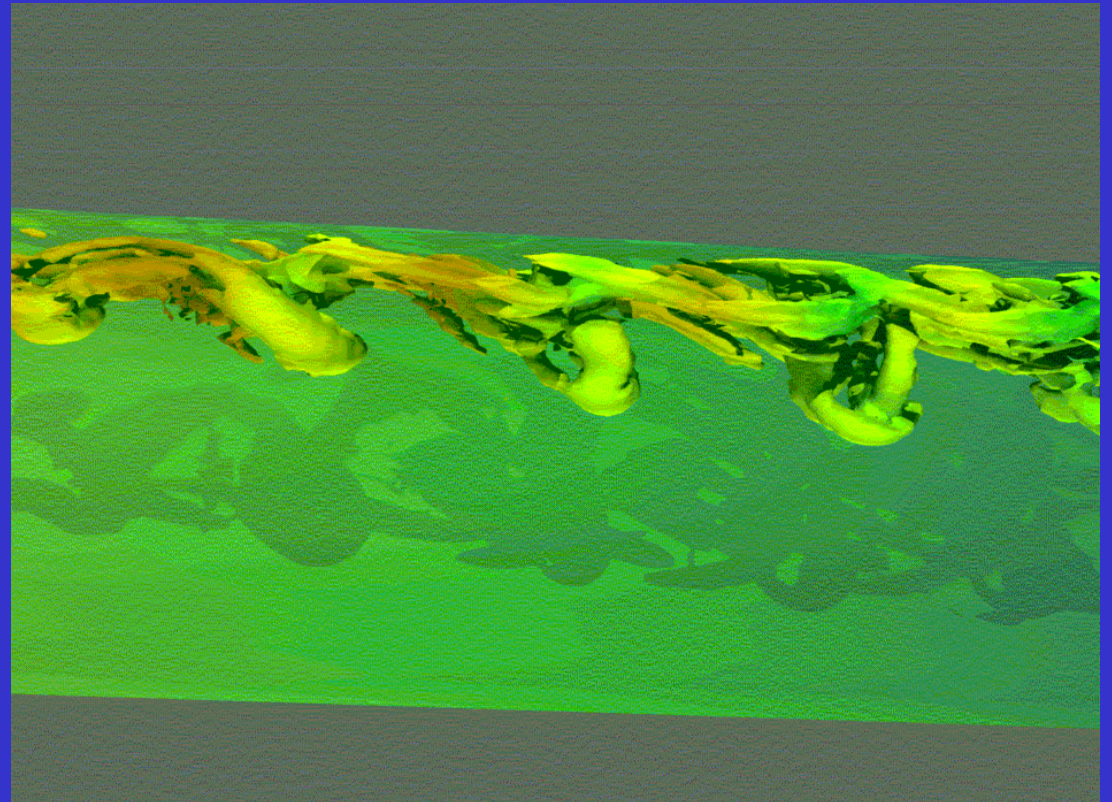
Numerical

Turbulent intensities (U_{rms}) in PVS scaled to in vivo values.

Coherent Vortical Structure



Transitional flow in PVS



Close-up of coherent vortical structures in PVS
visualized with the λ_2 criterion of Jeong & Hussain
(JFM'95)